

THE EFFECT OF SPIN WAVES IN THE SPIN SEEBECK EFFECT

Joseph Barker, Gerrit Bauer

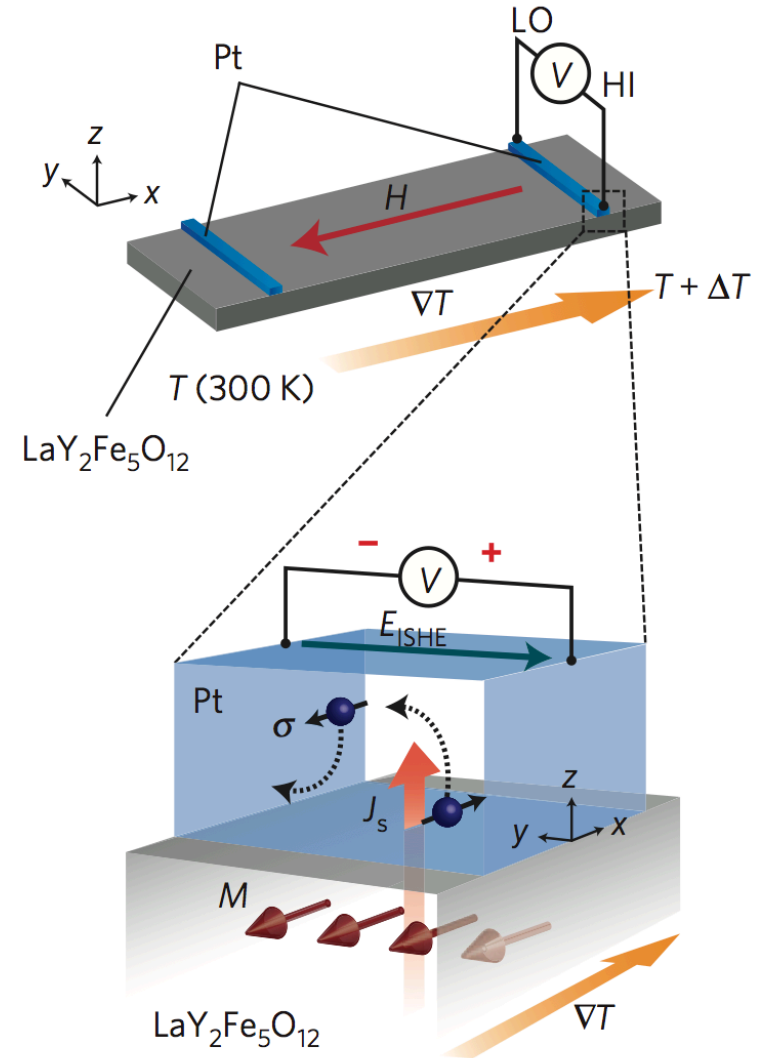
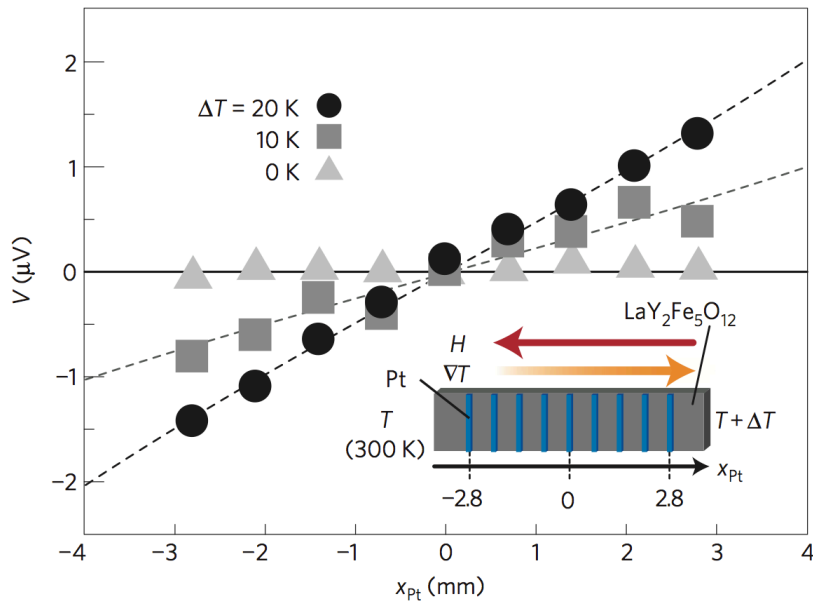
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Net spin current injected into Pt

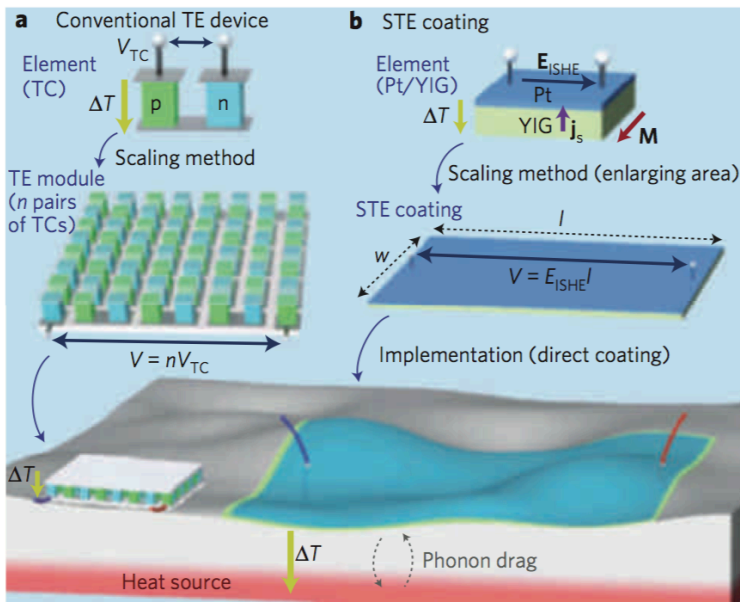
$$J_s = \frac{\gamma \hbar}{2\pi M_s V} \text{Re}[g_{\uparrow\downarrow}] k_B (T_F - T_N)$$



K. Uchida et al., Nature Mater. **9**, 894 (2010).

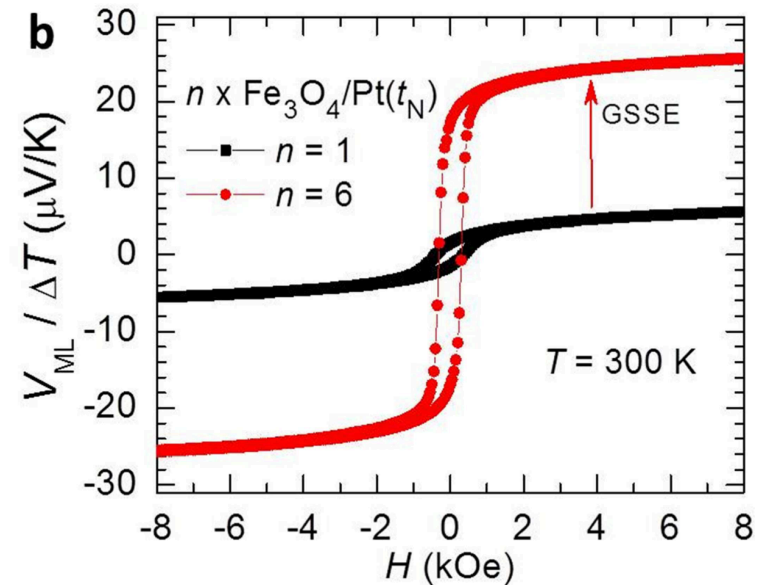
J. Xiao et al., Phys. Rev. B **81**, 214418 (2010).

Ability to coat surfaces in continuous films



A. Kirihara et al.,
Nature Mater. **11**, 686 (2012).

Enhancement using multilayers



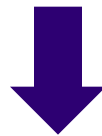
R. Ramos et al.,
arXiv **cond-mat.mtrl-sci**, (2015).

Transverse dynamical susceptibility

Not known in general and enters the spin current term.

$$J_s = \frac{M_s V}{\gamma} \left(\frac{\alpha_N}{\alpha_F} \sigma_N^2 - \sigma_F^2 \right) \int \chi_{xy}(\omega) - \chi_{yx}(\omega) d\omega$$

$$\sigma_{F,N}^2 = \frac{2\alpha_{F,N}\gamma k_B T_{F,N}}{M_s V}$$

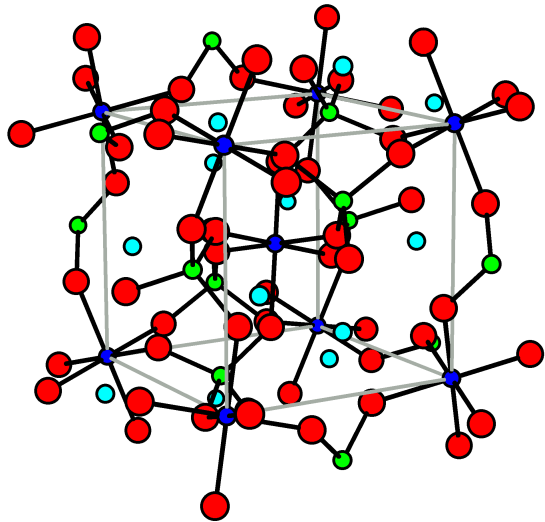


Assumption of simple FM

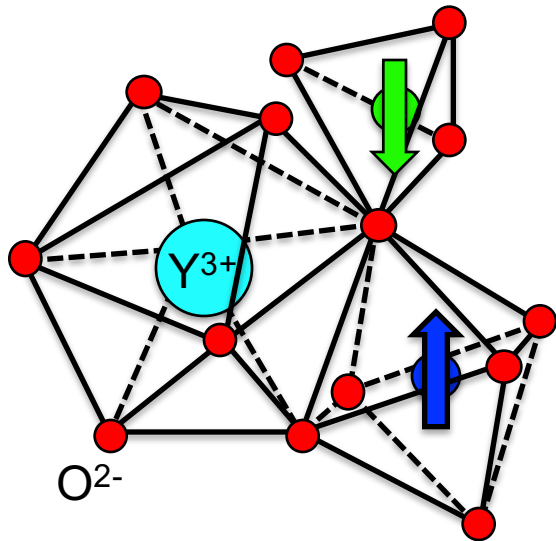
$$\alpha_N = \frac{\gamma \hbar}{4\pi M_s V} \text{Re}[g_{\uparrow\downarrow}]$$

$$J_s = \frac{\gamma \hbar}{2\pi M_s V} \text{Re}[g_{\uparrow\downarrow}] k_B (T_F - T_N)$$

Even exchange spin wave dispersion will determine the result.

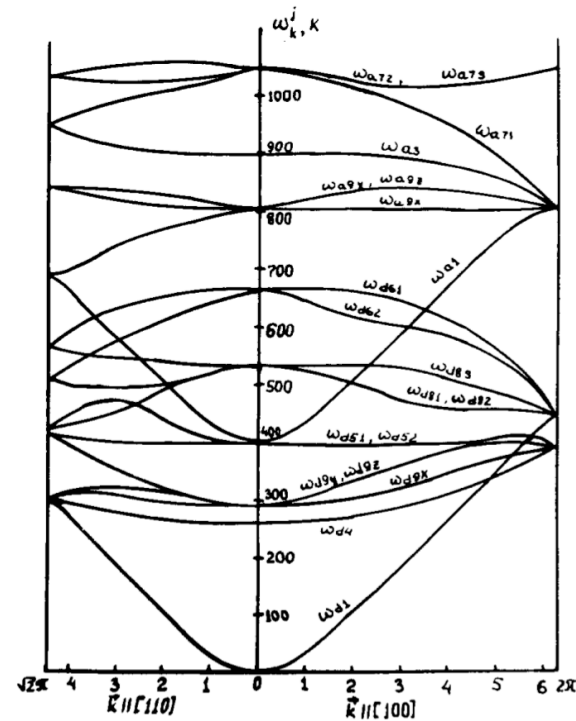


Fe³⁺ Tetrahedral (d)



Fe³⁺ Octahedral (a)

Spin wave spectrum of YIG



V. Cherepanov et al., Phys. Rep. **229**, 81 (1993)

$$\mathcal{H} = - \sum_{ij} J_{ij} \mathbf{S}_i \cdot \mathbf{S}_j$$

Nearest neighbour exchange interactions

$$J_{ad} = -39.8 \text{ K} \quad J_{dd} = -13.4 \text{ K} \quad J_{aa} = -3.8 \text{ K}$$

V. Cherepanov et al. *Phys. Rep.* **229**, 81 (1993)

Landau-Lifshitz-Gilbert

Equation of motion for a classical spin in a local field.

$$\frac{\partial \mathbf{S}_i}{\partial t} = -\frac{\gamma_i}{(1 + \alpha_i^2)} (\mathbf{S}_i \times \mathbf{H}_i + \alpha_i \mathbf{S}_i \times \mathbf{S}_i \times \mathbf{H}_i)$$

Langevin thermostat

Equation of motion for a classical spin in a local field.

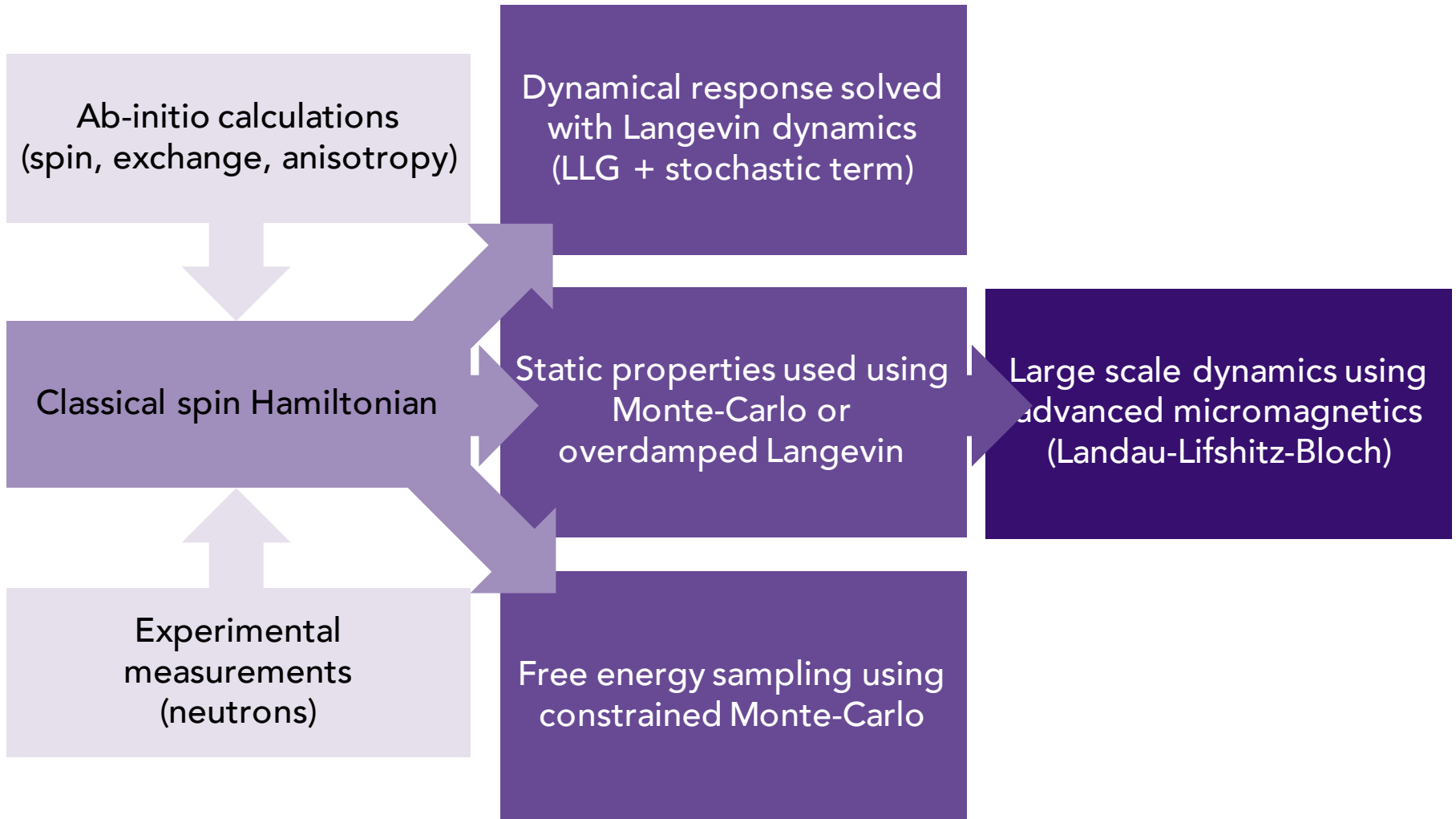
$$\mathbf{H}_i(t) = -\frac{\partial \mathcal{H}}{\partial \mathbf{S}_i} - \eta \int_{-\infty}^t \varphi(t - t') \frac{d\mathbf{S}_i}{dt'} dt' + \boldsymbol{\xi}_i(t)$$

$$\langle \xi_{i,a}(t) \rangle = 0$$

$$\langle \xi_{i,a}(t), \xi_{j,b}(t') \rangle = 2k_B T \eta \varphi(|t - t'|) \delta_{ij} \delta_{ab}$$

$$\varphi(|t - t'|) = \delta(|t - t'|)$$

White noise is usually used, coloured noise adds significant computational overhead.



Atomistic model allows the study of finite temperature effects
Spin wave interactions to arbitrary order

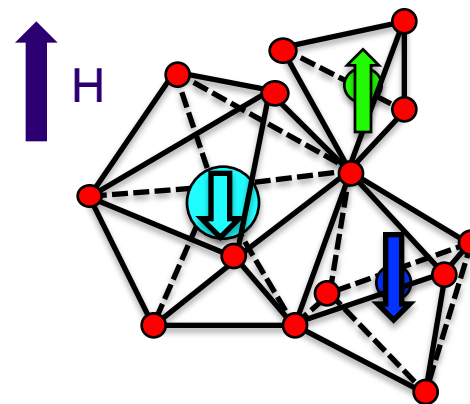
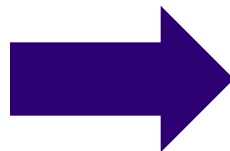
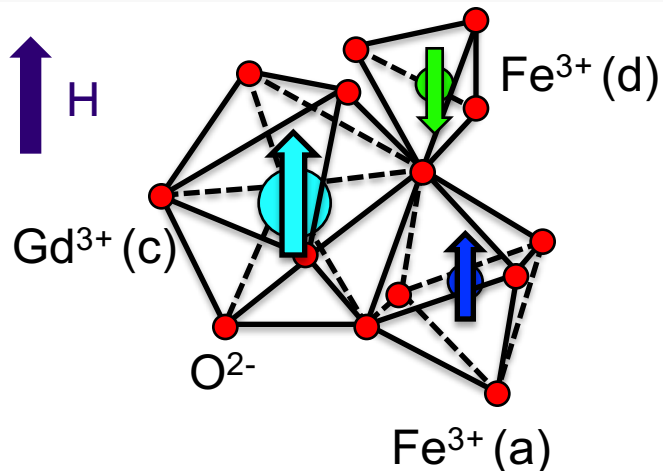
$$S_k(\mathbf{q}, \omega) = \frac{1}{\mathcal{N}\sqrt{2\pi}} \sum_{\mathbf{r}, \mathbf{r}'} e^{i\mathbf{q}\cdot(\mathbf{r}-\mathbf{r}')} \int_{-\infty}^{+\infty} e^{i\omega t} C_k(\mathbf{r} - \mathbf{r}', t) dt$$

Spin-spin correlation function

$$C_k(\mathbf{r} - \mathbf{r}', t) = \langle S_k(\mathbf{r}, t) S_k(\mathbf{r}', 0) \rangle - \langle S_k(\mathbf{r}, t) \rangle \langle S_k(\mathbf{r}', 0) \rangle$$

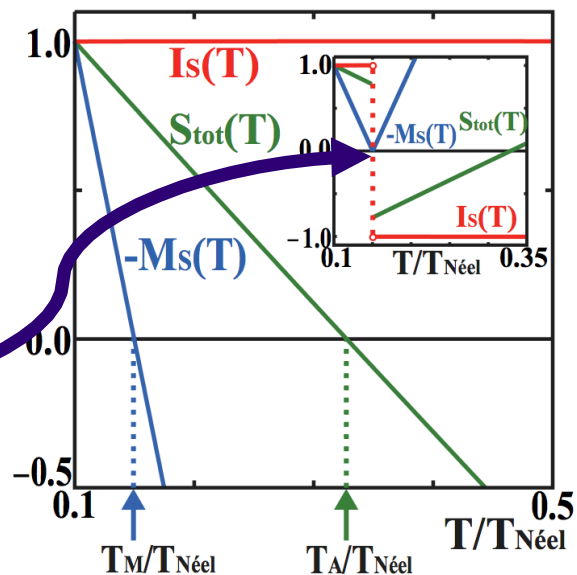
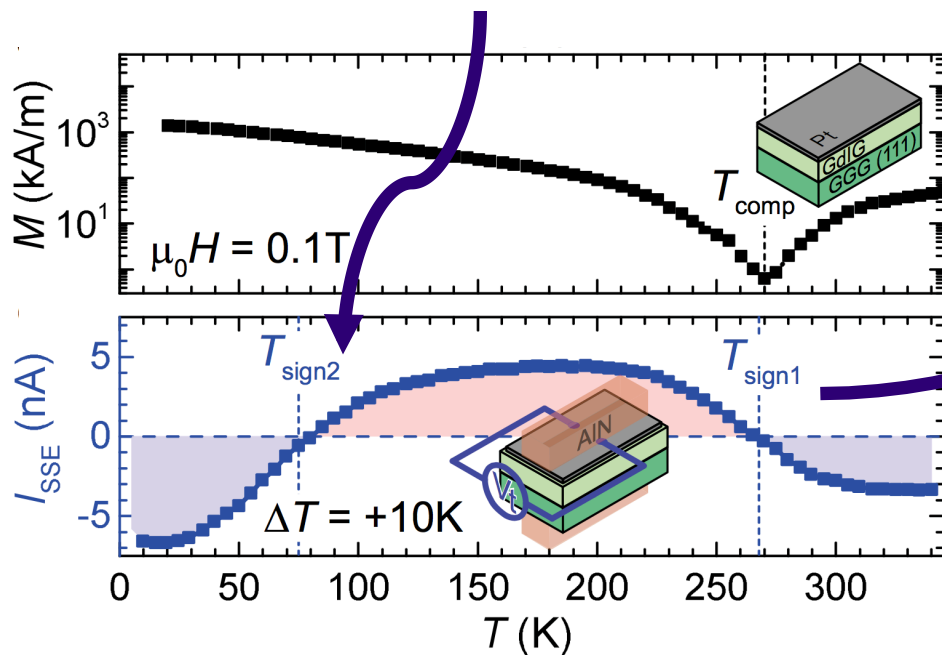
- ❖ Space-time Fourier transform
- ❖ The same quantity is measured in neutron scattering
- ❖ K-space resolution is limited by lattice size
- ❖ Frequency resolution is limited by simulation time

GIG – TWO SSE SIGN CHANGES



No macroscopically observable changes ?

Reorientation through T_{comp} reverses SSE sign



Y. Ohnuma et al.

Phys. Rev. B **87**, 014423 (2013).



- ❖ Quantitative analysis for direct comparison to experiments.
- ❖ Many different rare-earth iron garnets to investigate.
- ❖ Look at interface effects including disorder.
- ❖ Improve understanding to maximize the voltage from SSE.