

Universal Fermi liquid crossover and quantum criticality in a mesoscopic device

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Collaborators:

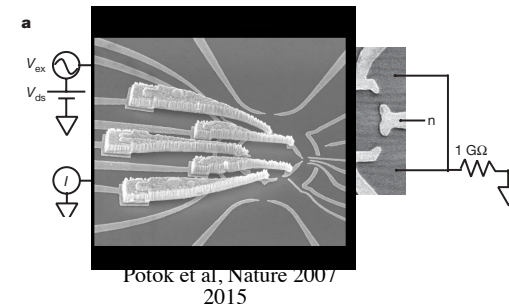
Experiments: Stanford: **Andrew Keller**
Lucas Peeters
David Goldhaber-Gordon
 Weizmann: **D. Mahalu and V. Umansky**

Theory: Budapest: **Pascu Moca**
 Poznan: **Ireneusz Weymann**

A. Keller et al, preprint [arxiv.org/1504.07620](https://arxiv.org/abs/1504.07620)

NPSMP Symposium, Tokyo, 2015

Choice of device

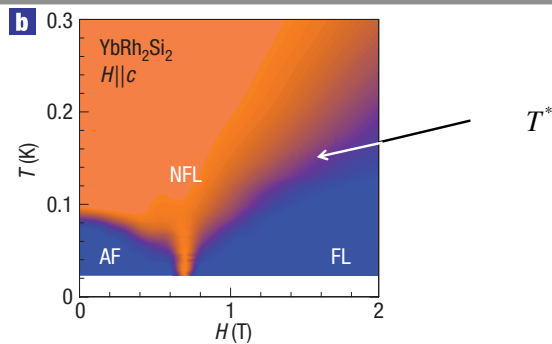


Tunable charge and spin 2-channel Kondo effect

Other possibilities:

Dissipative transitions: Mebrahtu et al, Nature Physics (2013)
 2-channel device (Frederic Pierre's group, 2015)

MOTIVATION

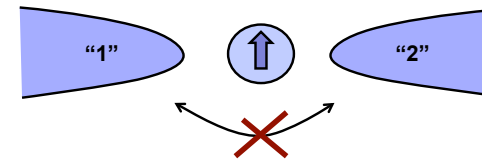


Gegenwart, Si, Steglich, Nature Physics (2008)

Goal: control/investigate QPT in a nano-device and address

- ➡ **fate of FL scale (T^*) ???**
- ➡ **universal cross-over ???**

The 2-channel Kondo „phase diagram”



Kondo Hamiltonian

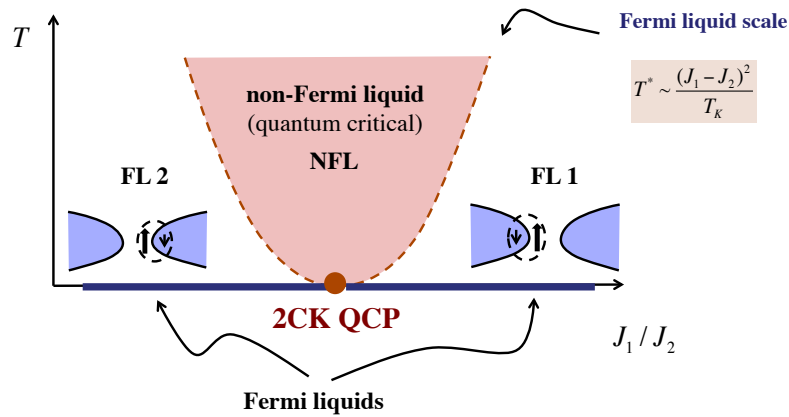
$$H_{\text{int}} = J_1 \underline{S} \cdot \underline{\sigma}_1 + J_2 \underline{S} \cdot \underline{\sigma}_2$$

- No charge transfer between "1" and "2"
- Competition between channels "1" and "2"

➡ **Quantum phase transition**

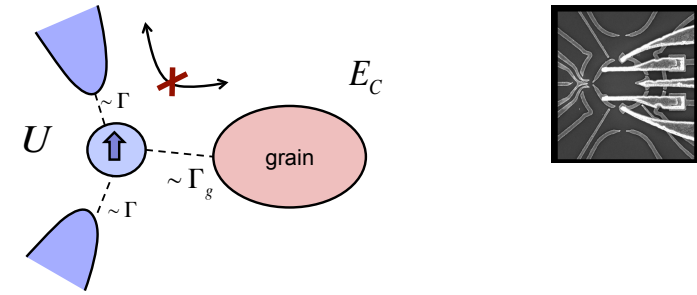
The 2-channel Kondo quantum criticality (2)

“Phase diagram”



Universal non-FL to FL cross-over at T^* !

The Oreg - Goldhaber-Gordon (OGG) device



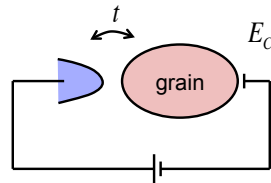
- charge transfer to grain forbidden at energies $\epsilon, T \ll E_C$
- grain (Γ_g) and leads (Γ) compete to screen the spin

Oreg and Goldhaber-Gordon, PRL (2003); Potok et al., Nature (2007)

Other (possible) 2-channel Kondo realizations

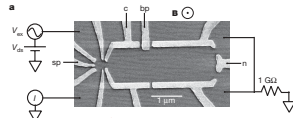
- Heavy fermion (U and Ce-based) materials
large SO coupling + crystal field

- Matveev's mapping
charge 2-channel Kondo effect
 $N = 0 \leftrightarrow 1$
spin = channel index



- Two-level systems ?

- Oreg – Goldhaber-Gordon (OGG) proposal

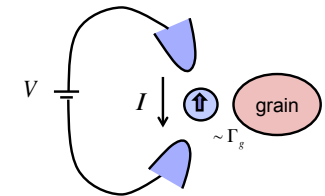


The Oreg - Goldhaber-Gordon device (2): transport in 1 electron limit

operate in 1 electron regime

$T \approx 0$

$\frac{dI}{dV}$



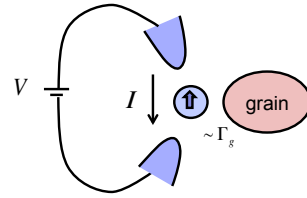
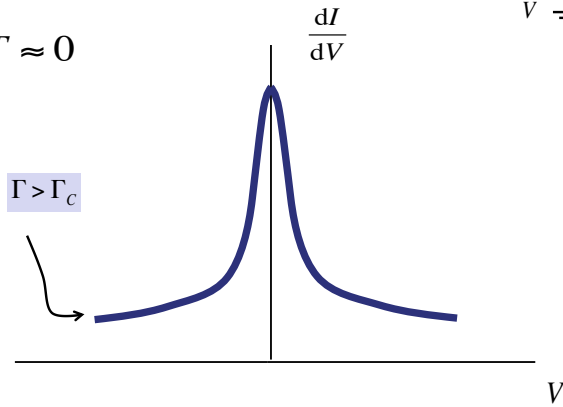
?

V

The Oreg - Goldhaber-Gordon device (2):
transport in 1 electron limit

operate in 1 electron regime

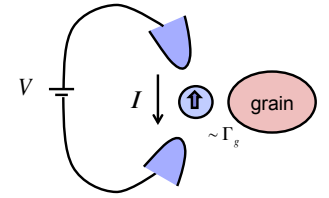
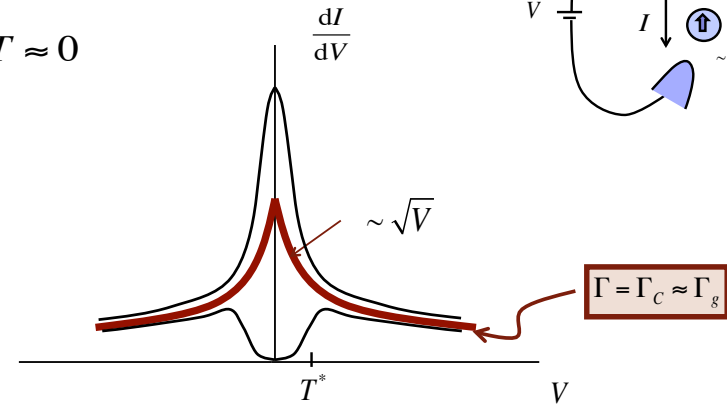
$T \approx 0$



The Oreg - Goldhaber-Gordon device (2):
transport in 1 electron limit

operate in 1 electron regime

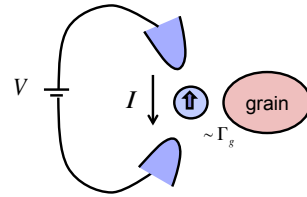
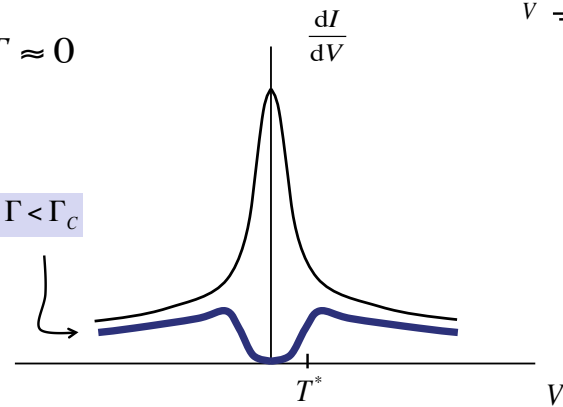
$T \approx 0$



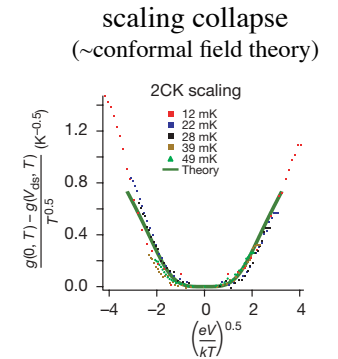
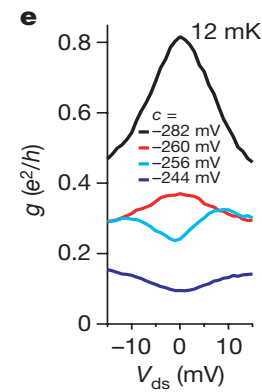
The Oreg - Goldhaber-Gordon device (2):
transport in 1 electron limit

operate in 1 electron regime

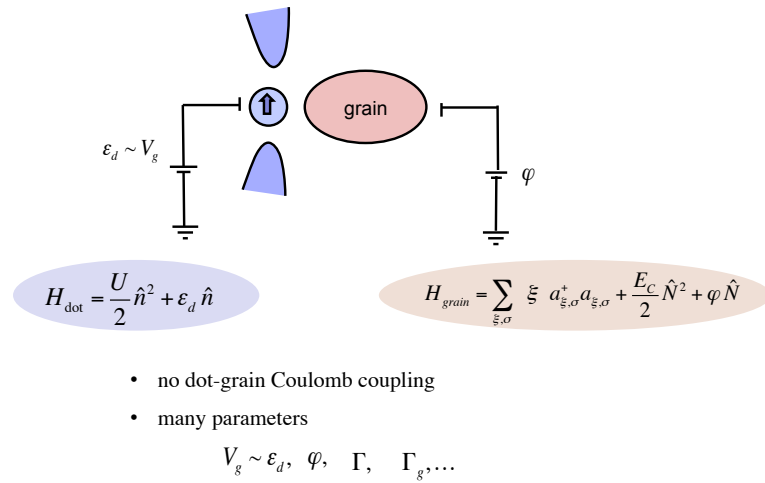
$T \approx 0$



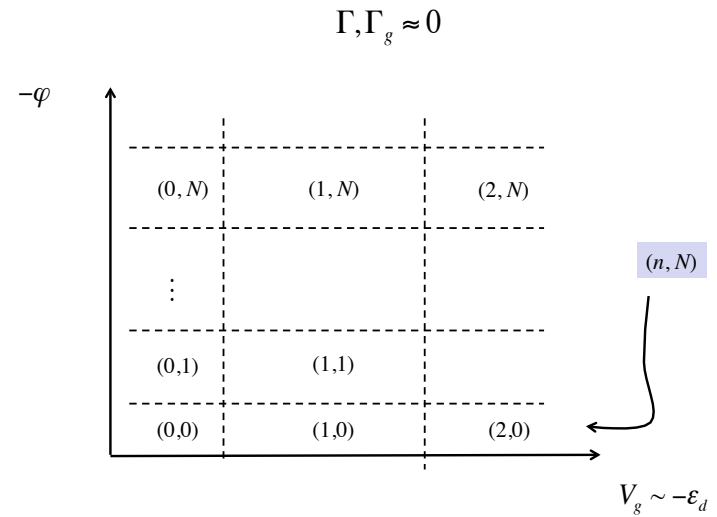
The Oreg - Goldhaber-Gordon device (2):
transport in 1 electron limit



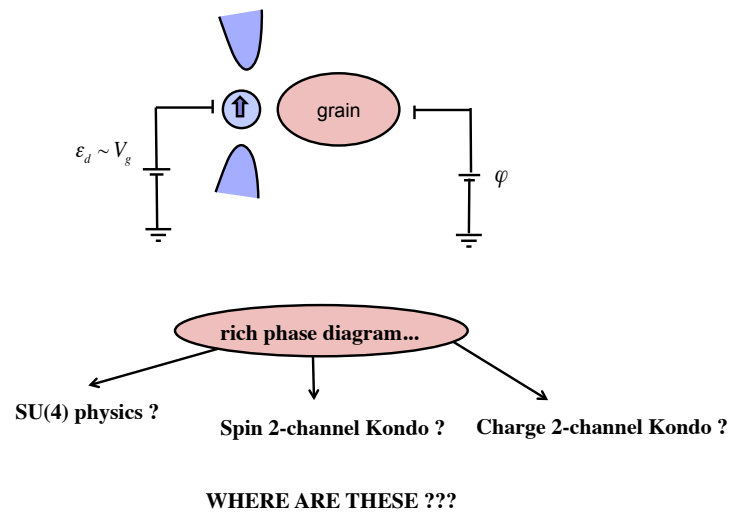
Phase diagram of OGG device ??



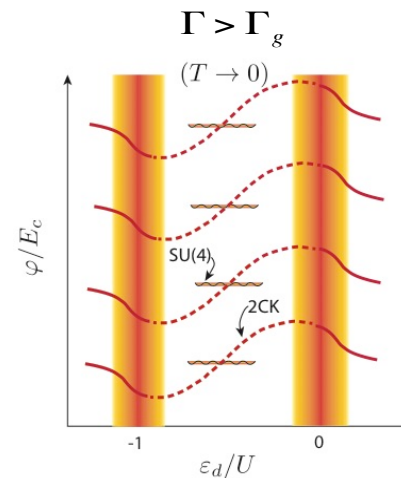
Stability diagram and predicted phases



Phase diagram of OGG device ??



Real phase diagram (from detailed NRG)



Numerical Renormalization Group (NRG) calculations

Consider $\hat{N} = \sum_{\xi, \sigma} a_{\xi, \sigma}^+ a_{\xi, \sigma}$ as independent variable

Introduce ladder operator: $\Lambda^+ |N\rangle = |N+1\rangle$

Rewrite tunneling: $t_g a_{\xi, \sigma}^+ d_{\sigma} \rightarrow t_g \Lambda^+ a_{\xi, \sigma}^+ d_{\sigma}$

Do NRG with $SU(2) \times U(1) \times U(1)$ symmetry

Remarks

- ladder operator \sim pseudospin of Matveev

$$\Lambda^{\pm} \leftrightarrow T^{\pm}$$

- Multiple Fock spaces (artificial)

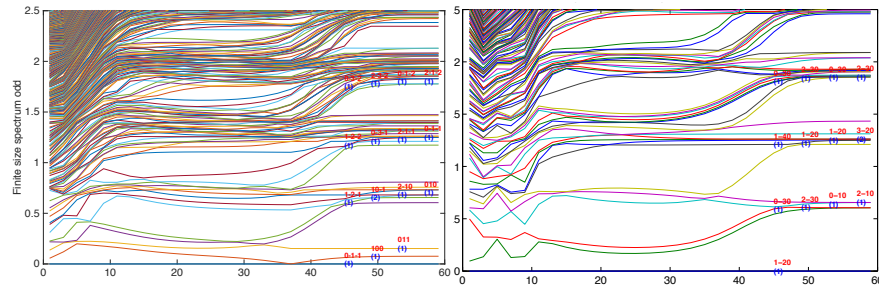
\Rightarrow projection to physical subspace !

$$\hat{Q} = \hat{N} - \sum_{\xi, \sigma} a_{\xi, \sigma}^+ a_{\xi, \sigma} = 0$$

Projection to physical subspace

unprojected finite size spectrum

projected finite size spectrum (2CK)

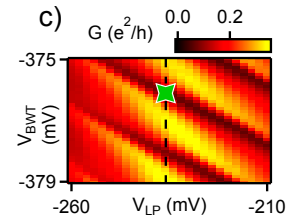
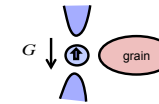


Flexible open access Budapest DM-NRG code: <http://www.phy.bme.hu/~dmnrg/>

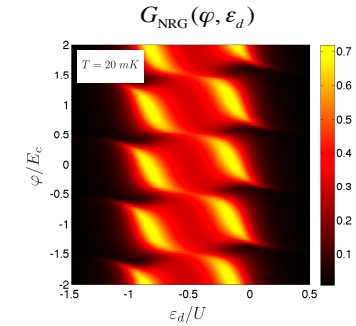
A. I. Toth, C. P. Moca, O. Legeza, and G.Z., PRB 78, 245109 (2008);
C. P. Moca, A. Alex, J. v. Delft, and G.Z., PRB 86, 195128 (2012).

Locating non-Fermi liquid lines ???

Experiment



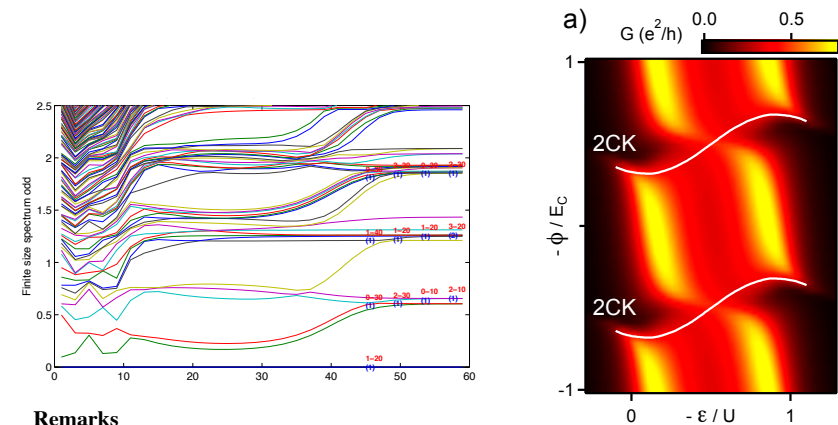
Theory



Find non-Fermi liquid lines:

- compute / measure spectral functions or $G(T) \Rightarrow$ check scaling collapse
- use finite size spectrum

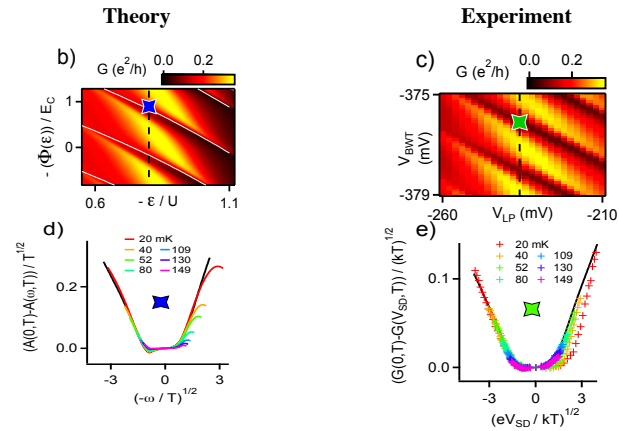
Locating non-Fermi liquid lines



Remarks

- Phase shifts visible
- Not simple 2CK spectrum...

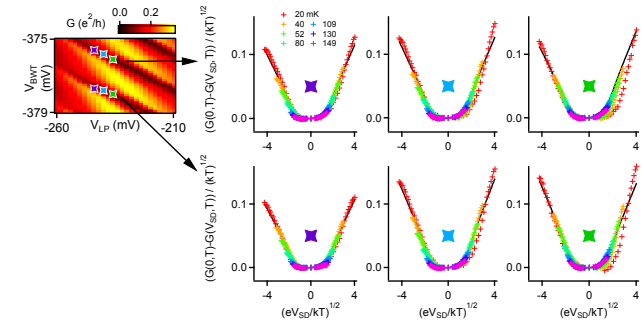
Check universal scaling



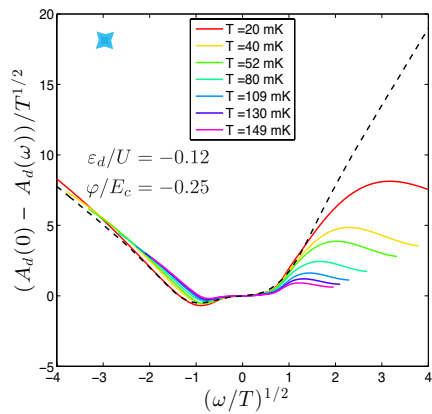
Asymmetry \iff potential scattering (phase shift)

$$\text{CFT by Affleck and Ludwig: } S_{2\text{CK}}(\omega, T) \rightarrow e^{2i\delta} S_{2\text{CK}}(\omega, T)$$

Critical lines...



Phase shifted universal scaling

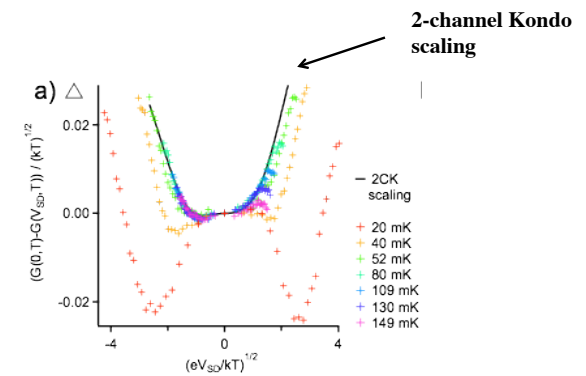


Asymmetry \iff potential scattering (phase shift)

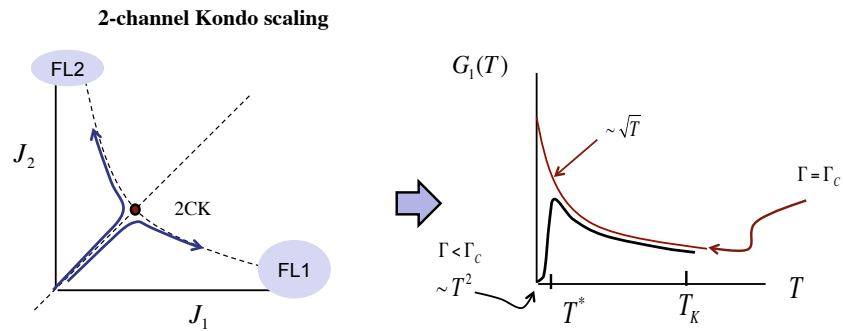
$$S_{2\text{CK}}(\omega, T) \rightarrow e^{2i\delta} S_{2\text{CK}}(\omega, T)$$

Deviations from universal scaling...

Slightly off the 2-channel Kondo points...



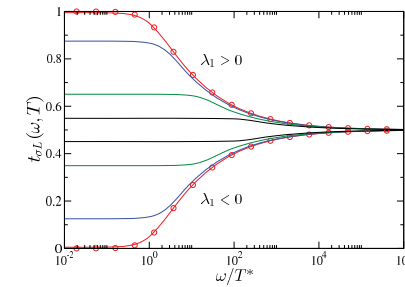
Deviations from critical scaling



- Cross-over between two strong coupling fixed points

Universal cross-over to FL

Universal cross-over functions from CFT



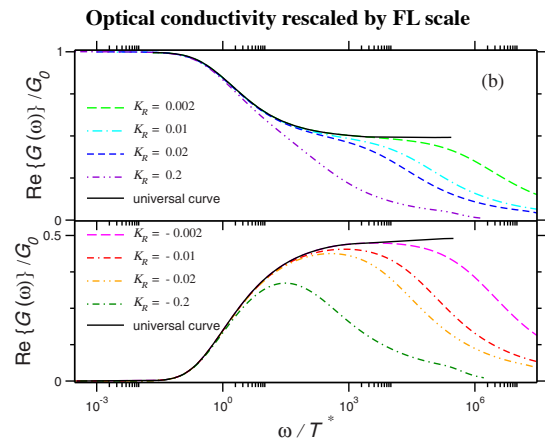
$$2\pi i v T_{\sigma\alpha,\sigma'\alpha'}(\omega, T) = \delta_{\sigma\sigma'}\delta_{\alpha\alpha'} - S_{\sigma\alpha,\sigma'\alpha'} \mathcal{G}\left(\frac{\omega}{T^*}, \frac{T}{T^*}\right)$$

$$G(\bar{\omega}, \bar{T}) = \frac{-i}{\sqrt{2\pi}\bar{T}} \frac{\Gamma(\frac{1}{2} + \frac{1}{2\pi\bar{T}})}{\tanh \frac{\bar{\omega}}{2\bar{T}} \Gamma(1 + \frac{1}{2\pi\bar{T}})} \int_{-\infty}^{\infty} dx \frac{e^{-ix\bar{\omega}}}{\sinh x} \times \text{Re} \left[{}_2F_1\left(\frac{1}{2}, \frac{1}{2}; 1 + \frac{1}{2\pi\bar{T}}, \frac{1 - \coth x}{2}\right) \right]$$

$$\Rightarrow G\left(\frac{T}{T^*}, \frac{eV}{T^*}, \delta\right)$$

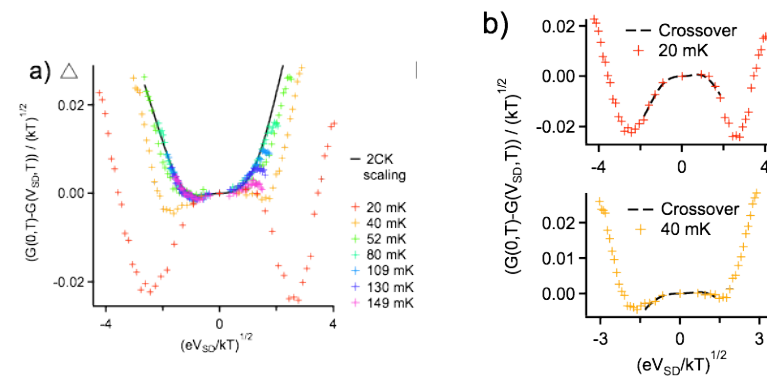
Sela, Mitchell, and Fritz, PRL (2011); Mitchell and Sela, PRB (2012).

Universal cross-over functions from NRG

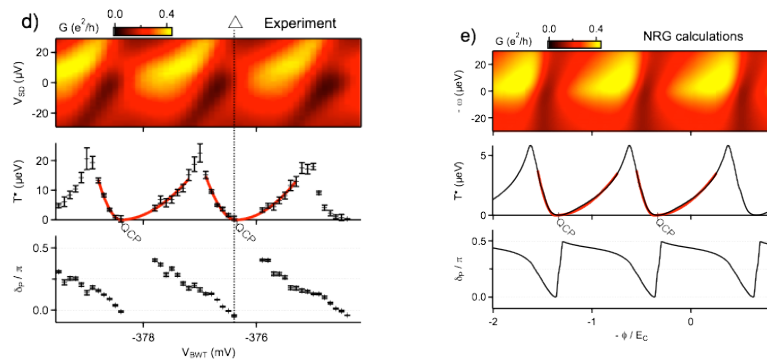


A.I Toth, L. Borda, J. vonDelft, and G.Z., PRB (2007); A.I Toth and G.Z., PRB (2008).

Extracting T^* from experimental data

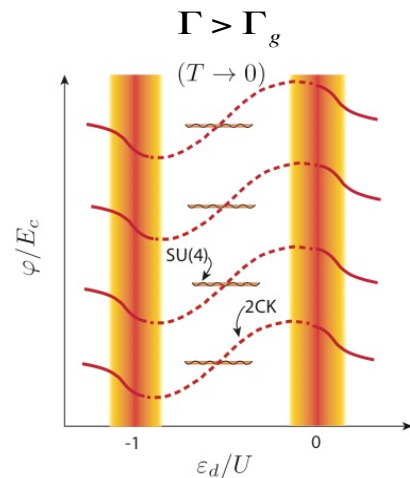


Extracting T^* from experimental data



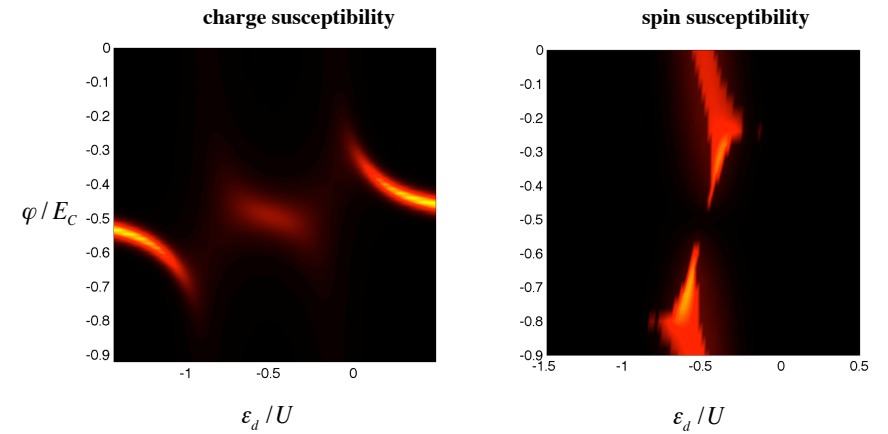
- FL scale vanishes at QCP: $T^* \sim (\varphi - \varphi_{\text{QCP}})^2$
- Phase shift jumps by $\delta \rightarrow \delta + \pi/2$

Real phase diagram (from detailed NRG)



Flexible open access Budapest DM-NRG code: <http://www.phy.bme.hu/~dmnrg/>

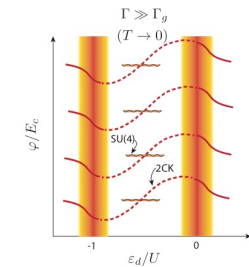
Charge and spin susceptibility



Conclusions

Theory

- Phase diagram: 2CK lines coexisting with SU(4) regions !
- Verification of phase shifted spectrum/scaling



Experiment

- FL scale vanishing at criticality
- Observation of universal 2CK \rightarrow FL cross-over
- Indications of charge Kondo state and SU(4) physics...

A. Keller et al, preprint [arxiv.org/1504.07620](https://arxiv.org/abs/1504.07620)

DM-NRG code: <http://www.phy.bme.hu/~dmnrg/>