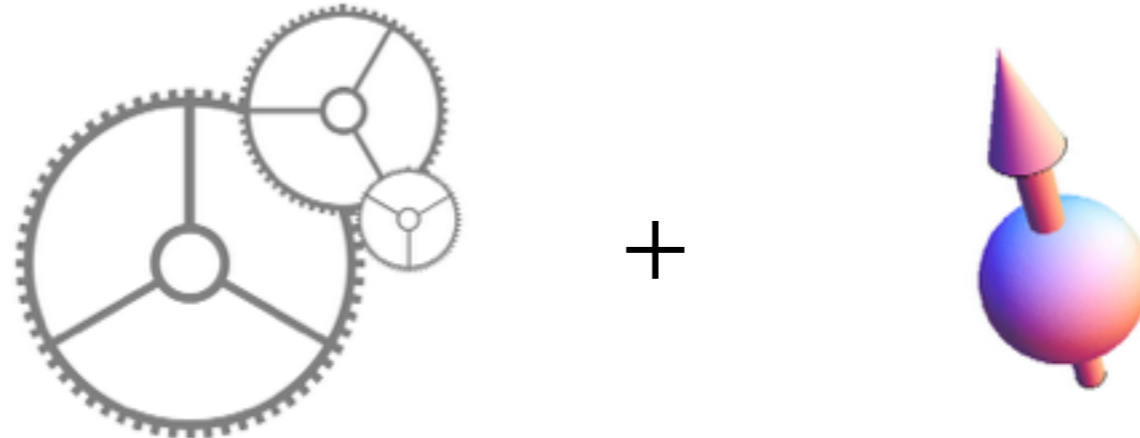


Theory of spin mechatronics



Mamoru Matsuo (JAEA-ASRC, JST-ERATO)

in collaboration with

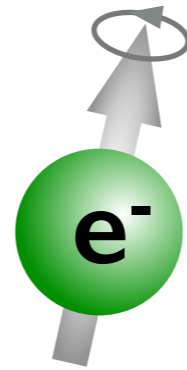
J. Ieda, S. Maekawa [theory]

H. Chudo, K. Harii, M. Ono, R. Takahashi, E. Saitoh [experiment]

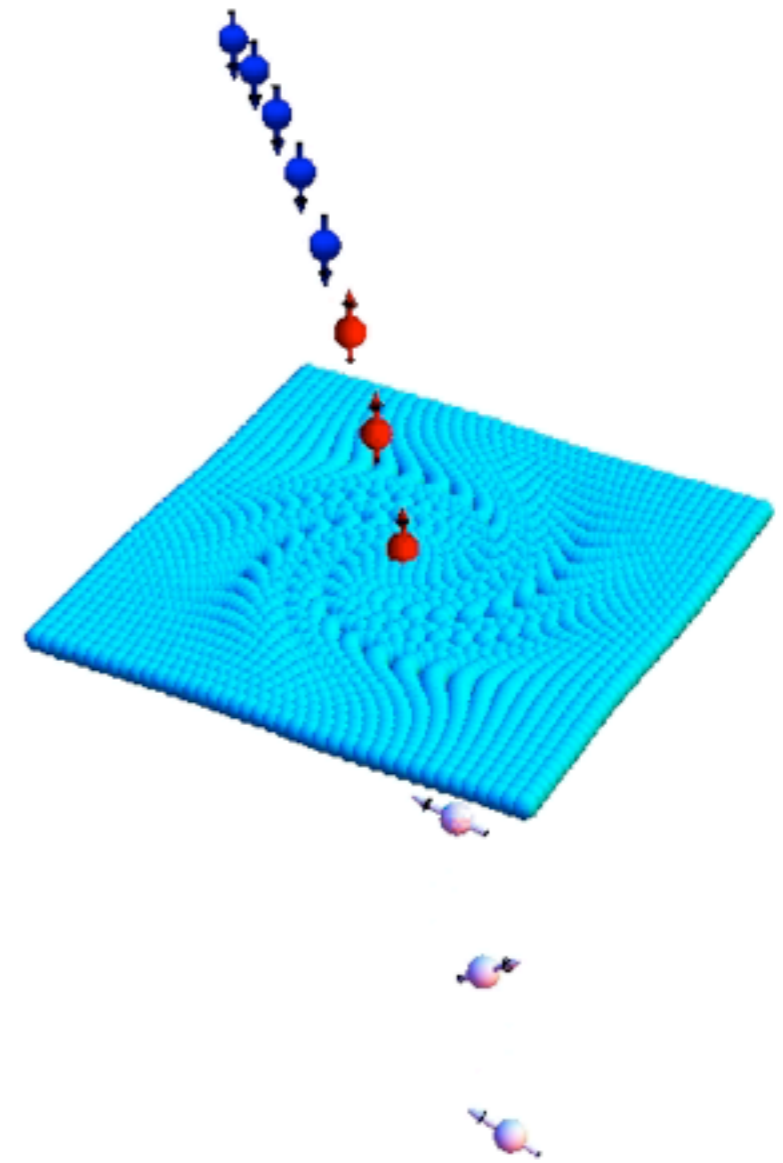
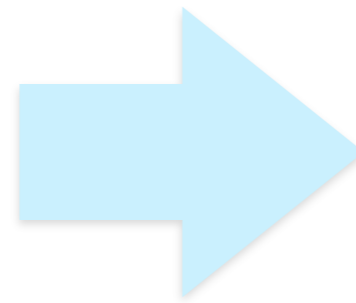
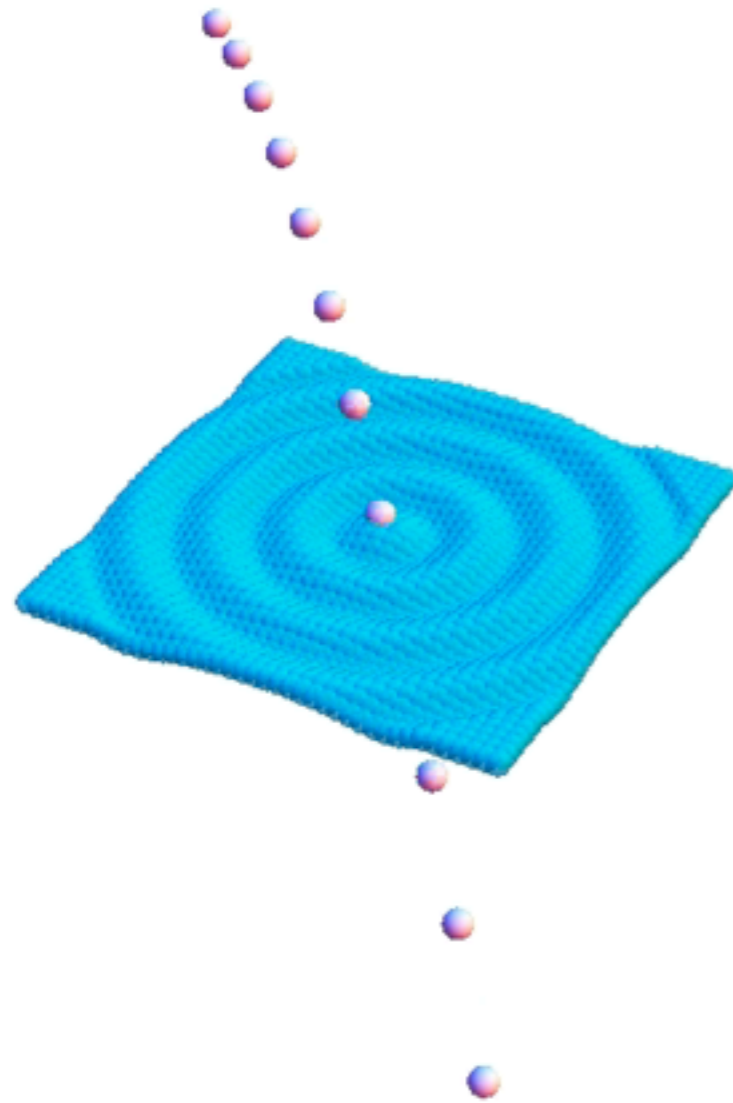


From mechatronics to “spin mechatronics”

Charge



Spin



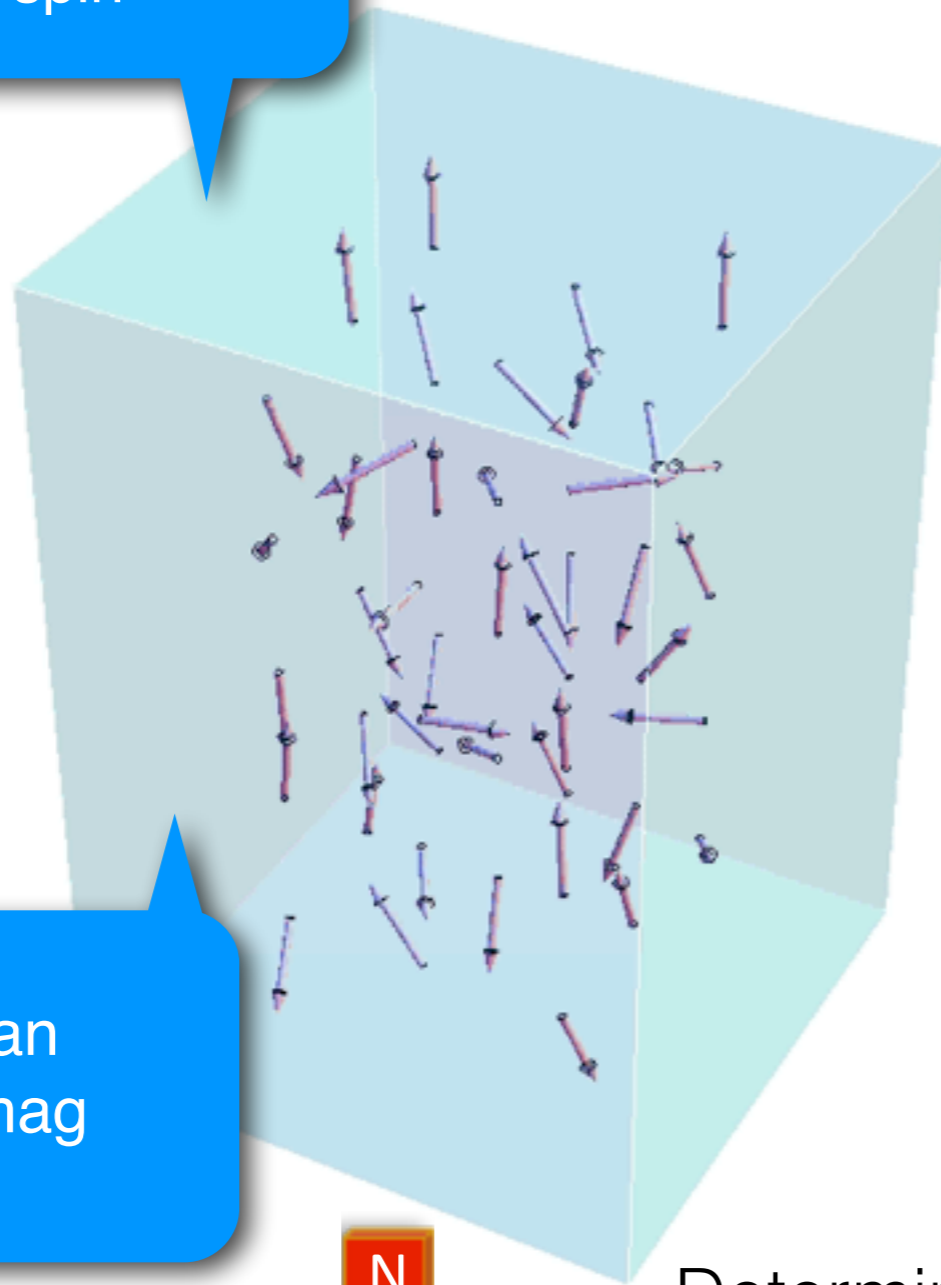
Charge current & mechanical motion

Spin current & mechanical motion

Angular momentum conversion
between spin and mechanical rotation

Einstein-de Haas (1915): Rotation by magnetization

Wheel = spin



Ayako-san
= Ferromag

Arm = Magnet



Determined $g \sim 2$ for electron before Quantum Mechanics

Ayako-san
(our secretary)

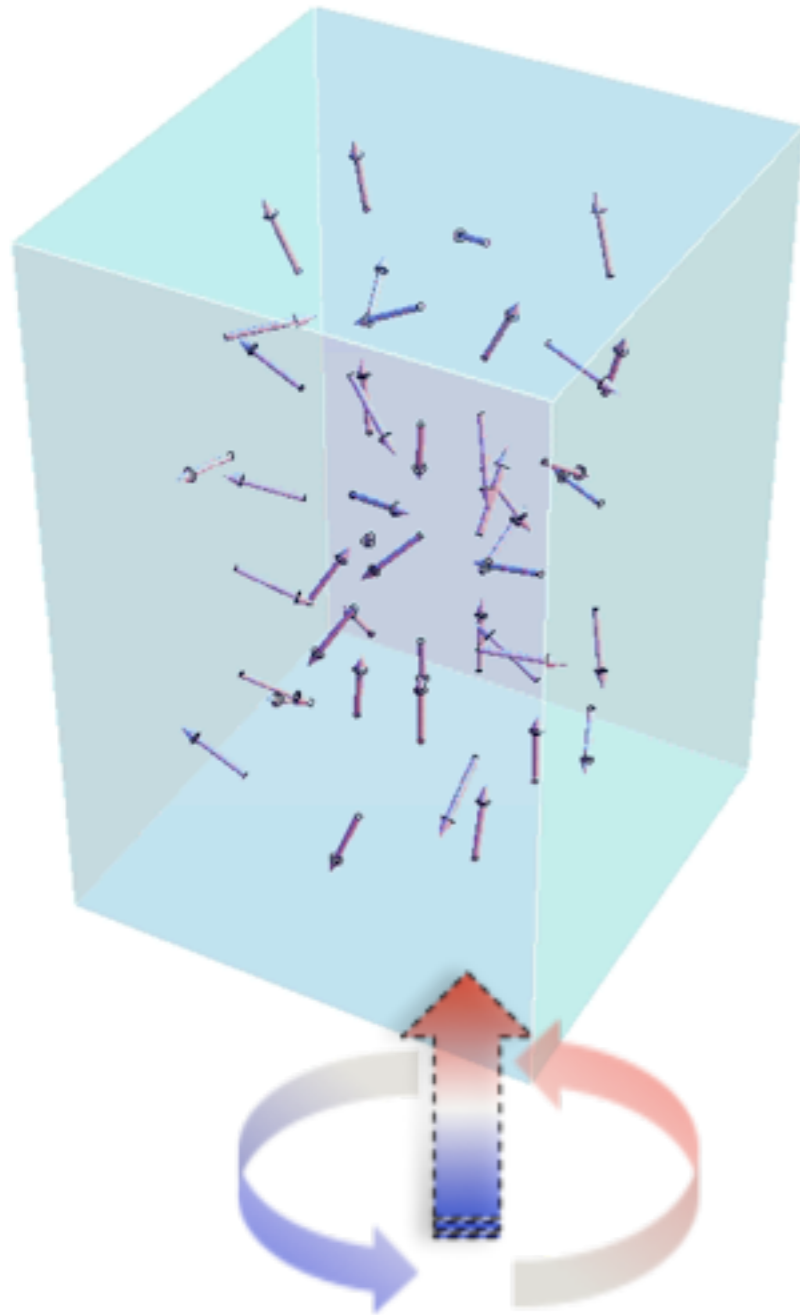


Magnetization by rotation: Barnett effect (1915)

$$H_{\text{Spin-rotation}} = S \cdot \Omega$$

$$H = L \cdot \Omega$$

L : angular momentum,
 Ω : rotation frequency



Rotation ~ Magnetic field



By Dr. Chudo

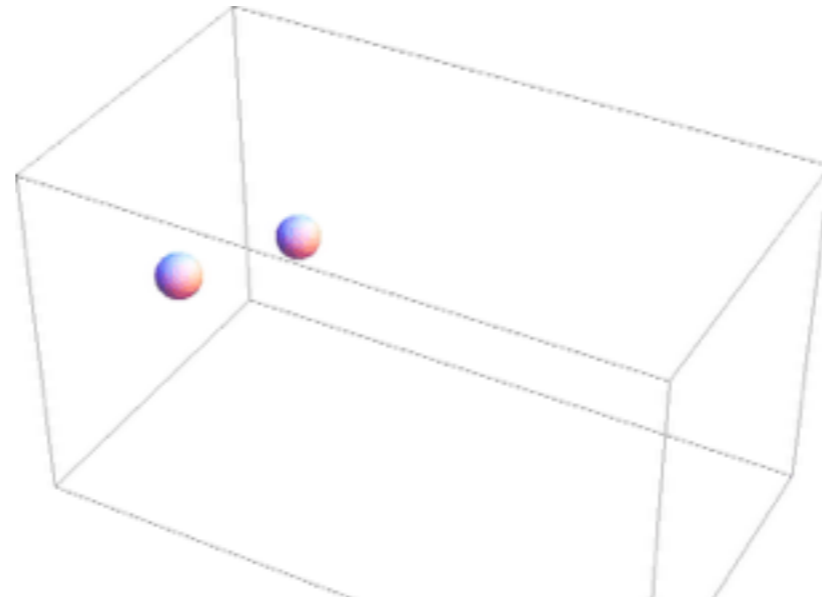
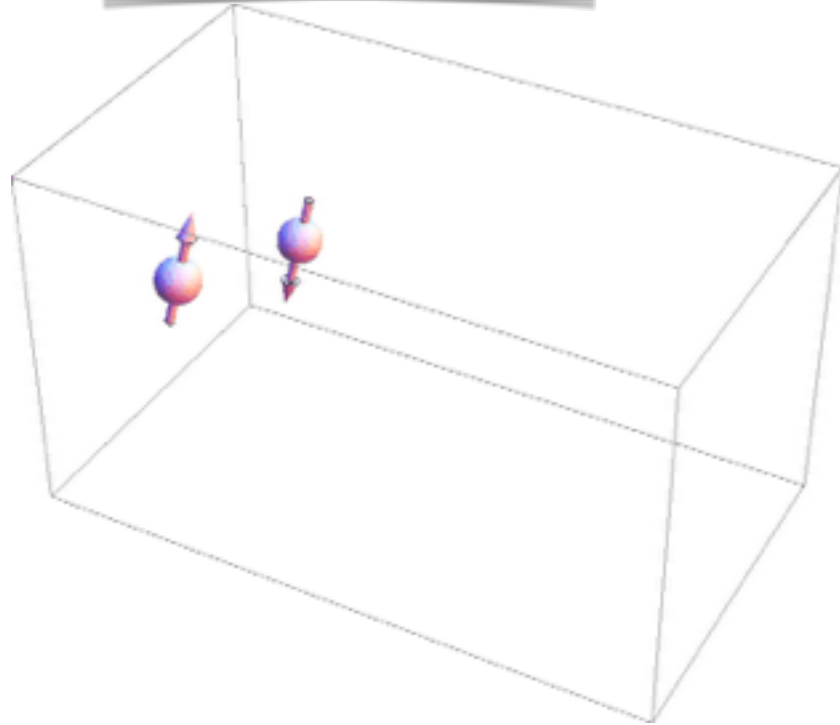
$$H_{\text{Zeeman}} = S \cdot \gamma B$$

$$B_{\Omega} = \frac{\Omega}{\gamma} \left[\gamma = \frac{e}{m} : \text{gyromagnetic ratio} \right]$$

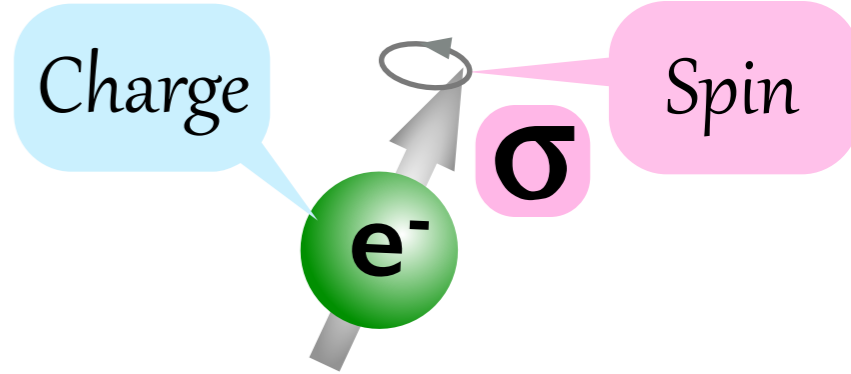
$$H_{\text{Spin-rotation}} = S \cdot \Omega$$

Charge current and spin current

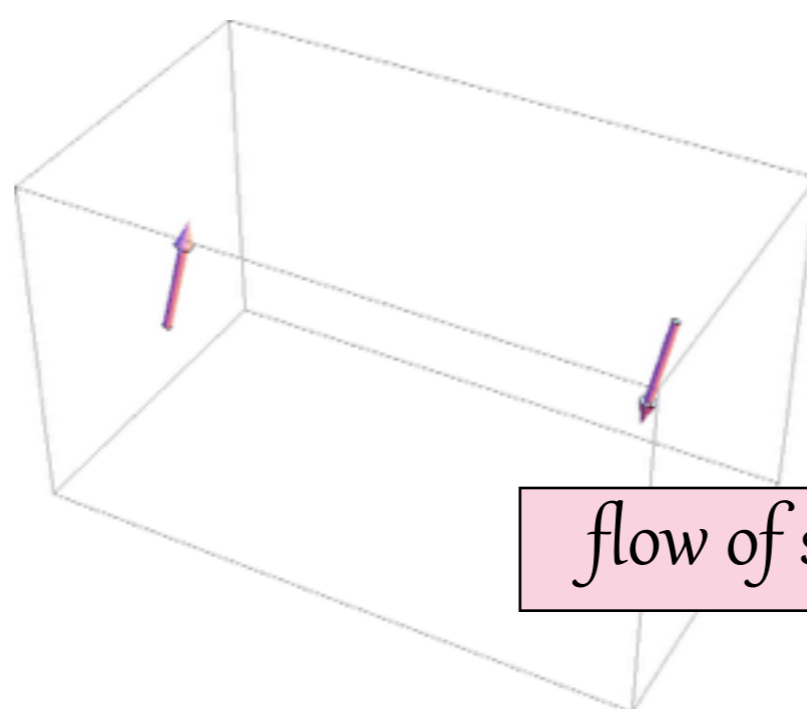
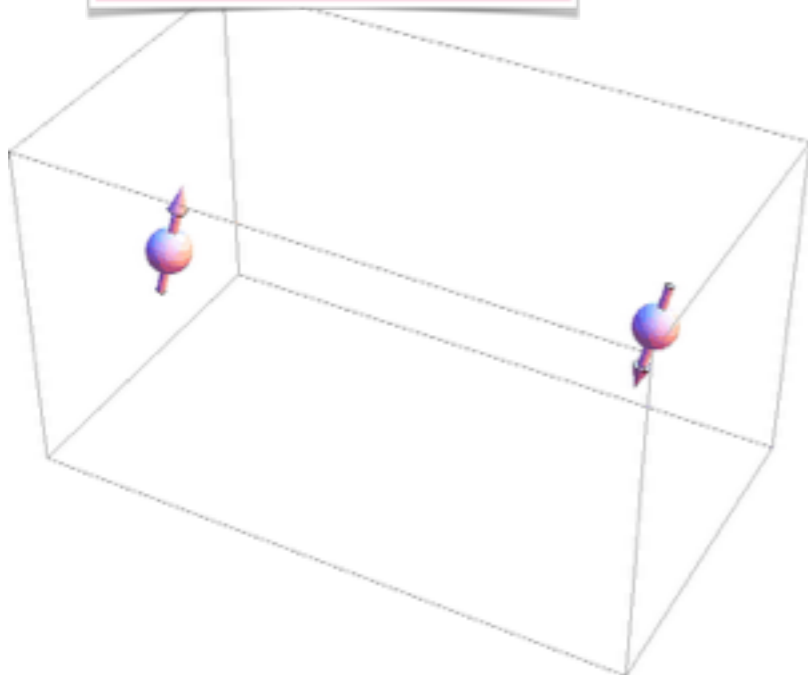
Charge current



flow of charges



Spin current

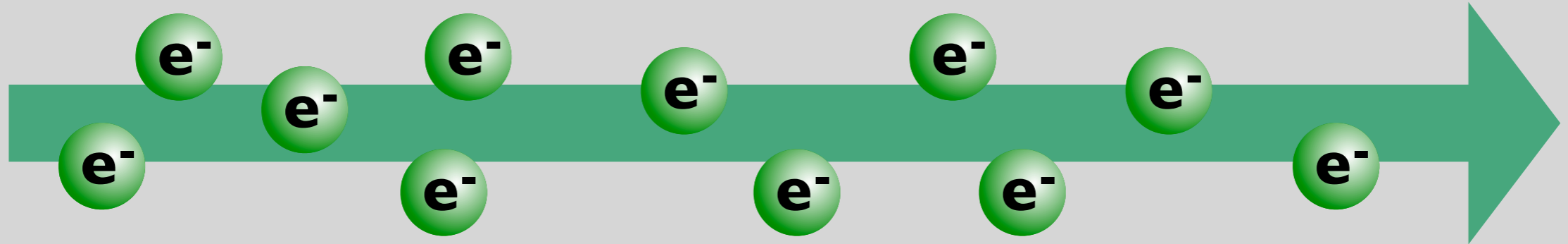


flow of spins

Spin current is fragile

Charge current:
conserved

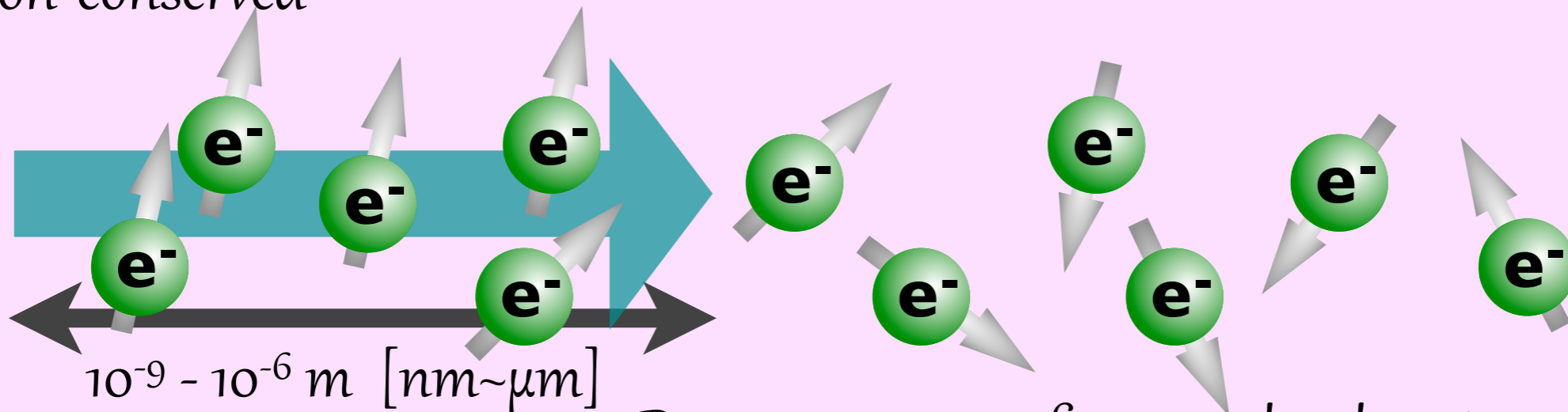
→ can travel infinite distance



Easy to control → Electronics in 20th century

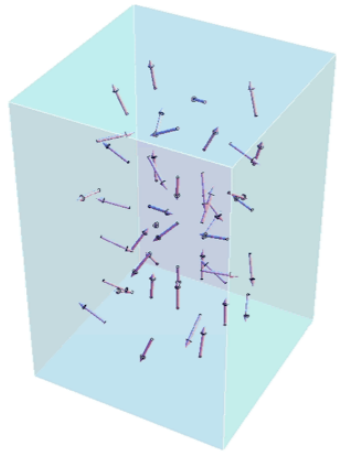
Spin current:
non-conserved

→ can travel only short distance [nm~ μ m]

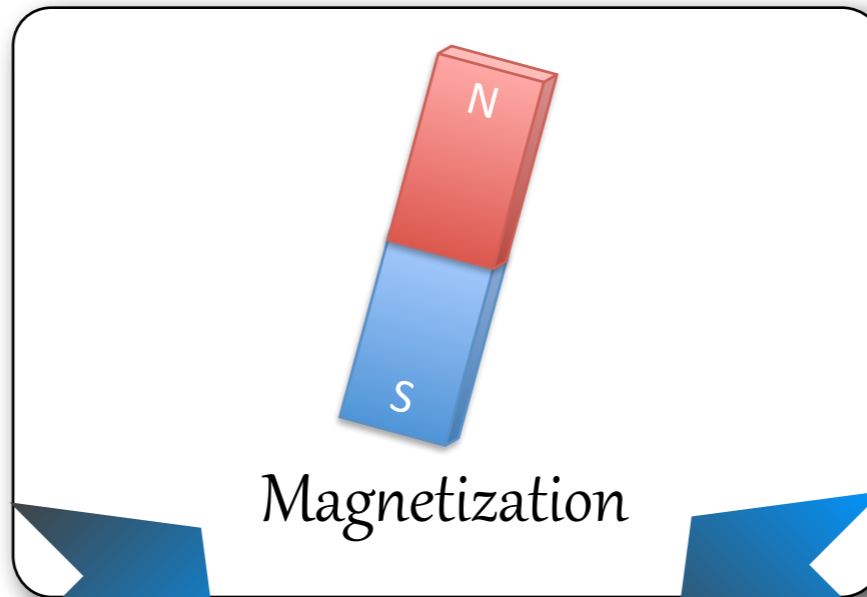


Recent progress of nanotechnology in spintronics
allows us to utilize spin current!

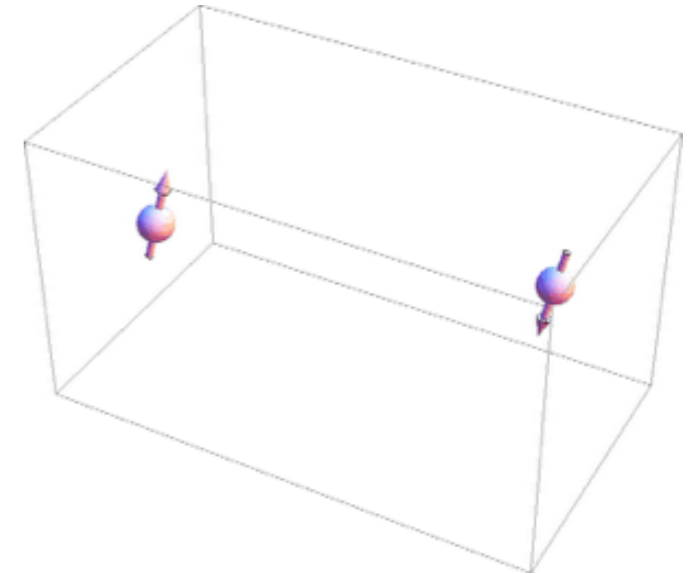
Motivation



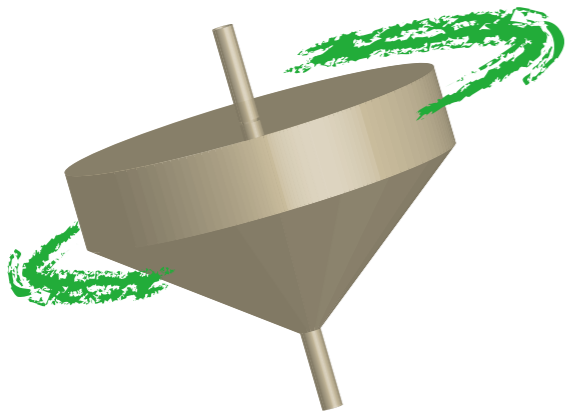
Einstein-de Haas
Barnett (1915)



Magnetization



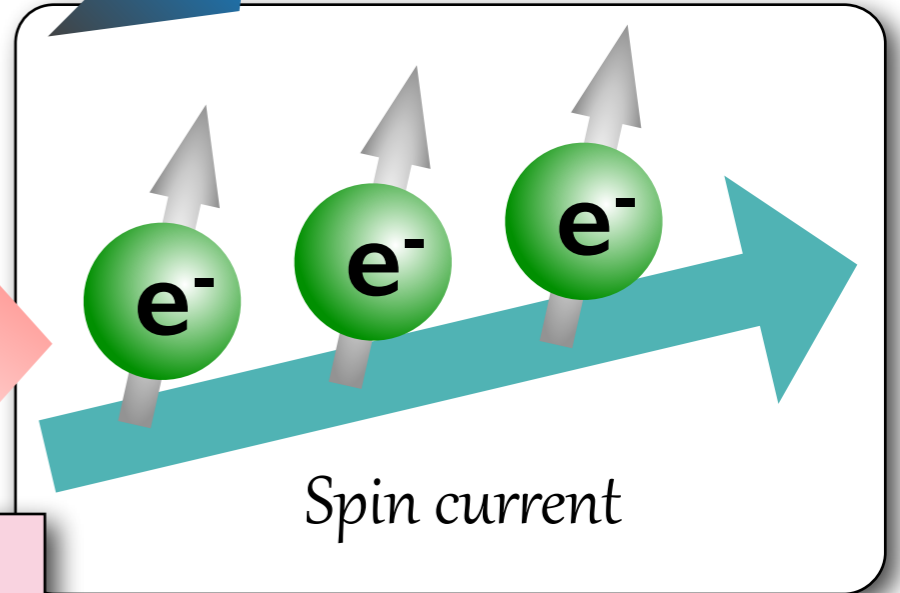
Spintronics (21st c)



Mechanical rotation



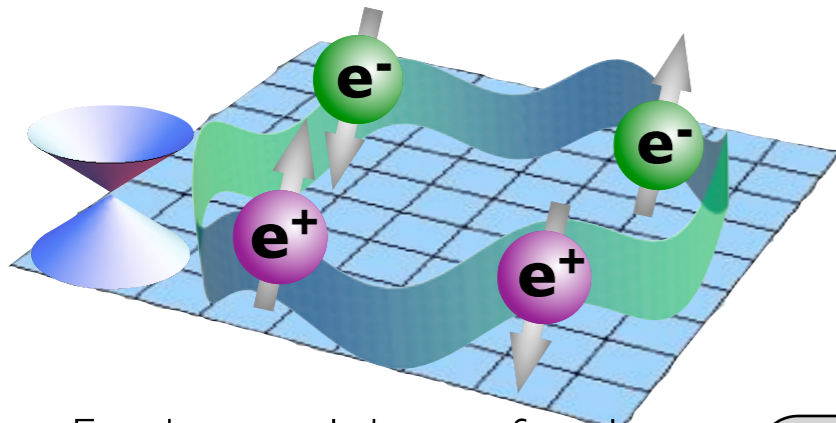
Direct link?



Spin current

Quantum theory in accelerating systems

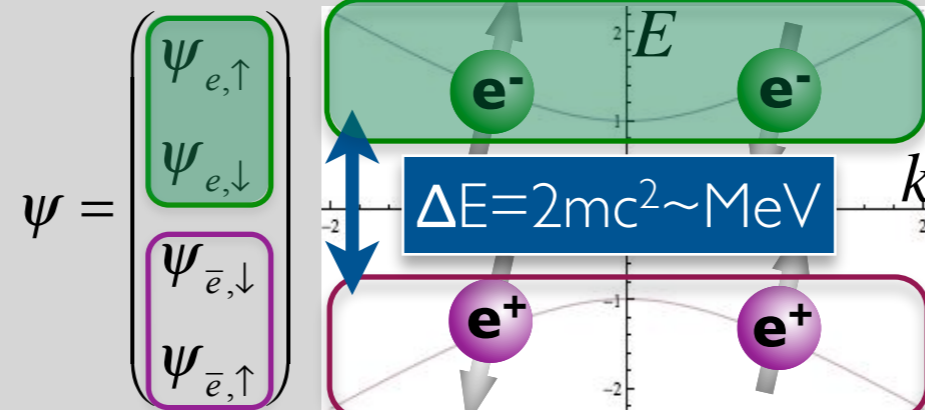
Special Relativistic Dirac equation



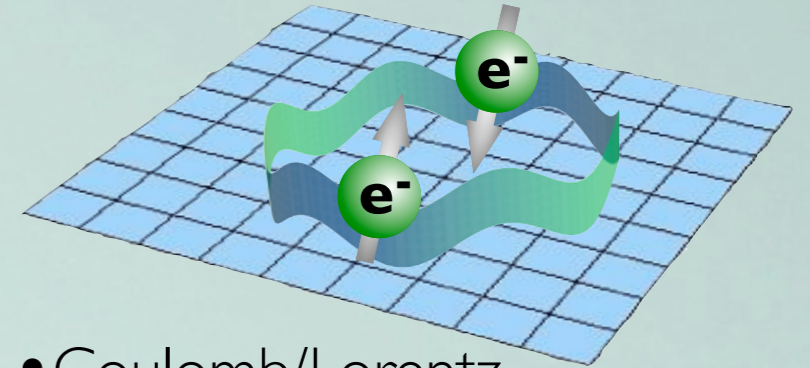
Fundamental theory for electron in non-accelerating systems

spin-1/2 electron/positron

Low energy limit



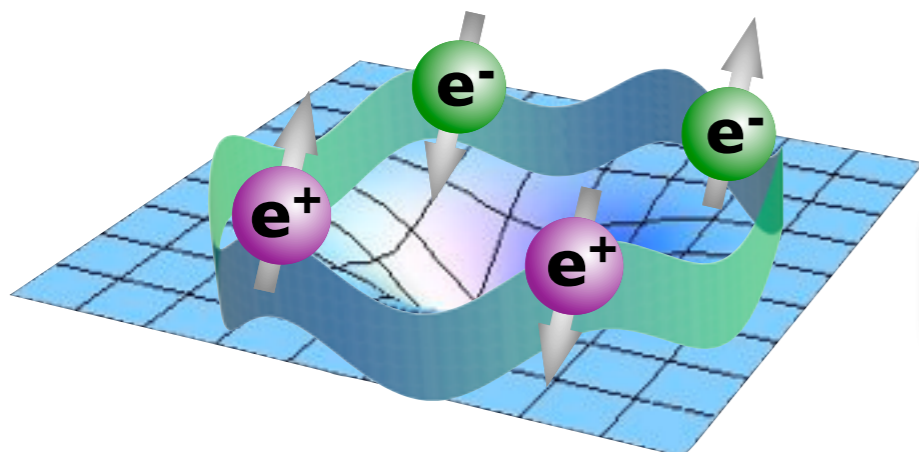
Pauli-Schrödinger equation



- Coulomb/Lorentz
- **Zeeman** (Spin precession)
- **Spin-Orbit** (Spin Hall)

spin-1/2 electron

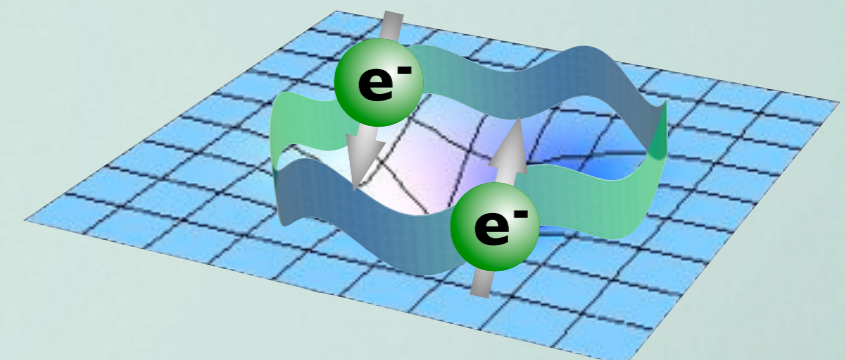
General Relativistic Dirac equation



Fundamental theory for electron in accelerating systems

Low energy limit

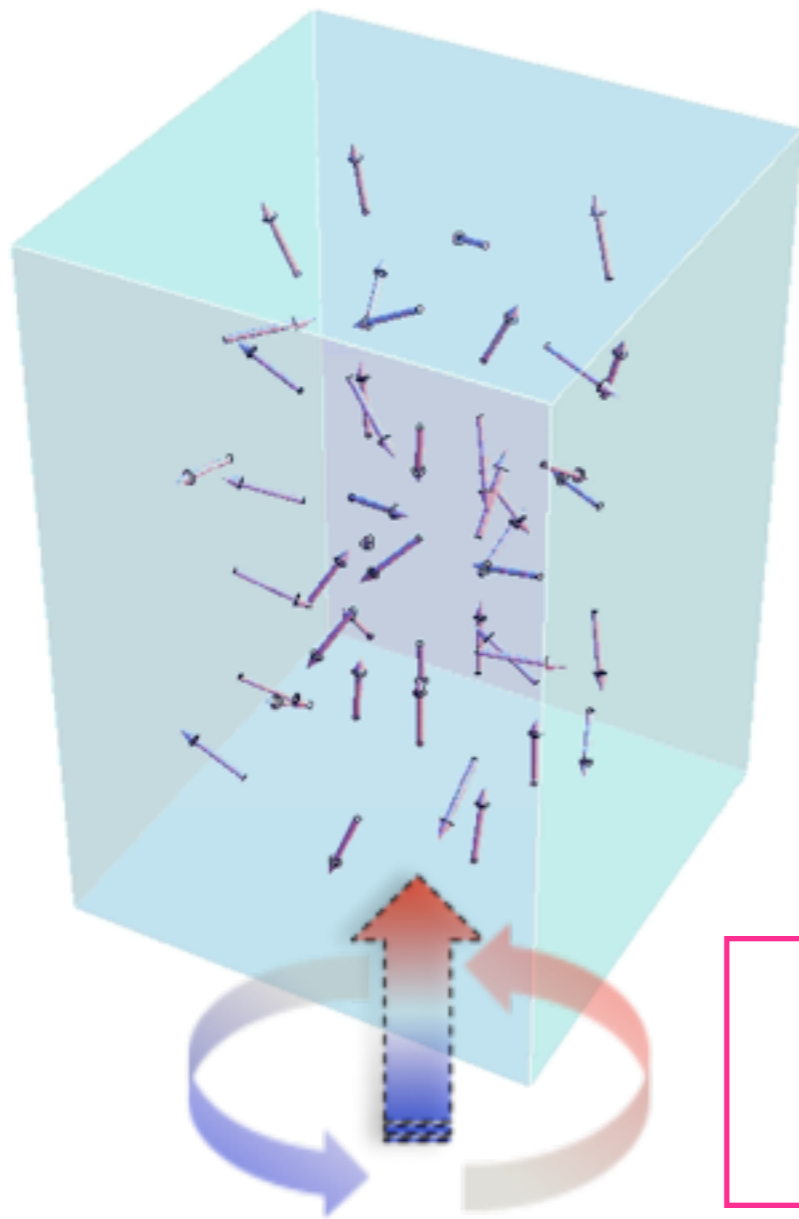
Pauli-Schrödinger equation in accelerating systems



Spin-rotation/vorticity

Magnetization by rotation: Barnett effect (1915)

$$H_{\text{Spin-rotation}} = S \cdot \Omega$$



Barnett detected magnetization of ferromagnets.

Can we observe the magnetic field due to mechanical rotation (Barnett field) ?

Rotation ~ Magnetic field

Barnett field observed by spinning NMR [1]

NMR spectrometer:
detect nuclear spin precession by induction

$$H_{\text{Zeeman}} = S \cdot \gamma B_0$$

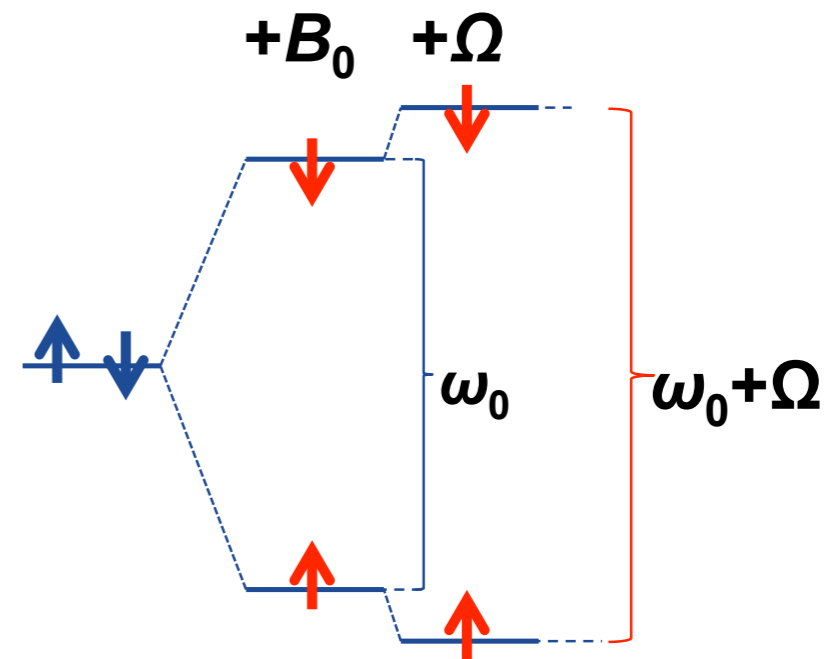
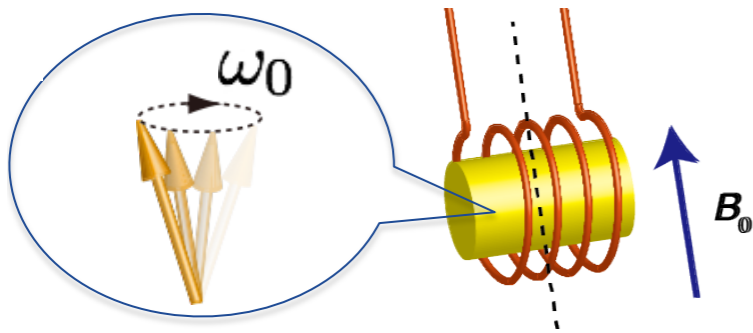
⇒ resonance condition :

$$\omega_0 = \gamma B_0$$

$$H_{\text{Zeeman+spin-rotation}} = S \cdot (\gamma B_0 + \Omega)$$

⇒ resonance frequency will be shifted :

$$\omega' = \omega_0 + \Omega$$

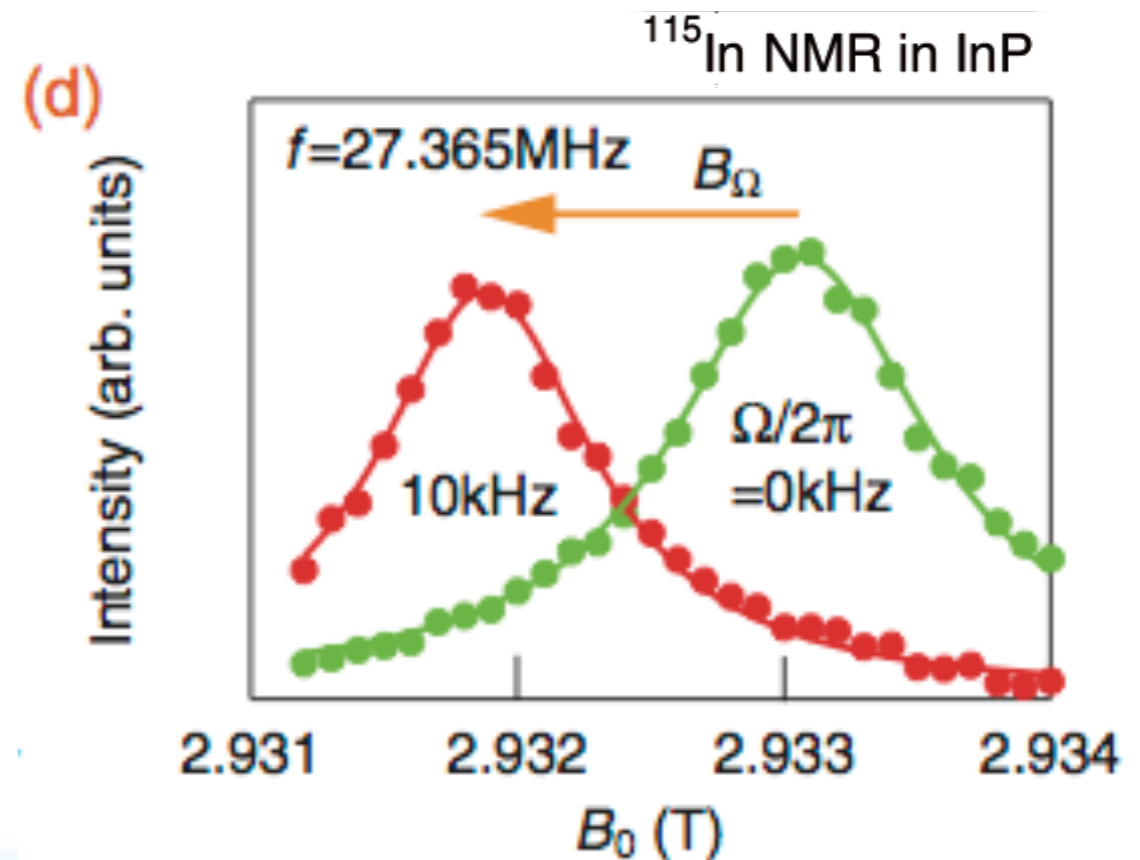
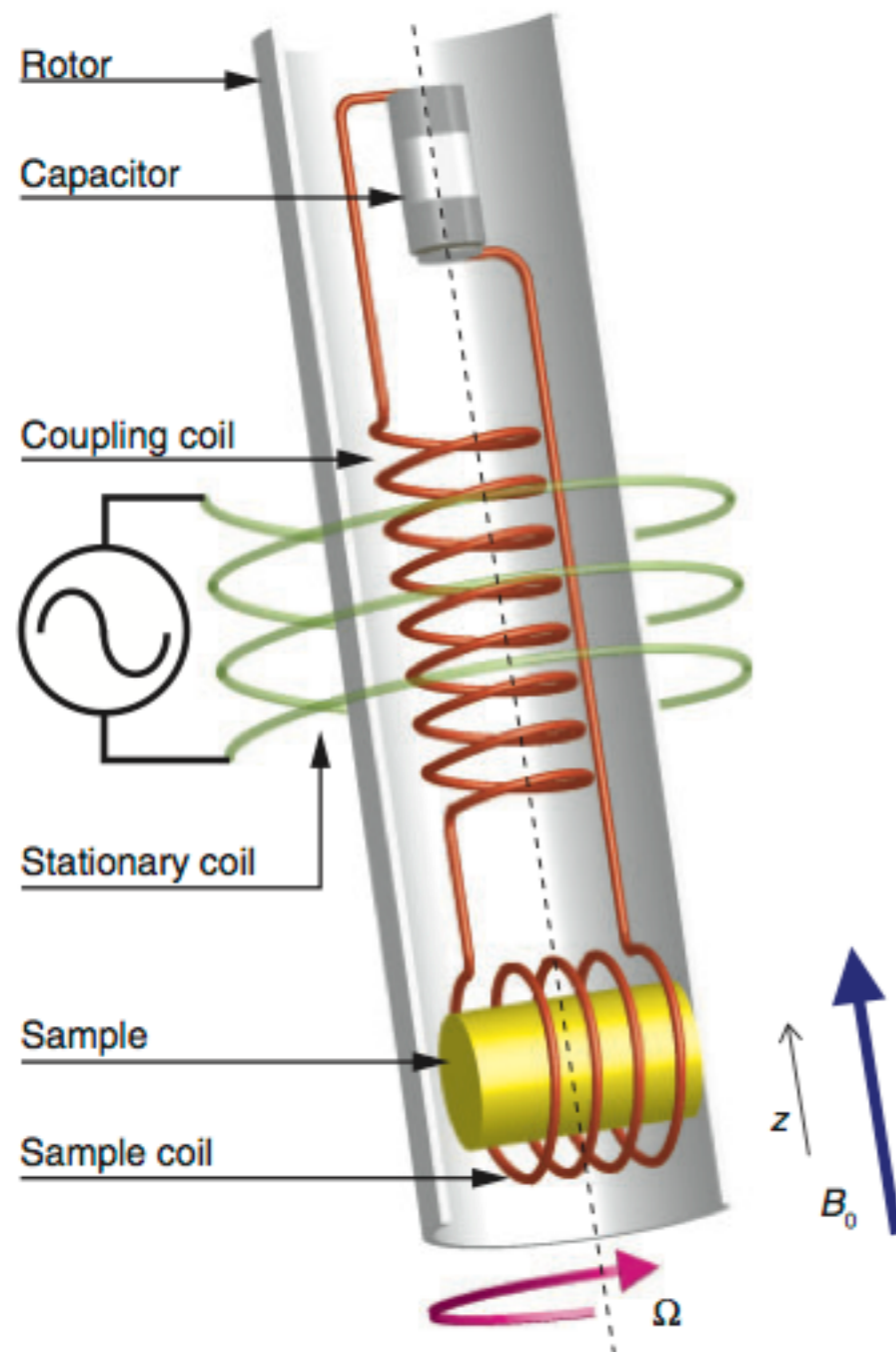


To observe magnetic field due to rotation,
NMR spectrometer should be rotated together with a sample.

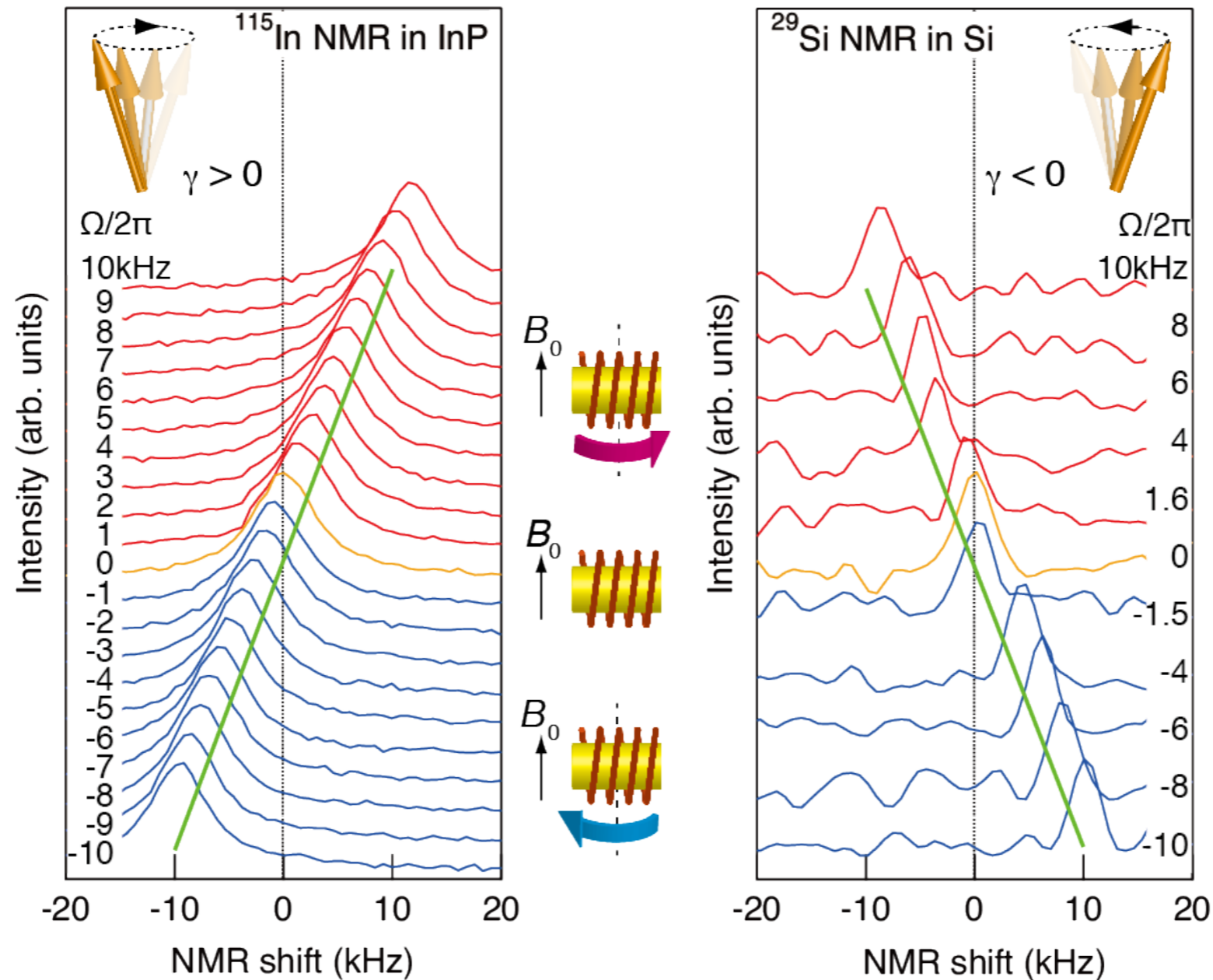
→ Need wireless system!

Barnett field observed by spinning NMR [2]

Chudo et al., Appl. Phys. Express 7, 063004 (2014)



Barnett field observed by spinning NMR [3]



^{115}In : $\gamma_{\text{In}} = 9.33 \text{ MHz/T}$
 ^{29}Si : $\gamma_{\text{Si}} = -8.45 \text{ MHz/T}$



Easily determine signs of
nuclear magnetic moments

PS46 Kazuya Harii "Rotation angle dependence
of NMR line structures in various nuclides"

Paramagnetic Barnett effect [1]

Sample: gadolinium

→ $T_c(292 \pm 0.5\text{K})$, near room temperature)

→ Large paramagnetic susceptibility

$$M_\Omega / \chi$$

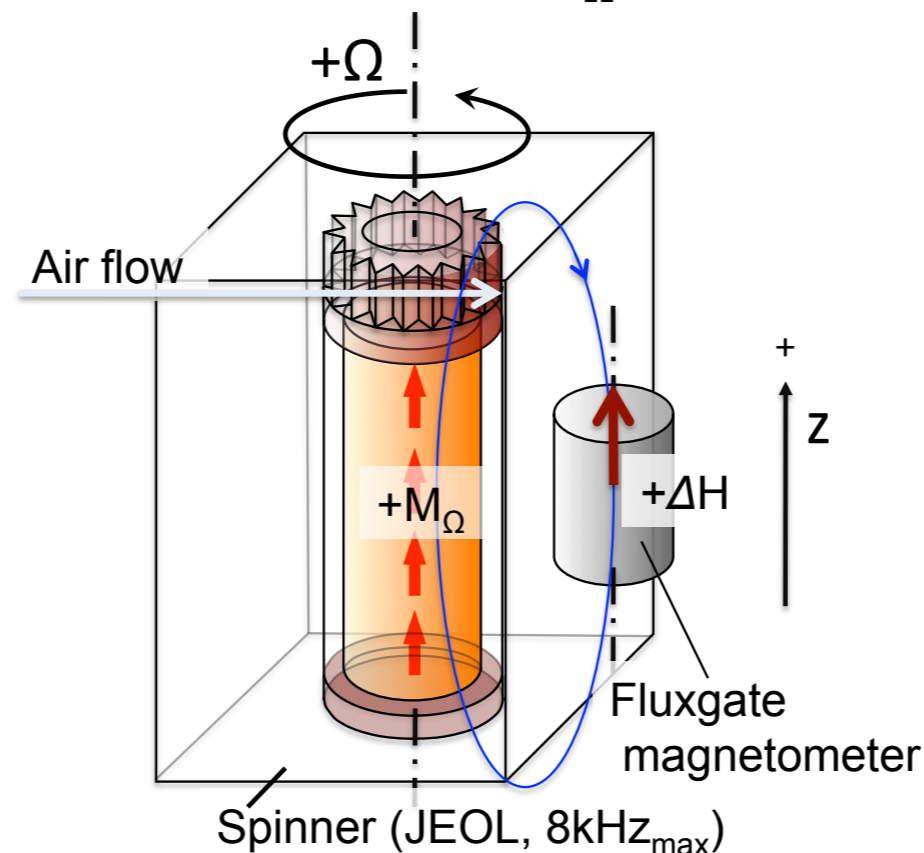
○ Susceptibility
SQUID fluxmeter (MPMS)

○ Estimation of magnetization M_Ω

measure the change of magnetic field around the sample ΔH_{stray} using a fluxgate magnetometer and estimate M_Ω using a dipole model.



Capsule ($\phi 8\text{mm}$),
Sample ($\phi 6 \times 20 \text{mm}$)



Apparatus for Barnett Effect
(*in situ* observation)



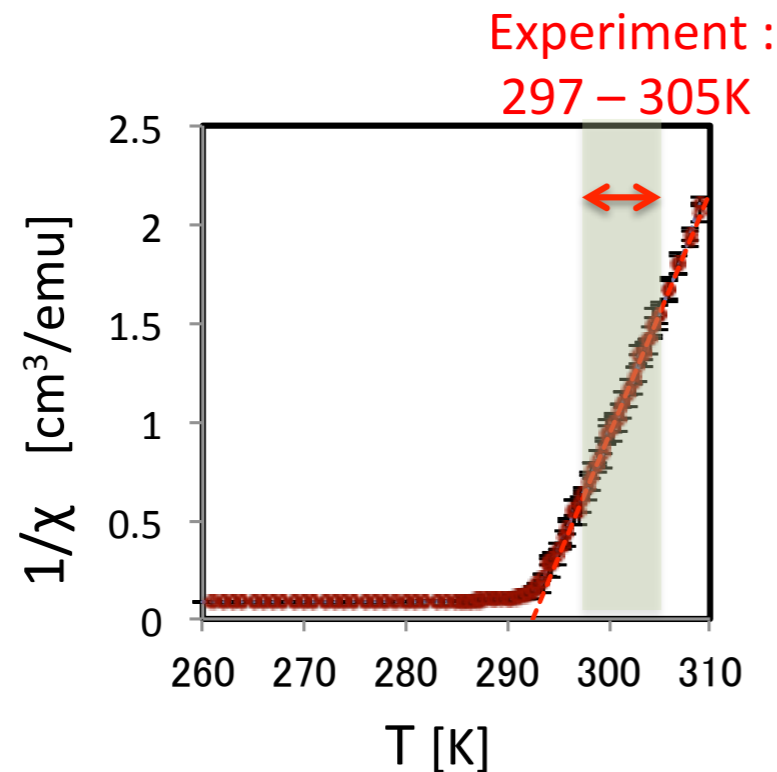
Magnetic shield
inside: 20nT

fluctuation: $<0.1\text{nT}$

PS29 Masao Ono "Barnett effect in a paramagnetic state"

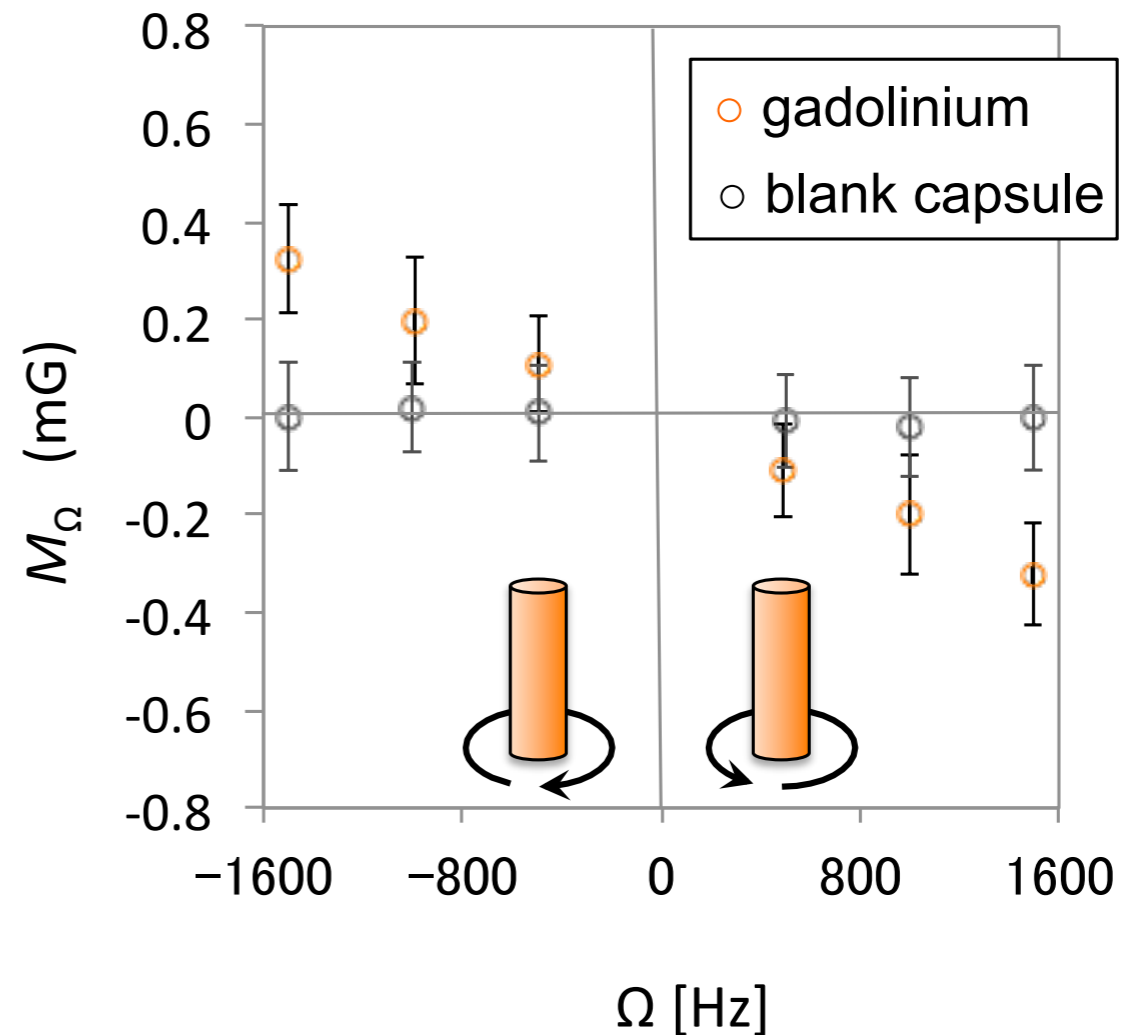
Paramagnetic Barnett effect [2]

- Temperature dependence of inverse magnetic susceptibility



→ The rotational experiments were performed in the paramagnetic state

- Rotational frequency dependence of magnetization ($300 \pm 0.5\text{K}$)



→ magnetization M_Ω is proportional to the rotation

Ono et al., in preparation

Spin-vorticity vs. Zeeman

Mechanical	Electromagnetic
$H_{\text{Spin-vorticity}} = S \cdot \Omega$	$H_{\text{Zeeman}} = S \cdot \frac{eB}{m}$
$\Omega = \frac{1}{2} \nabla \times \dot{u}$	$B = \nabla \times A$
\dot{u} : velocity field	A : vector potential

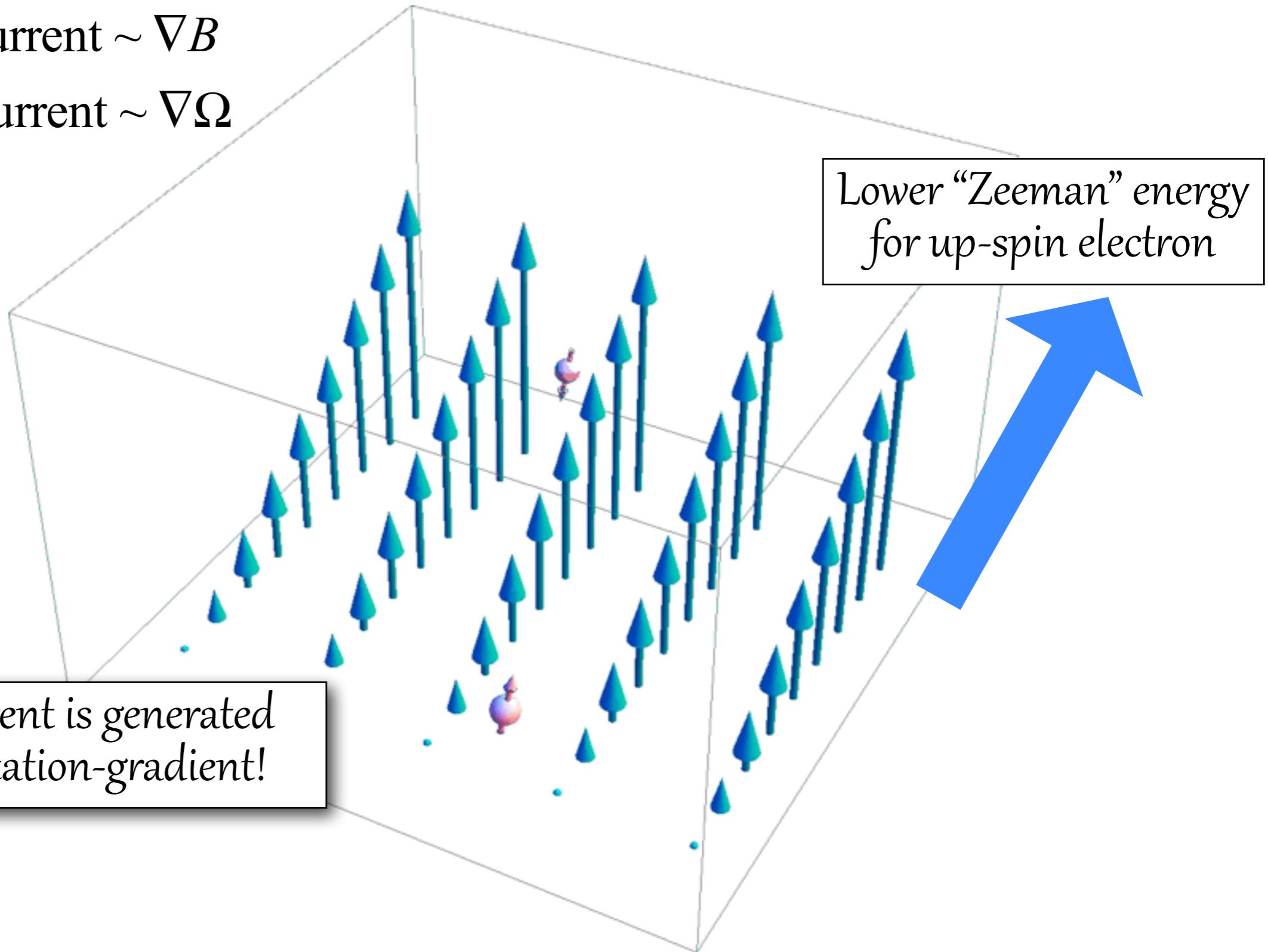
Mechanical Stern-Gerlach effect

$$S \cdot B \Rightarrow \text{Spin current} \sim \nabla B$$

$$S \cdot \Omega \Rightarrow \text{Spin current} \sim \nabla \Omega$$

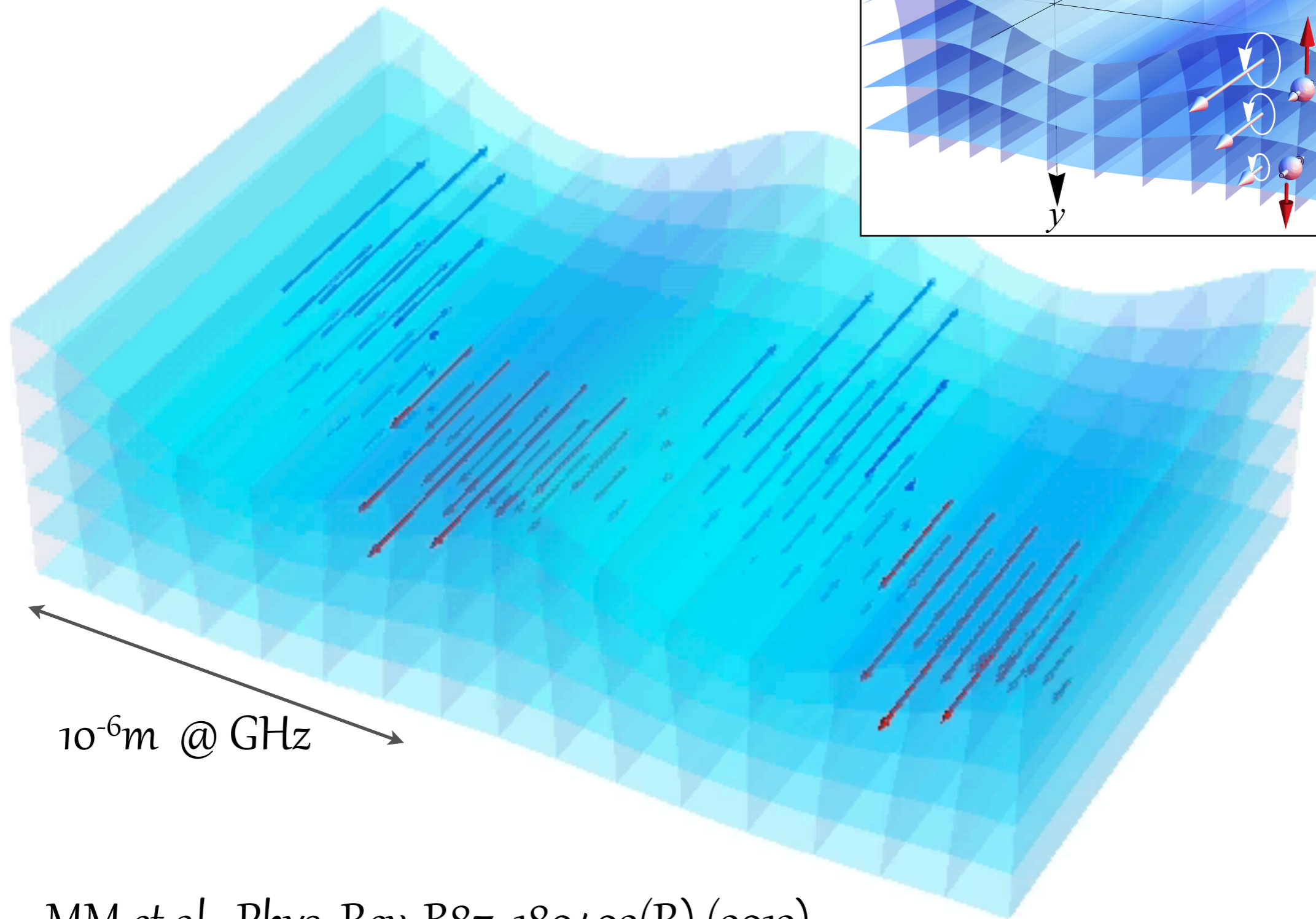
Lower "Zeeman" energy
for up-spin electron

Spin current is generated
along rotation-gradient!



Spin current from Surface Acoustic Wave

Spin current \propto Gradient of vorticity



MM et al., Phys. Rev. B87, 180402(R) (2013)