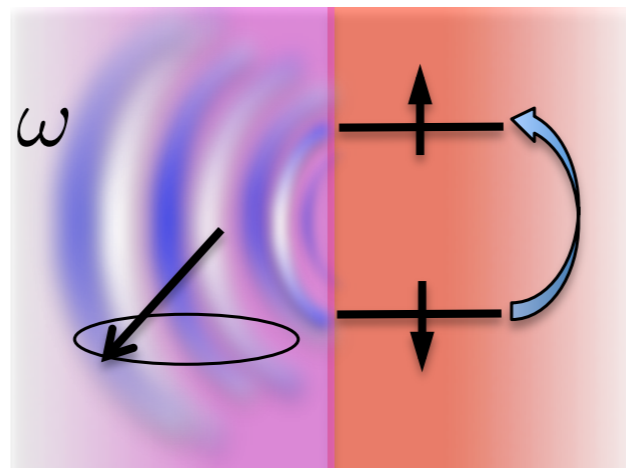


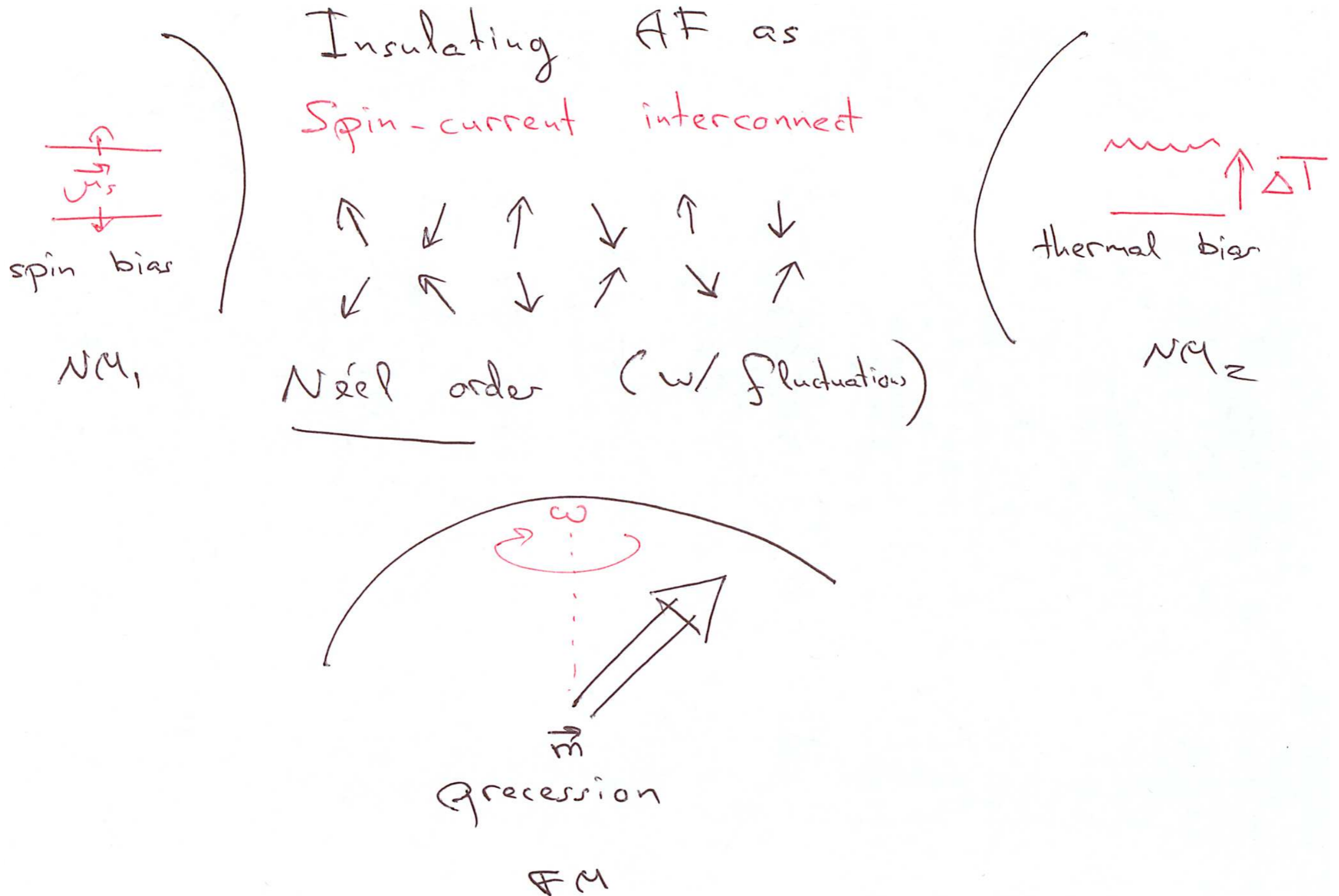
# Spin transport through antiferromagnets

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UCLA

*in collaboration with So Takei (UCLA), Bert Halperin and Amir Yacoby (Harvard),  
Takahiro Moriyama and Teruo Ono (Tokyo)*

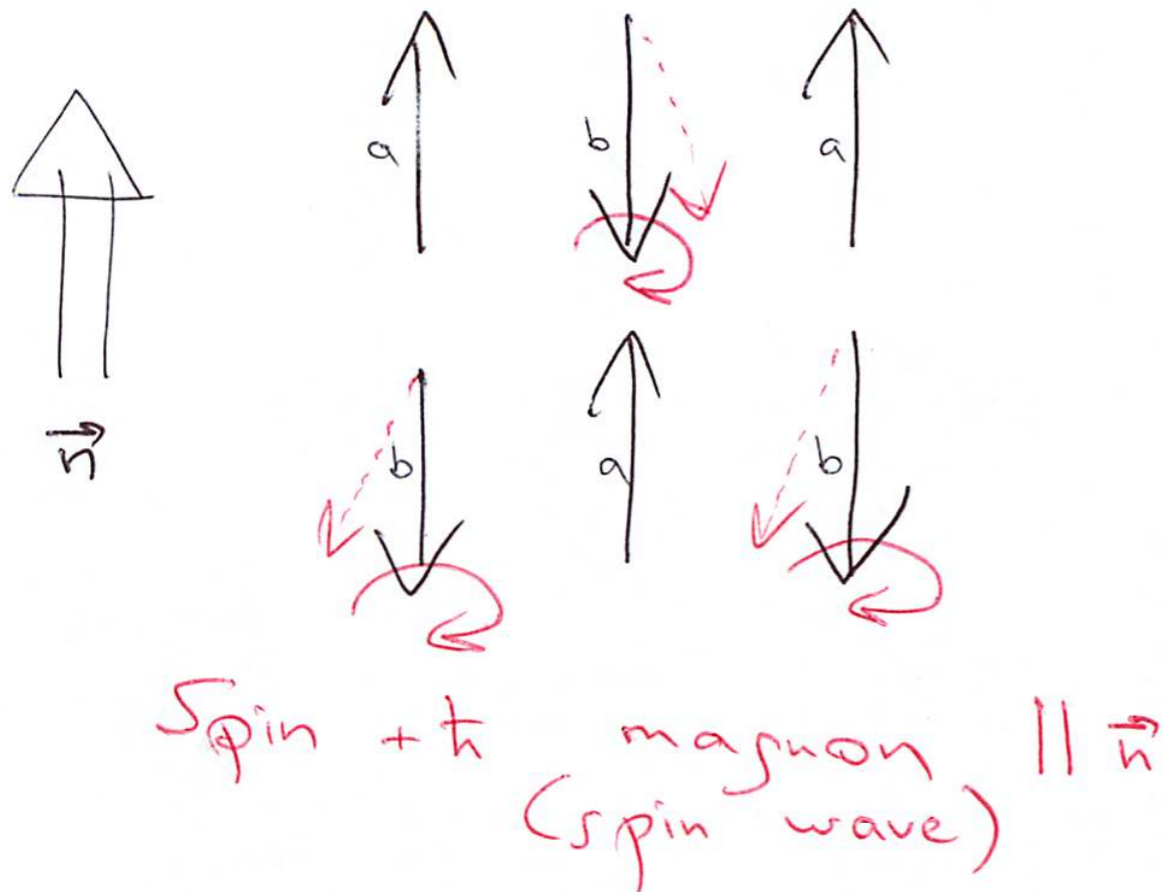


# Scope



# Two types of spin current

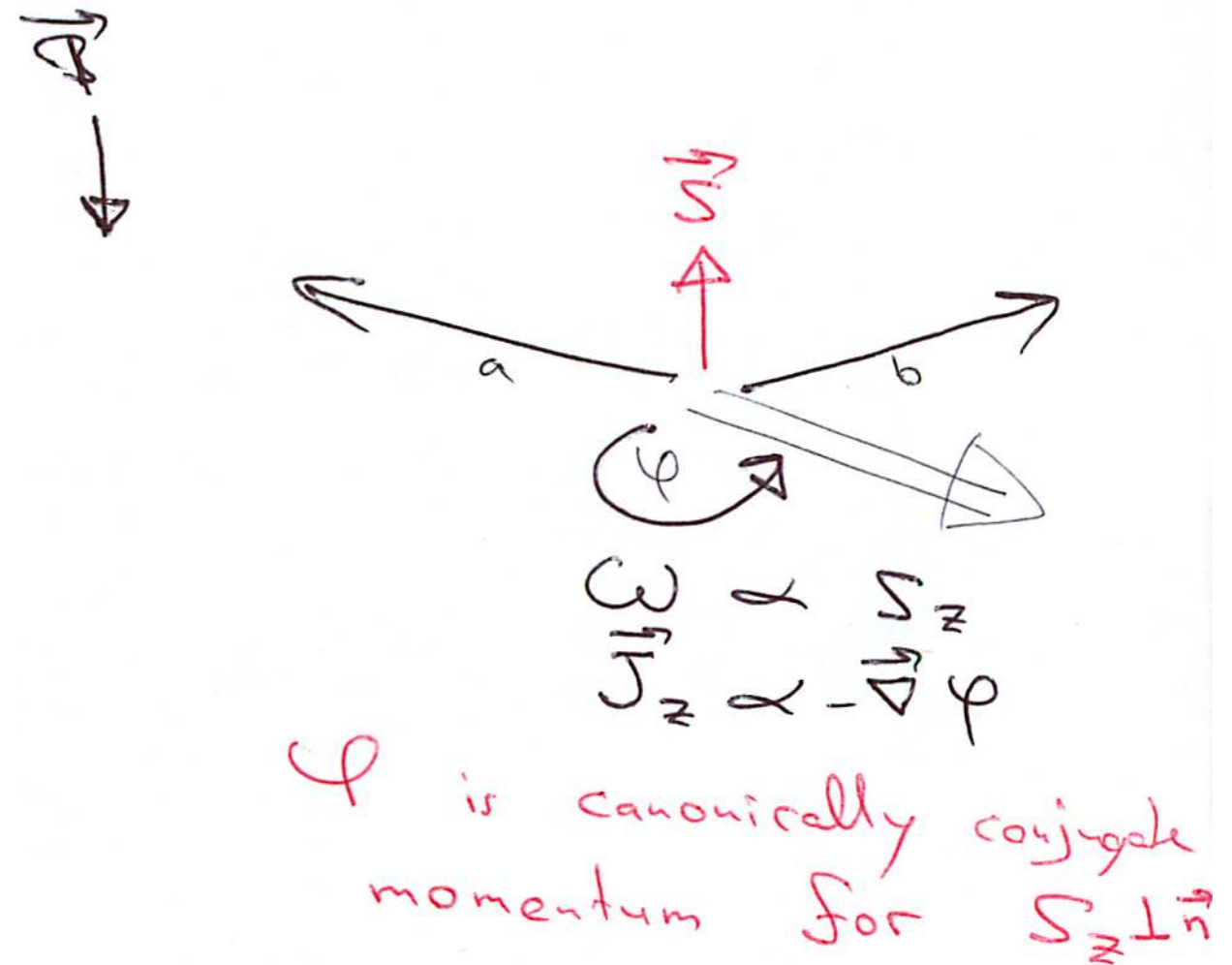
Néel order:



thermal spin transport  
(vanishes at zero temperature)

See, however, Meier and Loss, *PRL* (2003)

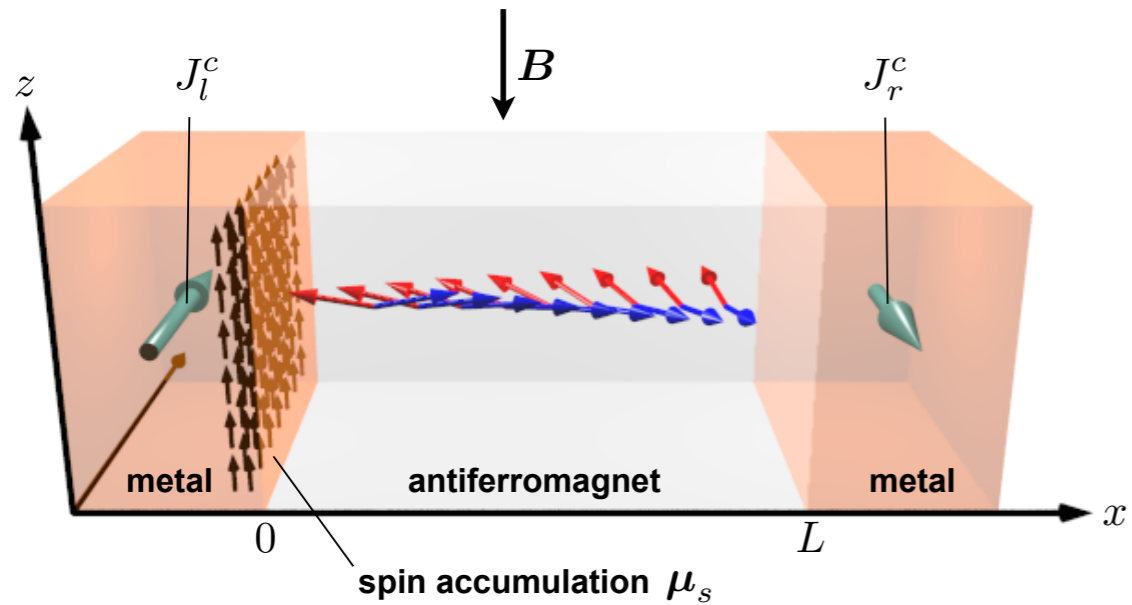
Canted AF:



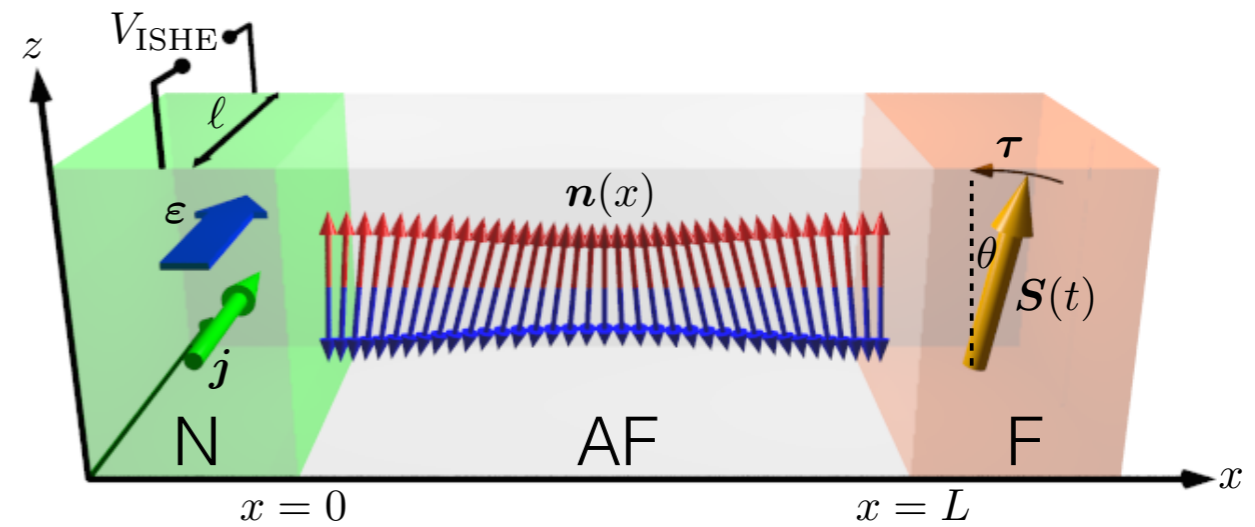
superfluid spin transport  
(largest at zero temperature)

Sonin, *AP* (2010)

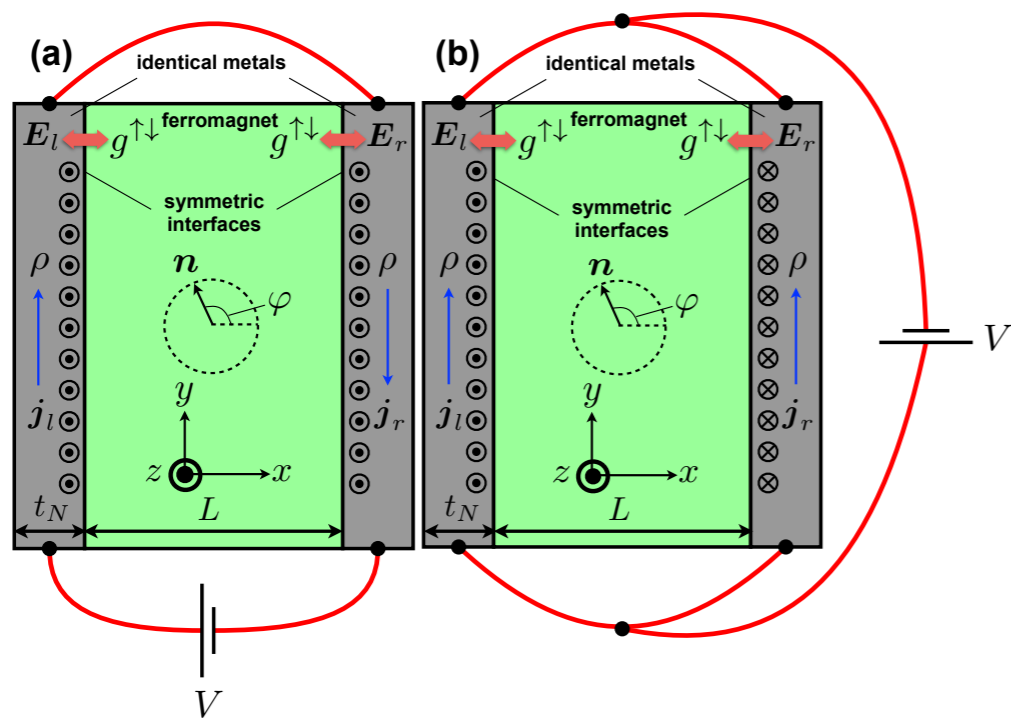
# Overview



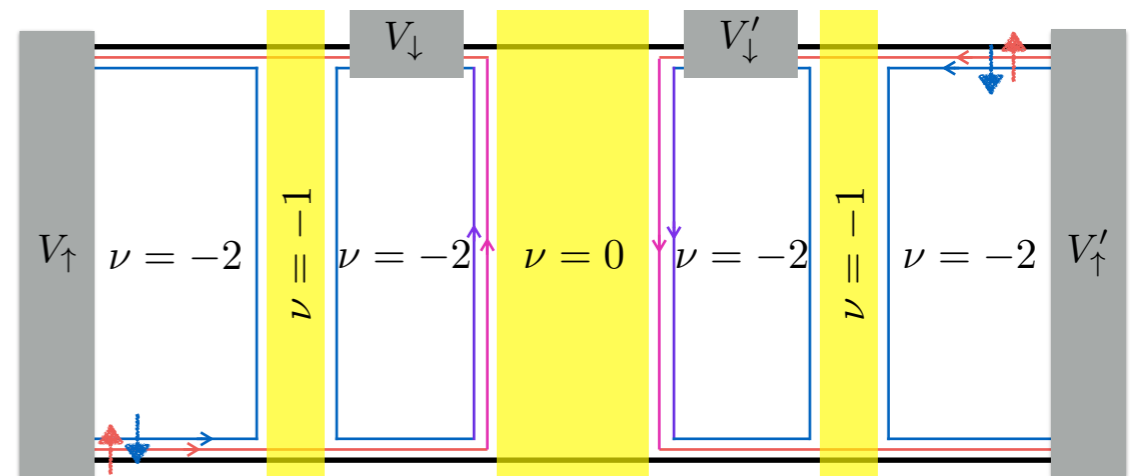
Takei, Halperin, Yacoby, and YT, *PRB* (2014)



Takei, Moriyama, Ono, and YT, *arXiv* (2015)



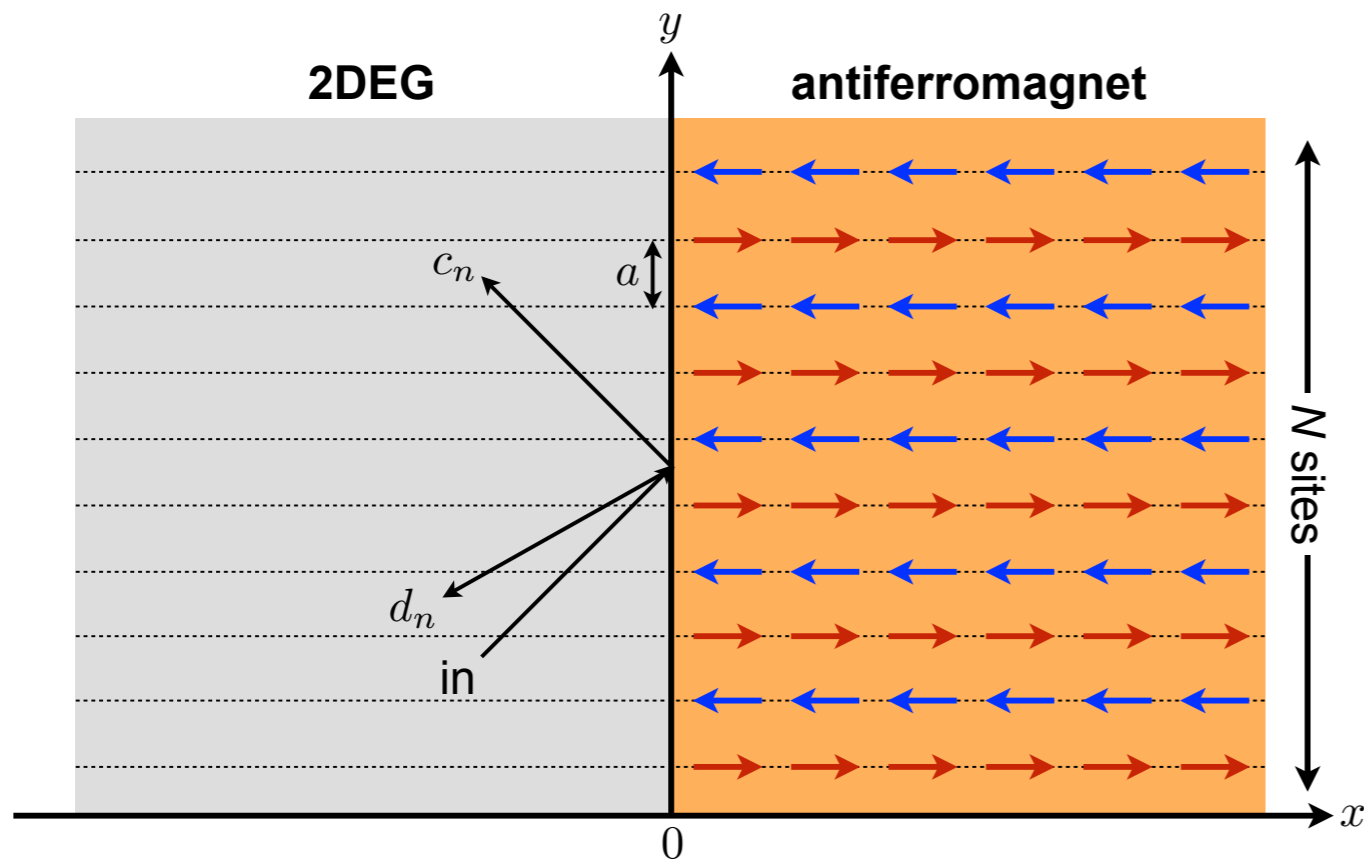
Takei and YT, *arXiv* (2015)



Takei, Yacoby, Halperin, and YT, *arXiv* (2015)

# Low-temperature interfacial torque

- ▶ In the absence of spin-orbit interactions and spin-order inhomogeneities, the collinear spin of scattered electrons is conserved; the phase shift governs the *spin-mixing conductance*:



$$g^{\uparrow\downarrow} = \sum_{nm} (\delta_{nm} - r_{nm}^{\uparrow} r_{nm}^{\downarrow*})$$

the interfacial spin current density:

$$\mathbf{J}_s = \frac{\text{Re } g^{\uparrow\downarrow}}{4\pi} \mathbf{n} \times \tilde{\boldsymbol{\mu}}_s \times \mathbf{n} + \frac{\text{Im } g^{\uparrow\downarrow}}{4\pi} \tilde{\boldsymbol{\mu}}_s \times \mathbf{n}$$

$$\tilde{\boldsymbol{\mu}}_s \equiv \boldsymbol{\mu}_s - \hbar \mathbf{n} \times \dot{\mathbf{n}}$$

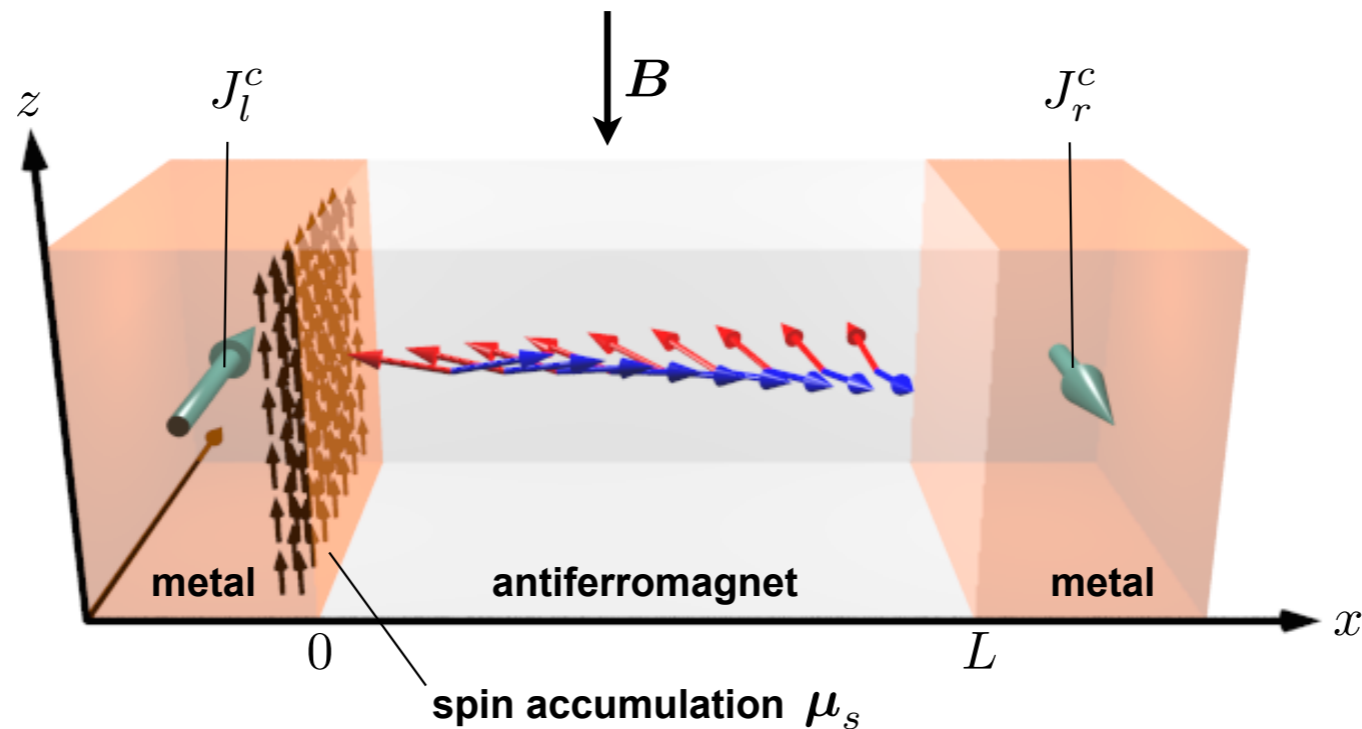
torque pumping

$$r_{n'n}^{\sigma} = \underbrace{c_n \delta_{n'n}}_{\text{specular}} + \underbrace{\sigma d_n \delta_{\bar{n}'n}}_{\text{umklapp}}$$

$\bar{n} = (n + N/2) \text{ mod } N$

Unitarity:  $|c_n|^2 + |d_n|^2 = 1 \quad \Rightarrow \quad g^{\uparrow\downarrow} = 2 \sum_n |d_n|^2$

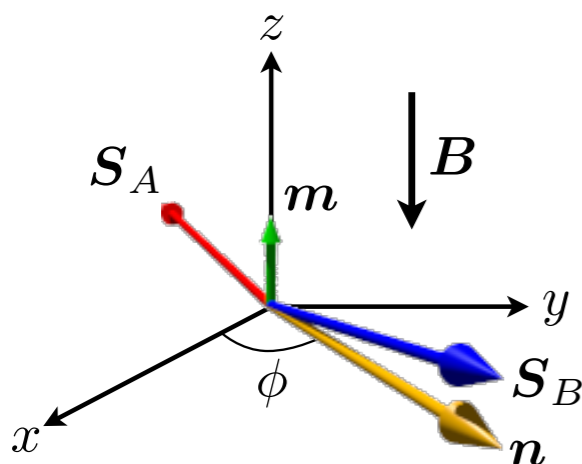
# Two-terminal spin superfluid



Takei, Halperin, Yacoby, and YT, *PRB* (2014)

nonlinear  $\sigma$  model: 
$$\mathcal{L}_{\text{AF}}[\mathbf{m}, \mathbf{n}] = \mathcal{L}_k - \frac{A}{2} (\partial_\mu \mathbf{n})^2 - \frac{\mathbf{m}^2}{2\chi} - \mathbf{b} \cdot \mathbf{m}$$

kinetic term (Berry phase): 
$$\mathcal{L}_k = s\mathbf{m} \cdot (\mathbf{n} \times \partial_t \mathbf{n})$$

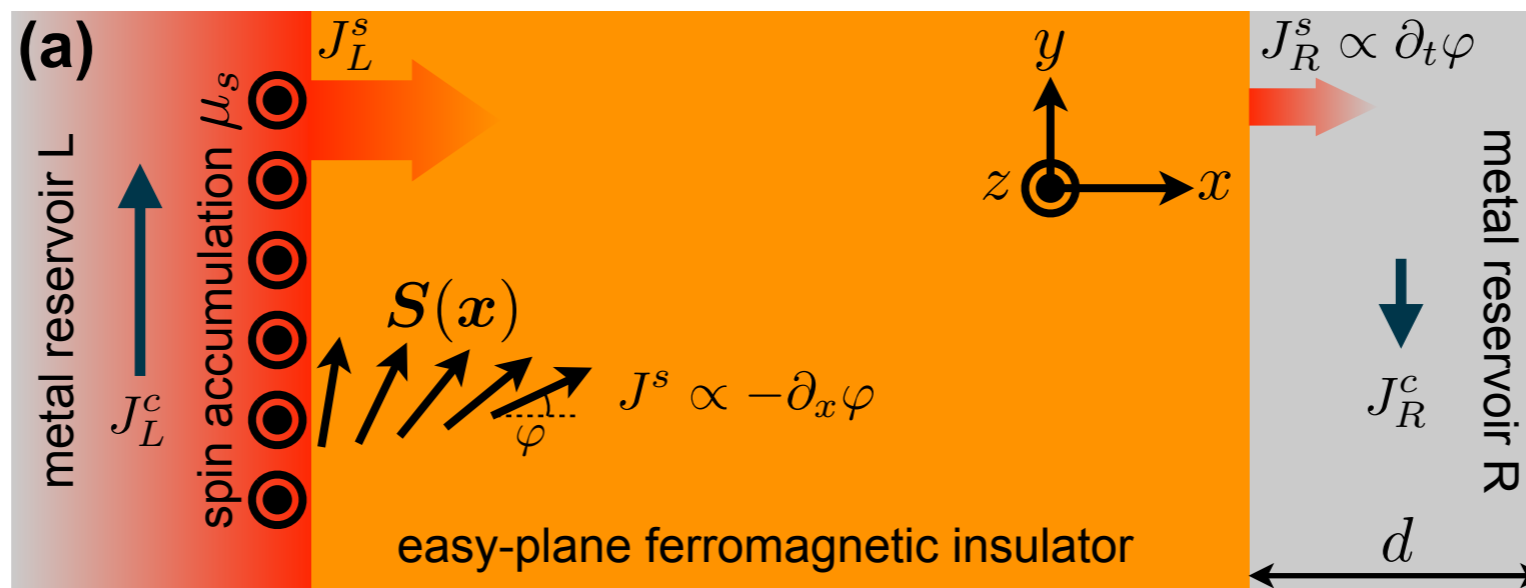


collective spin current: 
$$\mathbf{J}_s = -A\mathbf{n} \times \nabla \mathbf{n} \rightarrow -A\nabla \phi$$

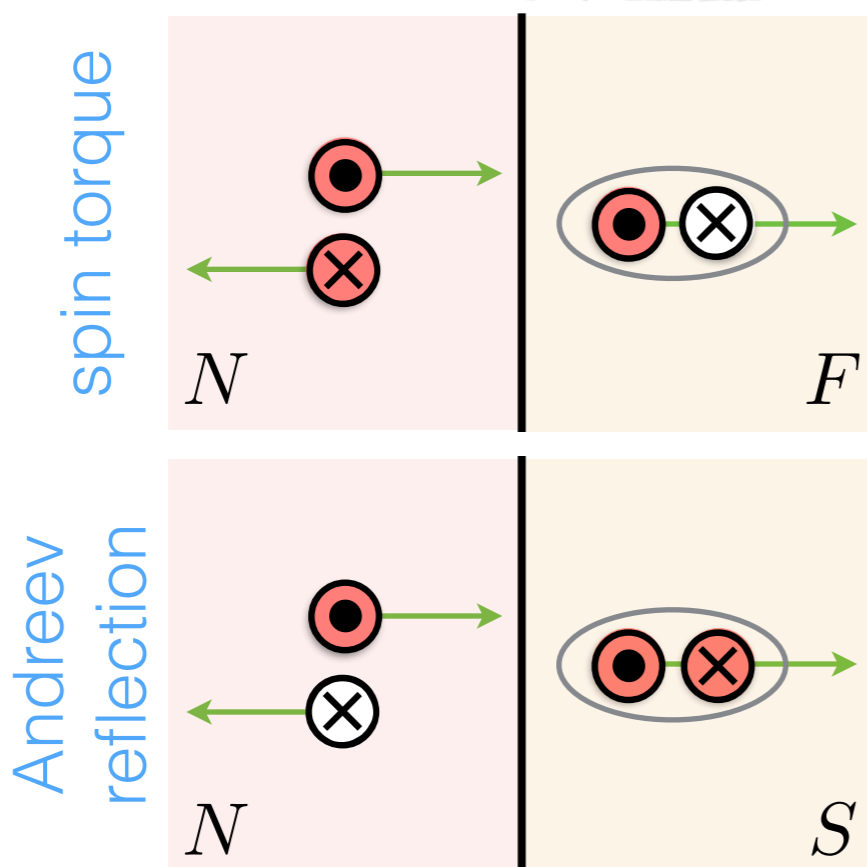
Gilbert damping: 
$$s\dot{\mathbf{m}} = -\alpha \mathbf{n} \times \dot{\mathbf{n}} + \dots$$

# Ferromagnetic analog

- ▶ Low-energy dynamics of easy-plane ferromagnet is fully equivalent:



Takei and YT, PRL (2014)



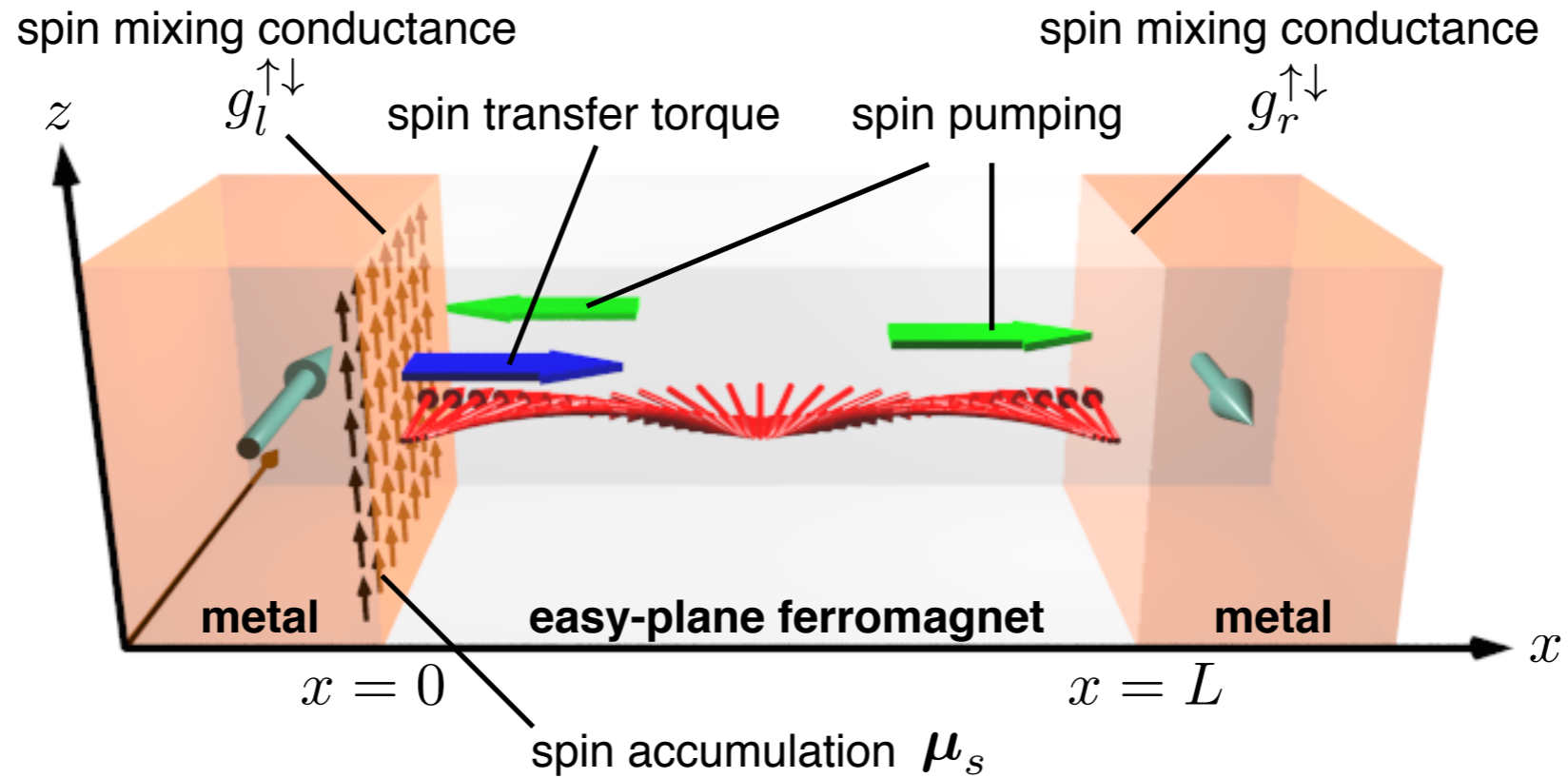
$$\mathbf{J}_s = \frac{\text{Re } g^{\uparrow\downarrow}}{4\pi} \mathbf{n} \times \tilde{\boldsymbol{\mu}}_s \times \mathbf{n} + \frac{\text{Im } g^{\uparrow\downarrow}}{4\pi} \tilde{\boldsymbol{\mu}}_s \times \mathbf{n}$$

$$\tilde{\boldsymbol{\mu}}_s \equiv \boldsymbol{\mu}_s - \hbar \mathbf{n} \times \dot{\mathbf{n}}$$

effective voltage difference

YT, Brataas, Bauer, and Halperin, RMP (2005)

# Spin-current circuit

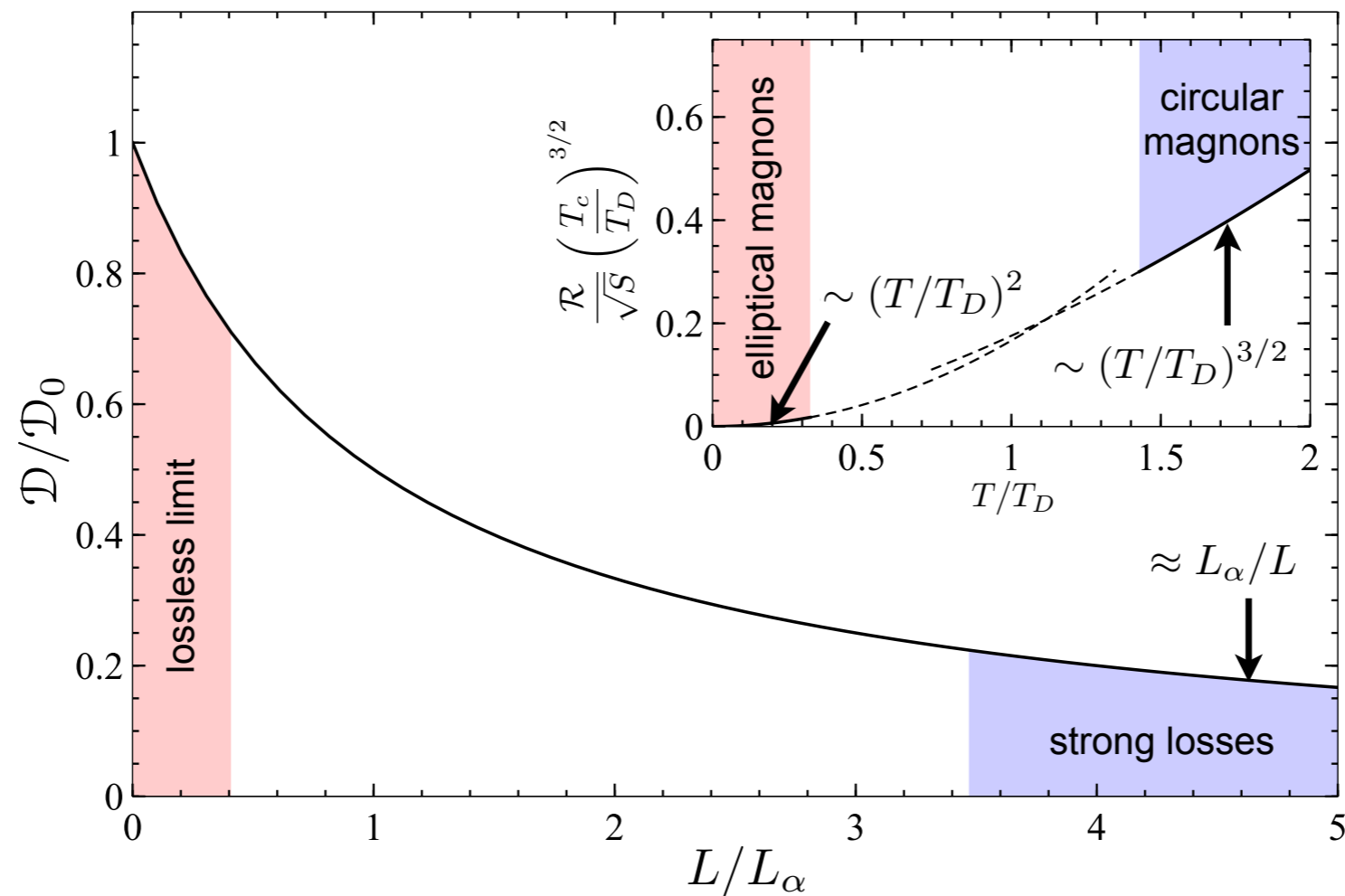
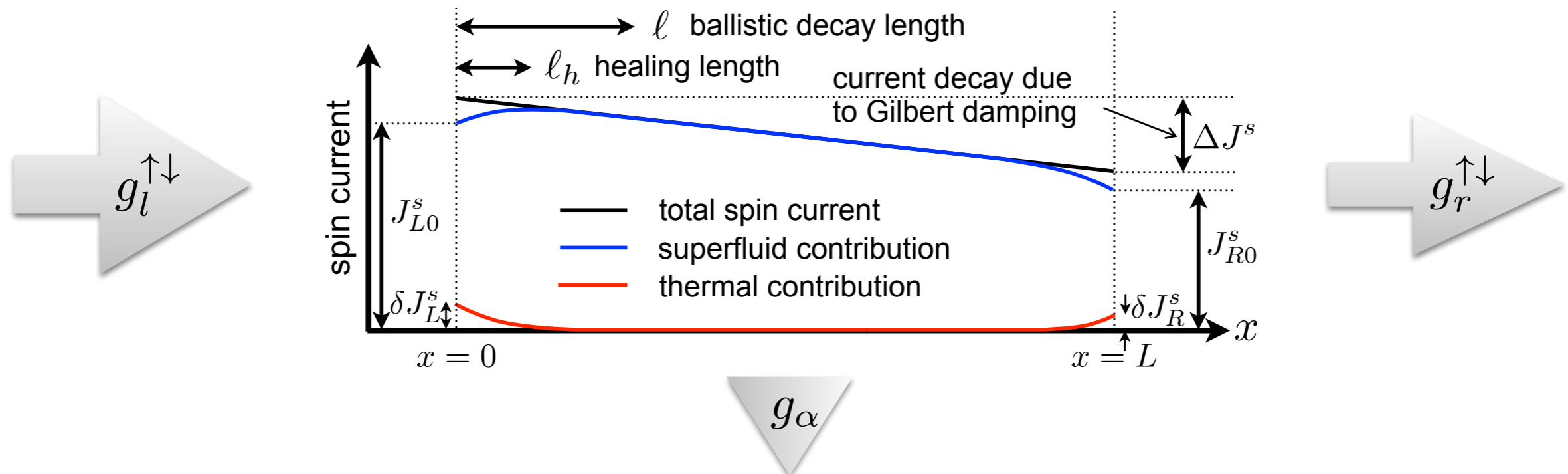


$$g_\alpha = \frac{4\pi\alpha sL}{\hbar}$$

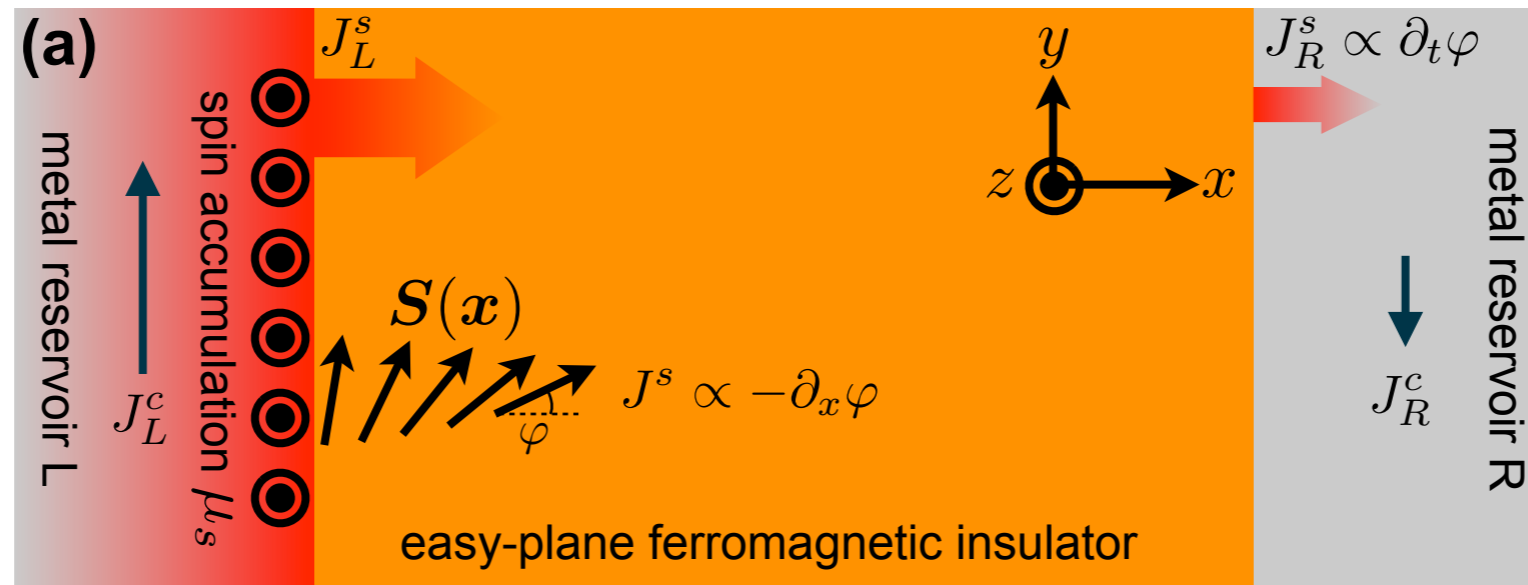
$$\Omega = \frac{\mu_s}{\hbar} \frac{g_l^{\uparrow\downarrow}}{g_l^{\uparrow\downarrow} + g_r^{\uparrow\downarrow} + g_\alpha}, \quad J_r^s = \frac{\mu_s}{4\pi} \frac{g_l^{\uparrow\downarrow} g_r^{\uparrow\downarrow}}{g_l^{\uparrow\downarrow} + g_r^{\uparrow\downarrow} + g_\alpha}$$



# Role of thermal magnons



# Negative DC electron drag



$$J_{\text{SH}}^s = \frac{\hbar}{2e} \theta_{\text{SH}} J_l^c \quad \text{Onsager} \quad J_r^c = -\frac{\hbar}{2e} \theta_{\text{SH}} \frac{\sigma}{d} \Omega$$

$$\mathcal{D} \equiv -\frac{J_r^c}{J_l^c} = \frac{h}{4e^2} \left( \frac{\theta_{\text{SH}}^2}{g^{\uparrow\downarrow}} \right)_{N|F} \left( \frac{\sigma}{\lambda_s} \right)_N \quad \text{assuming} \quad L < l_\alpha \equiv \frac{\hbar g^{\uparrow\downarrow}}{4\pi\alpha s}$$

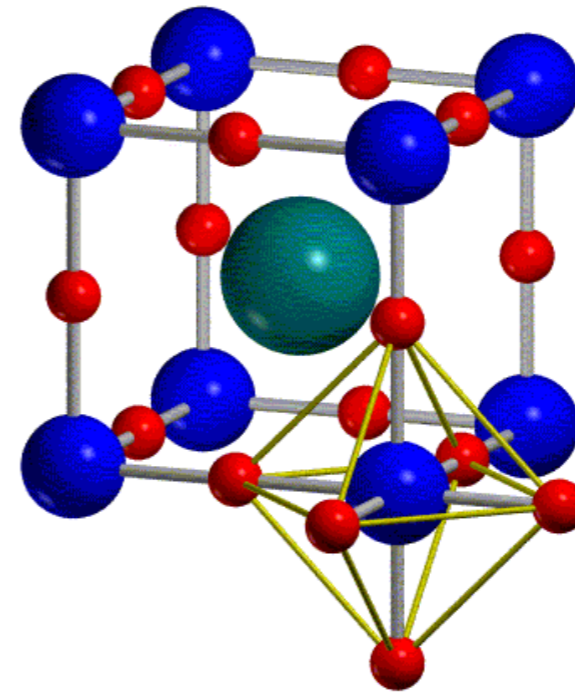
for Pt|YIG|Pt heterostructure:  $l_\alpha \sim 1 \mu\text{m}$  and  $\mathcal{D} \sim 0.1$

# Possible materials: Perovskites



$$S = 5/2$$

$$T_N \approx 83 \text{ K}$$



$$S = 1$$

$$T_N \approx 275 \text{ K}$$

$$\alpha \sim 10^{-4} \rightarrow \text{damping length } L_\alpha \sim 100 \text{ nm}$$

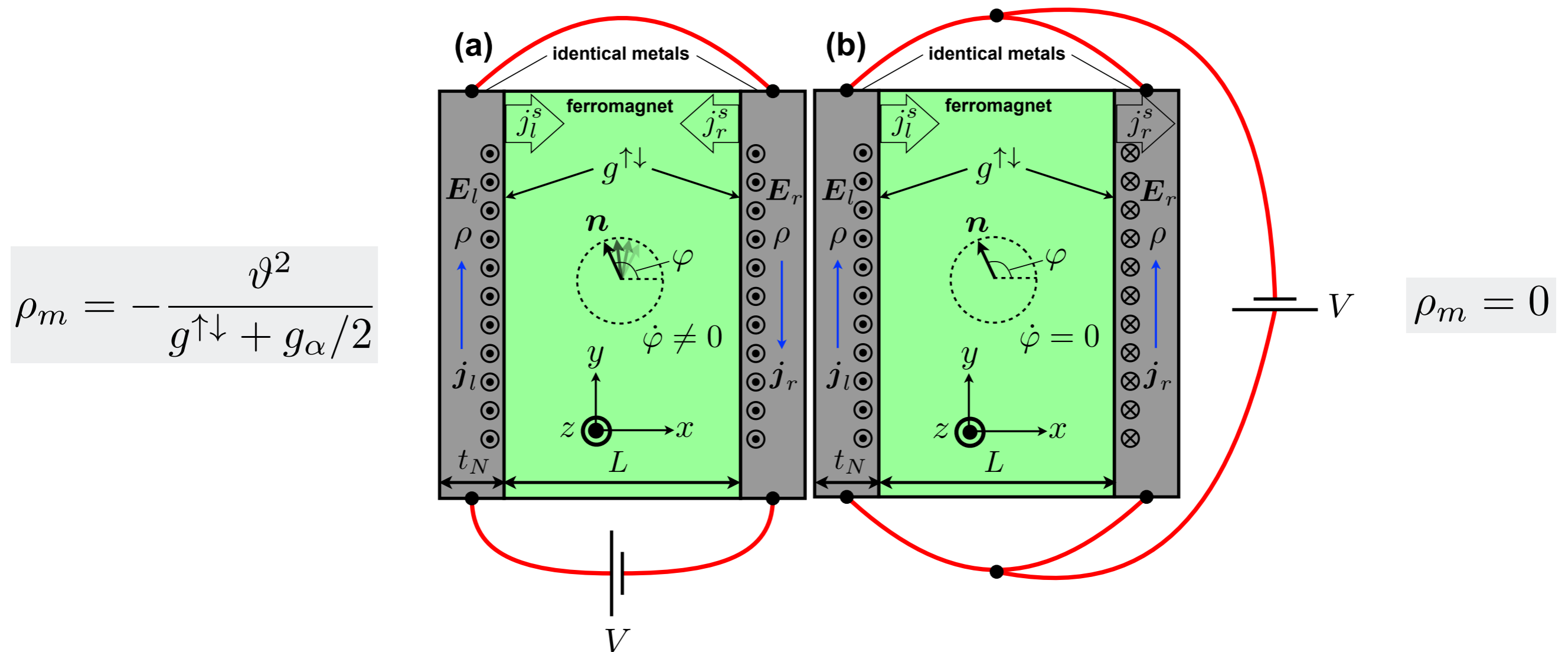
$$\text{anisotropy: } K/J \sim 10^{-5} \rightarrow \text{critical length } L_c = \sqrt{A/K} \sim 100 \text{ nm}$$

$$J_c^{(s)} = KL_c = \sqrt{AK} \rightarrow J^{(c)} \sim 10^{12} \text{ A/m}^2$$

$$\text{minimal magnetic field providing easy plane: } B_c = \sqrt{KJ} \sim 1 \text{ T}$$

# Topological magnetoresistance

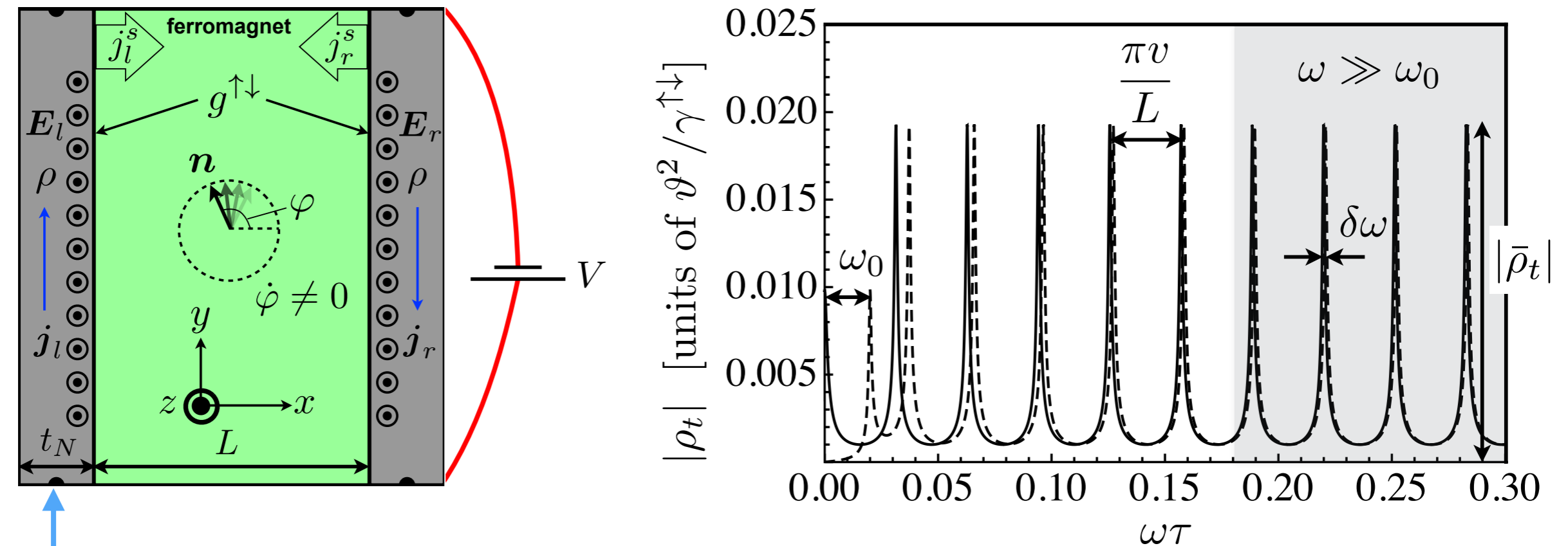
- ▶ Circulating current through two metal films in series (a) spins the order, reducing the overall dissipation



- ▶ In the parallel configuration, the torques are balanced, and the magnet remains stationary, causing more friction

# AC transresistance

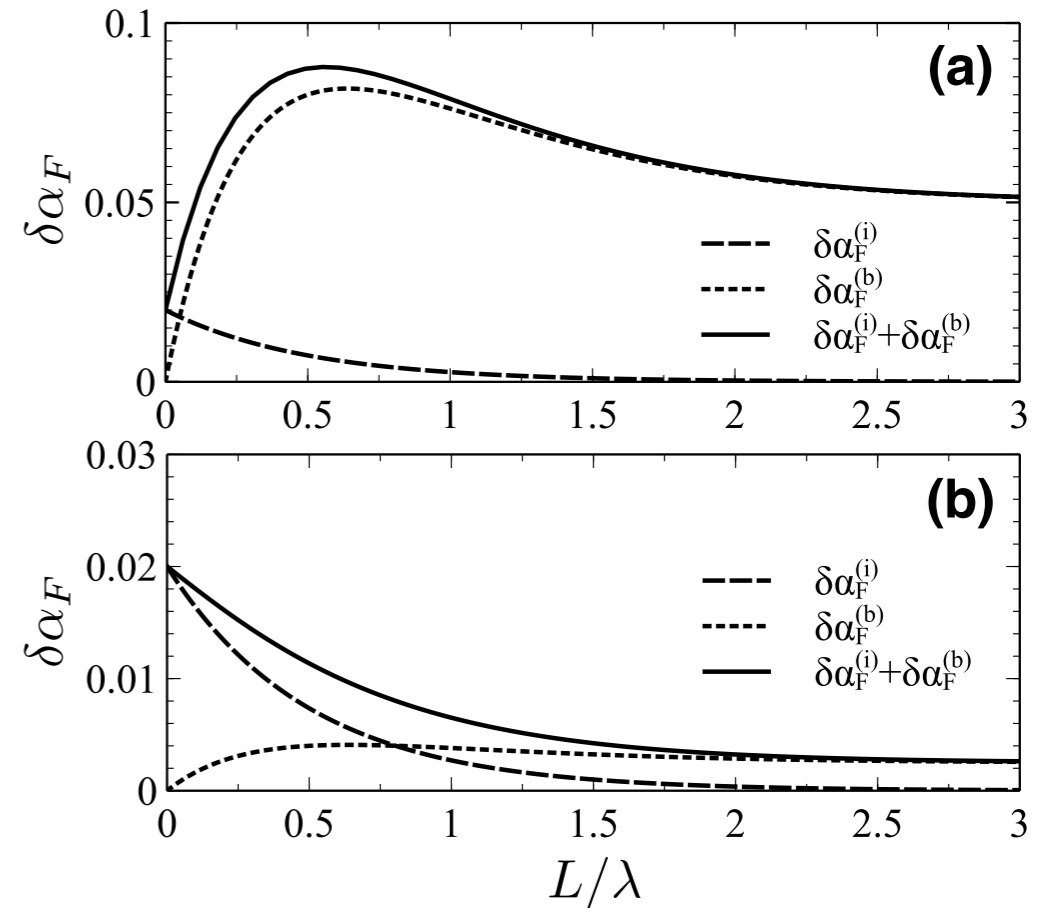
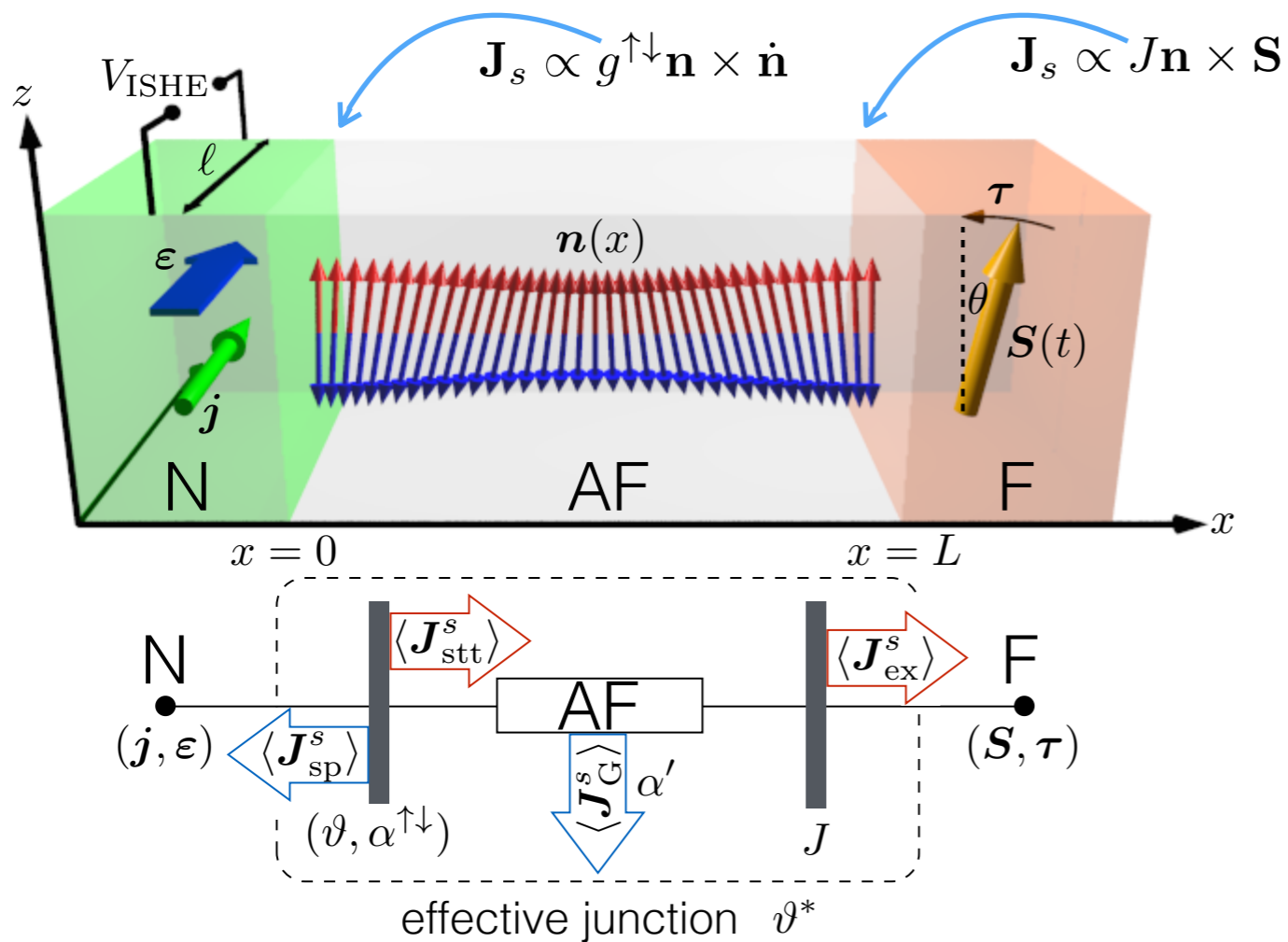
- While the DC spin supercurrent (and corresponding drag) can be quenched by an in-plane anisotropy, the AC transresistance is still fully operative on spin-wave resonances:



$$|\bar{\rho}_t| = \frac{v^2}{2g^{\uparrow\downarrow} + g_\alpha/2}$$

# AF-mediated spin transfer

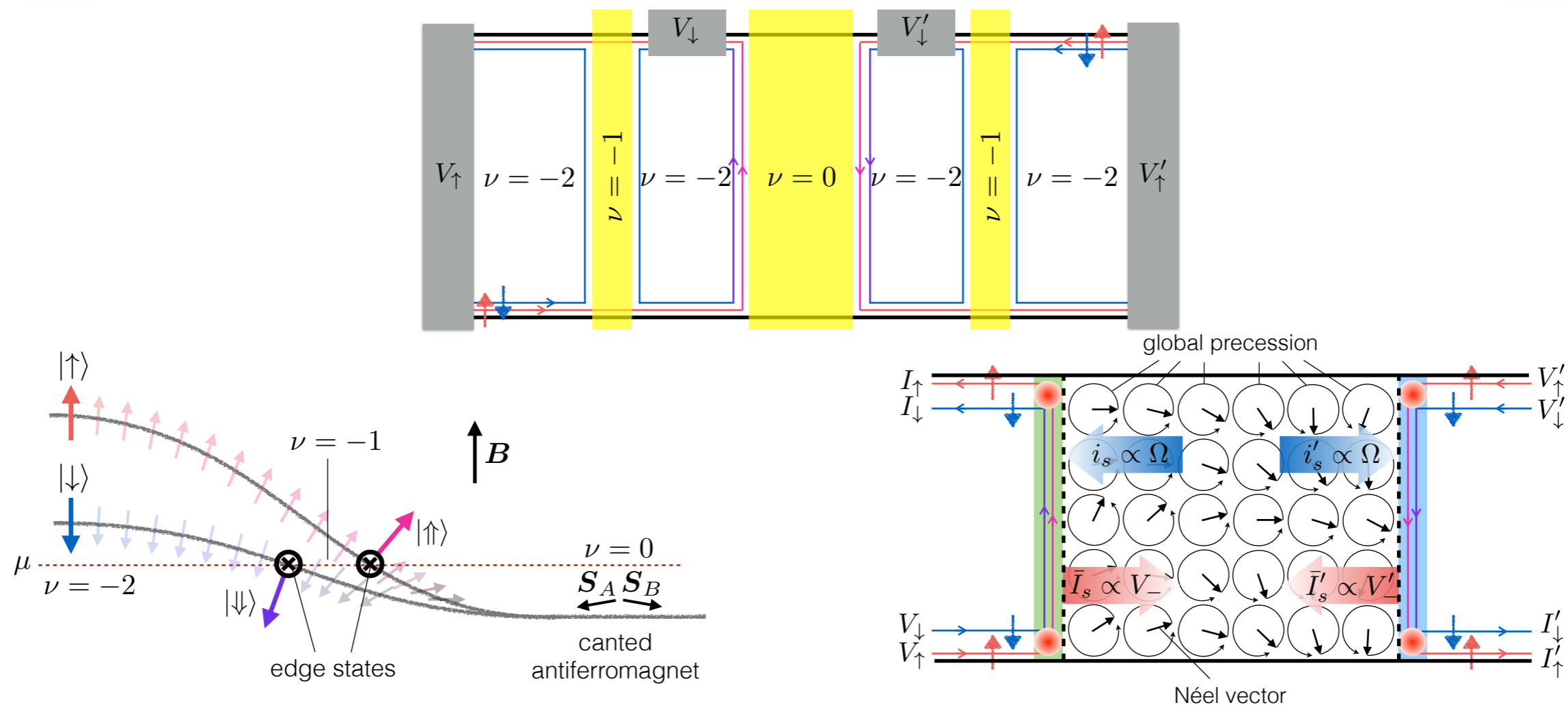
- Spin transfer torque and spin pumping mediated by AF:



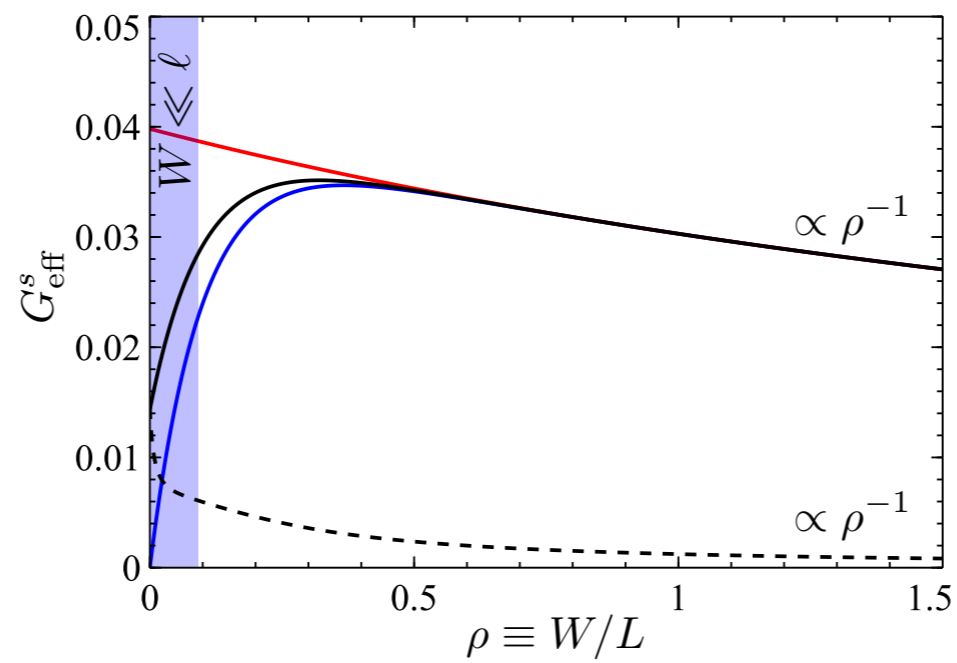
$$\alpha_F^{(i)} = \frac{1}{S} \frac{g^{\uparrow\downarrow} + \frac{\vartheta}{\omega_F} j}{\left( \cosh \frac{L}{\lambda} + \frac{1}{\eta} \sinh \frac{L}{\lambda} \right)^2}$$

$$\alpha_F^{(b)} = \frac{\alpha_{AF}}{S} \frac{\frac{L}{\lambda} + \frac{1}{2} \sinh \frac{2L}{\lambda}}{\left( \cosh \frac{L}{\lambda} + \frac{1}{\eta} \sinh \frac{L}{\lambda} \right)^2}$$

# Spin transport through 0LL in graphene



interplay between damping, vertex scattering, and interedge scattering:



# Summary

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- ▶ While antiferromagnets possess magnetic order that is hidden from generic electromagnetic probes, they appear as potentially efficient interconnects for spin transport
- ▶ It is natural to invoke a two-fluid picture, with the spin superfluid dominating transport at low temperatures (compared to  $T_N$ )
- ▶ Spin transport can be transmitted through interfaces with normal metals and ferromagnets, and thus manifested through spin Hall and FMR probes; exhibiting long-ranged and topological characteristics
- ▶ Intriguing prospects for edge transport in strongly-correlated symmetry-broken graphene under strong magnetic field

