

# Microwave Resonance of Wigner Crystal Phase around Integer Quantum Hall States

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We have observed, by microwave absorption spectroscopy, a well defined resonance in the real part of frequency-dependent diagonal conductivity ( $\text{Re}[\sigma_{xx}(f)]$ ) of high quality 2DES *near integer filling factors*.

Figure 1 and Figure 2 show the resonances observed around  $\nu = 1$  and  $\nu = 2$  respectively. The measurements were performed in a dilution refrigerator at its base temperature of 50mK, using a GaAs/AlGaAs quantum well sample with density  $n = 3.0 \times 10^{11} \text{ cm}^{-2}$  and mobility about  $2.4 \times 10^7 \text{ cm}^2 \text{ V}^{-1} \text{ s}^{-1}$ . Similar resonances around  $\nu = 3$  and  $\nu = 4$  have also been observed on this sample, although they are significantly weaker compared to those around  $\nu = 1$  and  $\nu = 2$ .

Fig. 1(A) displays a series of  $\text{Re}[\sigma_{xx}(f)]$  spectra measured at filling factors ( $\nu$ ) between 0.78 and 1.22. The resonance is observable for  $0.84 < \nu < 0.96$  and  $1.04 < \nu < 1.16$ . Within either of these  $\nu$  ranges, the resonance shifts to higher frequency as  $\nu \rightarrow 1$  and is sharpest when  $\nu$  is  $\sim 0.9$  or  $1.1$ . In Fig. 1(B) and (C) we plot the peak frequency ( $f_{\text{pk}}$ ) and full width at half maximum ( $\Delta f$ ) of the resonance as functions of  $\nu$ , where  $f_{\text{pk}}$  and  $\Delta f$  are extracted from Lorentzian fit of the resonance. We see  $f_{\text{pk}}$  monotonically increases as  $\nu \rightarrow 1$  and  $\Delta f$  has minima at  $\nu \sim 0.9$  and  $\nu \sim 1.1$ , where the resonance has quality factor  $Q$  (defined as  $f_{\text{pk}}/\Delta f$ ) about 3. In similar fashion to Fig. 1, we show in Fig. 2(A) a series of  $\text{Re}[\sigma_{xx}(f)]$  spectra at filling factors around 2 (from 1.75 to 2.25), where the resonance is observable for  $1.77 < \nu < 1.92$  and  $2.05 < \nu < 2.15$ , and in Fig. 2(B)(C) we plot the extracted  $f_{\text{pk}}$  and  $\Delta f$  as functions of  $\nu$ . In this case  $f_{\text{pk}}$  monotonically increases as  $\nu \rightarrow 2$  and  $\Delta f$  is found to have minima at  $\nu \sim 1.85$  and  $\nu \sim 2.12$ .

We have also studied the temperature ( $T$ ) dependence of the resonance. With increasing  $T$ ,  $\Delta f$  monotonically increases whereas  $f_{\text{pk}}$  is relative insensitive. The resonance disappears for  $T$  above  $\sim 200$  mK.

We interpret the resonance as the signature of 2D Wigner crystal phase formed around integer Landau fillings, by the electrons/holes in the partially filled top Landau level with effective filling factor  $\nu^*$  (where  $\nu^* = \nu - K$  for filling factor  $\nu$  around positive integer  $K$ ) and density  $n^* = (n/\nu)\nu^*$ . The “pinning mode”[1], caused by such Wigner crystalline domains oscillating in impurity potential, gives rise to the observed resonance. The collective many-particle nature of this resonance is reflected by the high  $Q$  achieved and the existence of resonance at temperature several times higher than that corresponding to its resonating frequency ( $hf_{\text{pk}}/k_B$ ).

Wigner crystal has been conjectured to be the ground state of a sufficiently clean 2DES at  $\nu = K + \nu^*$  for small enough  $\nu^*$  and positive integer  $K$ [2], as in the case of  $K = 0$  (that is, in the lowest Landau level (LLL))[3]. The LLL ( $K = 0$ ) Wigner crystal has been supported by, for example, previous observations of similar resonance at small  $\nu$  in LLL for both 2DES and 2D hole systems[4]. The feature of  $f_{\text{pk}}$  increasing with decreasing density also observed in these experiments, is consistent with the weak-pinning picture[5].

Our observation also indicates that the pinning of a many-particle ground state such as Wigner crystal, can be relevant for IQHE, which has traditionally been explained by a disorder induced single-particle localization mechanism.

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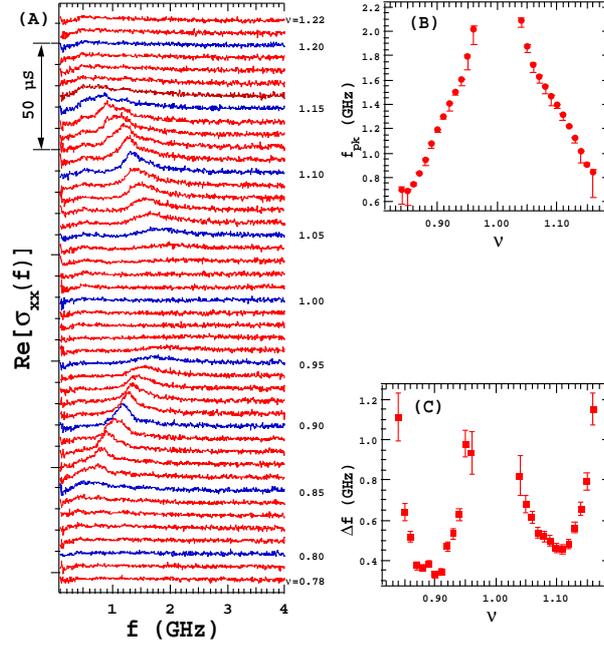


FIG. 1: (A)  $\text{Re}[\sigma_{xx}(f)]$  spectra around  $\nu = 1$ : from  $\nu = 0.78$  (bottom trace) to  $\nu = 1.22$  (top trace). Adjacent traces differ 0.01 in  $\nu$  and are offset  $6 \mu\text{S}$  from each other for clarity. Filling factors for selected traces are labeled at right. Measurements performed at  $\sim 50 \text{ mK}$ . (B)  $f_{\text{pk}}$  versus  $\nu$ . (C)  $\Delta f$  versus  $\nu$ .

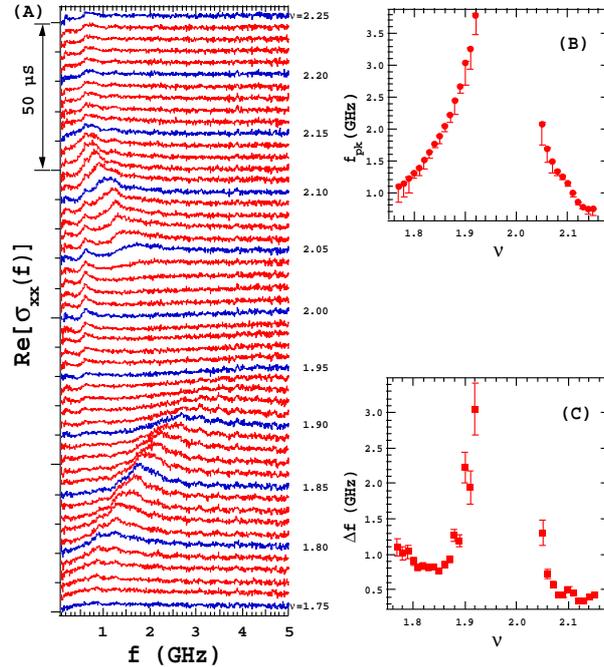


FIG. 2: (A)  $\text{Re}[\sigma_{xx}(f)]$  spectra around  $\nu = 2$ : from  $\nu = 1.75$  (bottom trace) to  $\nu = 2.25$  (top trace). Adjacent traces differ 0.01 in  $\nu$  and are offset  $4 \mu\text{S}$  from each other for clarity. Filling factors for selected traces are labeled at right. Measurements performed at  $\sim 50 \text{ mK}$ . (The small spike near 600 MHz in some traces is likely due to an experimental artifact). (B)  $f_{\text{pk}}$  versus  $\nu$ . (C)  $\Delta f$  versus  $\nu$ .