Supersolidity in Two-dimensional supersolids in the presence of an obstacle

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A supersolid is the state that exhibits Bose-Einstein condensation(BEC) and Bragg peak simultaneously. It has been studied for more than 40 years theoretically and experimentally. After the experiments of Kim and Chan[1] the topic attracts many researchers and many studies have done. Experiments of Cold atoms are also attractive. The realization of supersolids is expected in the BEC of ⁵²Cr[2] and ¹⁶⁴Dy[3] because of their strong magnetic dipole-dipole interaction.

As in theory, Pomeau and Rica[4] showed two-dimensional supersolids do not have supersoridity in the presence of an obstacle in the framework of the

Gross-Pitaevskii(GP) theory. However we expect that as in the one-dimensional case[5], there is superuidity in two-dimensional supersolids.

We solved a modified version of the GP equation[4] with a finite range two-body repulsive interaction. Fig.1 shows the density profile of the macroscopic wave function for velocity v = 0. This solution is a supersolid phase. The ground states are hexagonal in all solid regime where we calculated. The main results are as follows.

First, in the absence of an external potential, we showed the phase diagram of Λ and v, where Λ is a dimensionless parameter which represents the strength of interaction. We obtained the SF(Superuid)-SS(Supersolid) first order phase transition line. In the one-dimensional case[5], the phase transition line is second order.



Figure 1: Density profile for velocity v = 0, potential height $U_0 = 0$ and $\Lambda = 60$. *a* is the interaction length.

Second, in the presence of the external potential that separates the supersolid into two regimes, we showed the Josephson-relation which is the relation between a difference of two macroscopic phase and a current. Similarly to the famous Josephson-relation in Superconductors[6], the relation exhibits superuidity. Similarly to the one-dimensional case[5], in the large U_0 limit the Josephson-relation comes closer to sine. We can also calculate non-classical rotational of inertia fraction in this model.

In this presentation, we will show the detail data and discuss the properties of two-dimensional supersolids and supersolidity.

References

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