



# spin Hall angle dispersion induced Hall effect

- Hall detection of spin accumulation in normal metal

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# • $\partial \theta_{\rm SHE} / \partial \varepsilon$ —> Hall probe of spin accumulation

- Hall detection of the spin accumulation due to:
  - spin pumping
  - spin Seebeck

T-dependence of spin transport in AFM

# the outline

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(Pure) spin Hall effect no magnetic field necessary

No Hall voltage but spin accumulation





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spin Hall angle:  $\theta_{
m SHE}=j_s/j_c$ 



$$P = \frac{j^{\uparrow} - j^{\downarrow}}{j^{\uparrow} + j^{\downarrow}}$$





"spin injection Hall effect"

shared formula of Hall current:

P > 1%

$$j_H = P\theta_{\rm SHE} j_c$$





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shared formula of Hall current:

P > 1%

$$j_H = P\theta_{\rm SHE} j_c + \dots$$

 $\Rightarrow$  to detect *P* in metal~0.0001%,  $\theta_{\rm SHE}$  > 1 needed

x sensitivity down to 0.0001% spin polarization in metals



total Hall current:  $\mathbf{j}_{AHE} = \mathbf{j}_{H}^{\uparrow} + \mathbf{j}_{H}^{\downarrow}$ Hall current in two sub-bands:  $\mathbf{j}_{H}^{\uparrow(\downarrow)} = \sigma_{SHE}^{\uparrow(\downarrow)} \boldsymbol{\sigma} \times \mathbf{E}$ 



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 $\sigma_{\rm SHE}^{\uparrow(\downarrow)} = 1/2[\sigma_{\rm SHE} \pm (\partial \sigma_{\rm SHE}/\partial \varepsilon)\mu_s/2]$ 



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spin accumulation Hall effect (SaHE)  $\mathbf{j}_{\mathrm{SaHE}} = \frac{\mu_s}{2} \frac{\partial \sigma_{\mathrm{SHE}}}{\partial \varepsilon} \frac{-\widetilde{\mathbf{m}}}{|\widetilde{\mathbf{m}}|} \times \mathbf{E}$ 



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conventional AHE in ferromagnet ${f j}_{
m AHE}=\sigma_{
m AHE}rac{-{f M}}{|{f M}|} imes{f E}$ 

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$$P = \frac{\mu_s}{2} \frac{\partial \sigma / \partial \varepsilon}{\sigma}$$

## Hall contribution from spin Hall angle dispersion





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#### Hall resistance estimation for 20 nm Culr alloy:



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# T-response of spin current transport in AFM

## Hall measurement setup



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## **Experiment: Hall signal in Cu<sub>95</sub>Ir<sub>5</sub>/YIG**



microwave off: only normal Hall



# **Experiment: Hall signal in Cu<sub>95</sub>Ir<sub>5</sub>/YIG**



 $\mathbf{E}_{\mathrm{SaHE}} \sim \mathbf{j}_c imes \widetilde{\mathbf{m}}$ 

# $\boldsymbol{j}_c \, \text{and} \, \widetilde{\boldsymbol{m}} \, \, \text{symmetry of the Hall signal}$

$$\mathbf{E}_{\mathrm{SaHE}} \sim \mathbf{j}_c imes \widetilde{\mathbf{m}}$$
  
 $\mathbf{E}_{\mathrm{SaHE}}(\mathbf{j}_c) = -\mathbf{E}_{\mathrm{SaHE}}(-\mathbf{j}_c) \qquad \mathbf{E}_{\mathrm{SaHE}}(\widetilde{\mathbf{m}}) = -\mathbf{E}_{\mathrm{SaHE}}(-\widetilde{\mathbf{m}})$ 







# Hall detection of ppm spin polarization



# **Thickness dependence**

Hall resistance of spin accumulation AHE:



 $R_{AHE} = \frac{V_{AHE}}{I} = -\frac{1}{2\sigma^2 d} \frac{\partial \sigma_{SHE}}{\partial \varepsilon} \bar{\mu}_s \sin \theta_M$ fitting result:  $\partial \sigma_{SHE} / \partial \varepsilon = -9620 \ \Omega^{-1} \text{m}^{-1} / \text{meV}$  $\frac{\partial \sigma_{SHE}}{\partial \varepsilon} = \frac{\partial \sigma}{\partial \varepsilon} \theta_{SHE} + \frac{\partial \theta_{SHE}}{\partial \varepsilon} \sigma$ evaluate the first term:

 $\theta_{\rm SHE} \partial \sigma / \partial \varepsilon = -35 \ \Omega^{-1} {\rm m}^{-1} / {\rm meV}$ 

Dazhi Hou et al., arXiv:1503.00816

# **Thickness dependence**

Hall resistance of spin accumulation AHE:



$$\frac{\partial \sigma_{\rm SHE}}{\partial \varepsilon} = \frac{\partial \sigma}{\partial \varepsilon} \theta_{\rm SHE} + \frac{\partial \theta_{\rm SHE}}{\partial \varepsilon} \sigma$$

evaluate the first term:

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spin Hall angle energy derivative

$$\partial \theta_{\rm SHE} / \partial \varepsilon = -2.6$$
 /eV.

### **Dominent Contribution in Culr**

Dazhi Hou et al., arXiv:1503.00816

# **Thickness dependence**

Hall resistance of spin accumulation AHE:



#### **Experiment: Hall signal in Au**



# Not only in Culr!



## Summary

Mall detection of ppm spin polarization



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Mall detection of ppm spin polarization



Spin accumulation Hall effect is **NOT** anomalous Hall effect

$$\mathbf{j}_{\mathrm{SaHE}} = \frac{\mu_s}{2} \frac{\partial \sigma_{\mathrm{SHE}}}{\partial \varepsilon} \frac{-\widetilde{\mathbf{m}}}{|\widetilde{\mathbf{m}}|} \times \mathbf{E}$$
$$\frac{\partial \sigma_{\mathrm{SHE}}}{\partial \varepsilon} = \frac{\partial \sigma}{\partial \varepsilon} \theta_{\mathrm{SHE}} + \frac{\partial \theta_{\mathrm{SHE}}}{\partial \varepsilon} \sigma$$

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# spin current in antiferromagnetic insulator

PRI. 113, 097202 (2014) PHYSICAL REVIEW LETTERS 29 AUGUST 2014

Antiferromagnonic Spin Transport from Y3Fe5O12 into NiO

Hailong Wang, Chunhui Du, P. Chris Hammel, and Fengyuan Yang



T. Moriyama et al., Appl. Phys. Lett. 106, 162406 (2015)

# spin current in antiferromagnetic insulator



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#### reduced Neel temperature in thin films



T. Ambrose and C. L. Chien, Phys. Rev. Lett. (1996)



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Finite-Size Effects and Uncompensated Magnetization in Thin Antiferromagnetic CoO Layers



T. Ambrose and C. L. Chien





- Finite size effect
- Double check







# Thank you!