

# Quantum Hall effects at oxide heterointerfaces

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University of Tokyo*

**Quantum Hall effect**



**Superconductivity**

Generality

- **GaAs/AlGaAs**
- Si MOSFET, Si/SiGe
- InSb, CdTe
- Graphene
- Topological insulator HgTe, (Bi,Sb)<sub>2</sub>Te<sub>3</sub>
- **ZnO**

Diversity

- Metal (Al, Nb, In)
- Alloy (NbTi, Nb<sub>3</sub>Sn)
- High  $T_c$  ((La,Sr)<sub>2</sub>CuO<sub>4</sub>, YBCO)
- Iron-based (*Ln*FeAs(O,F), FeSe)
- Organic (Cs<sub>3</sub>C<sub>60</sub>)

# Collaborators

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*University of Tokyo*



Denis Maryenko

*RIKEN*



Atsushi Tuskazaki

*Tohoku University*



Benedikt Friess  
Ding Zhang  
Jurgen Smet

*Max-Planck Institute*



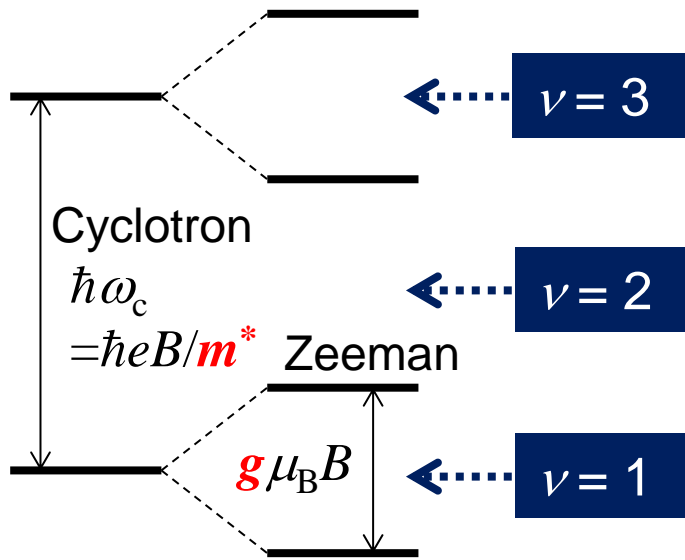
MAX-PLANCK-GESELLSCHAFT

# Quantum Hall Effect

$$\nu = \frac{(\text{\# of electrons})}{(\text{\# of magnetic flux quanta})} = \frac{\hbar n}{eB}$$

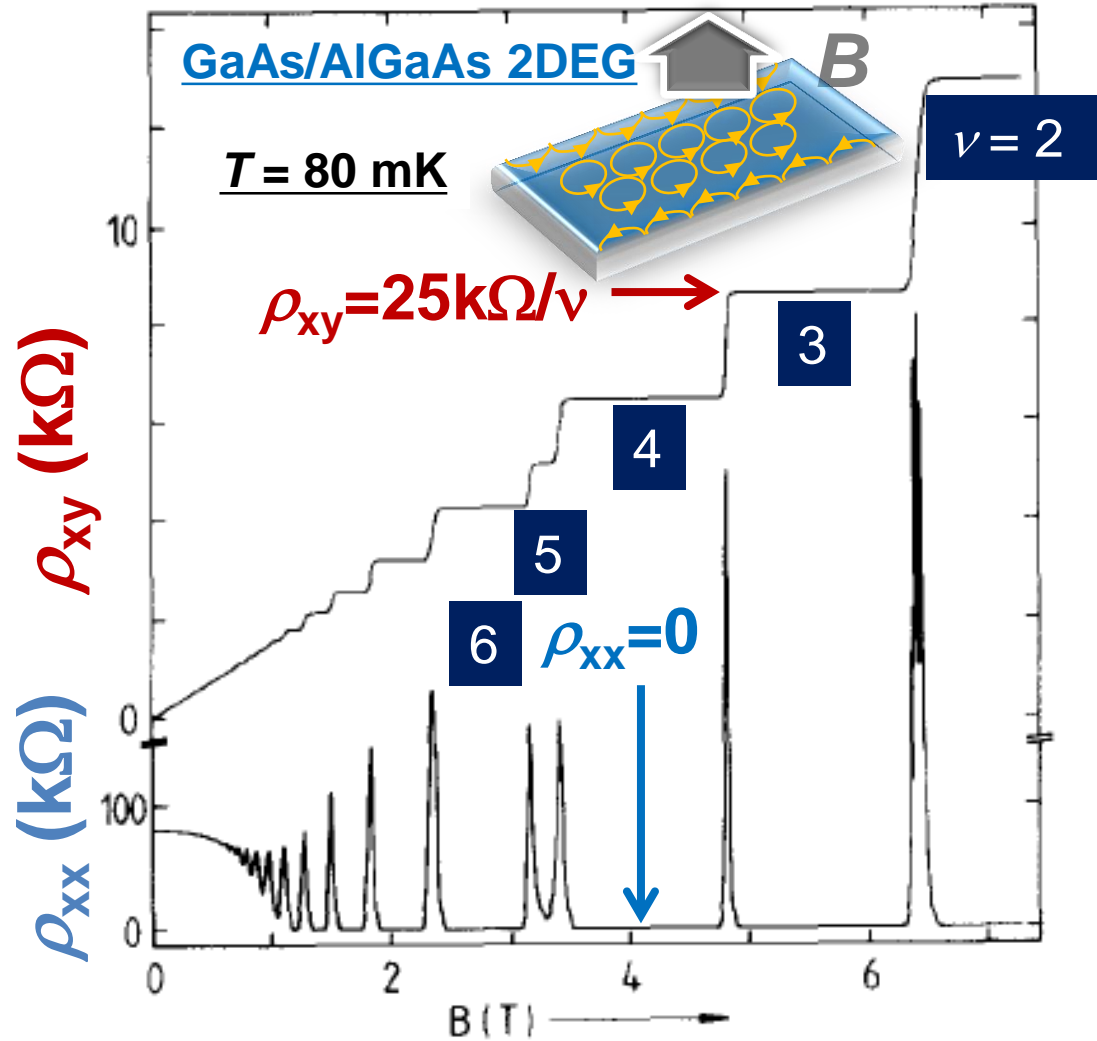
- $\hbar\omega_c > k_B T$
- $\omega_c \tau > 1$

$$\mu > 10,000 \text{ cm}^2/\text{Vs}$$



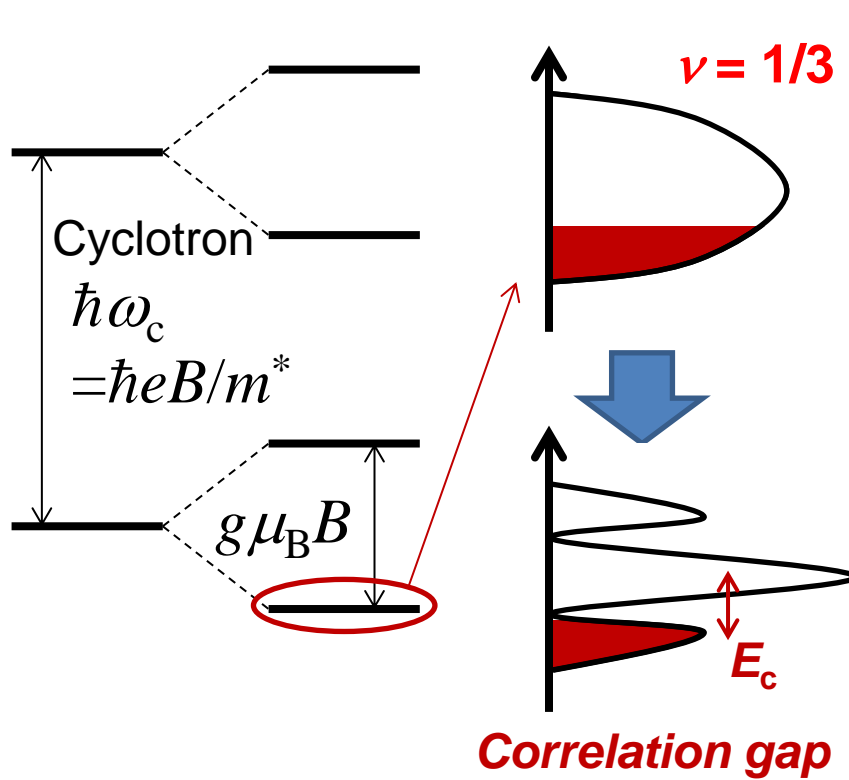
$$\Psi = \frac{C}{lm} z^m \exp\left[-\frac{|z|^2}{4l^2}\right]$$

( $z = x + iy$ : complex coordinate)



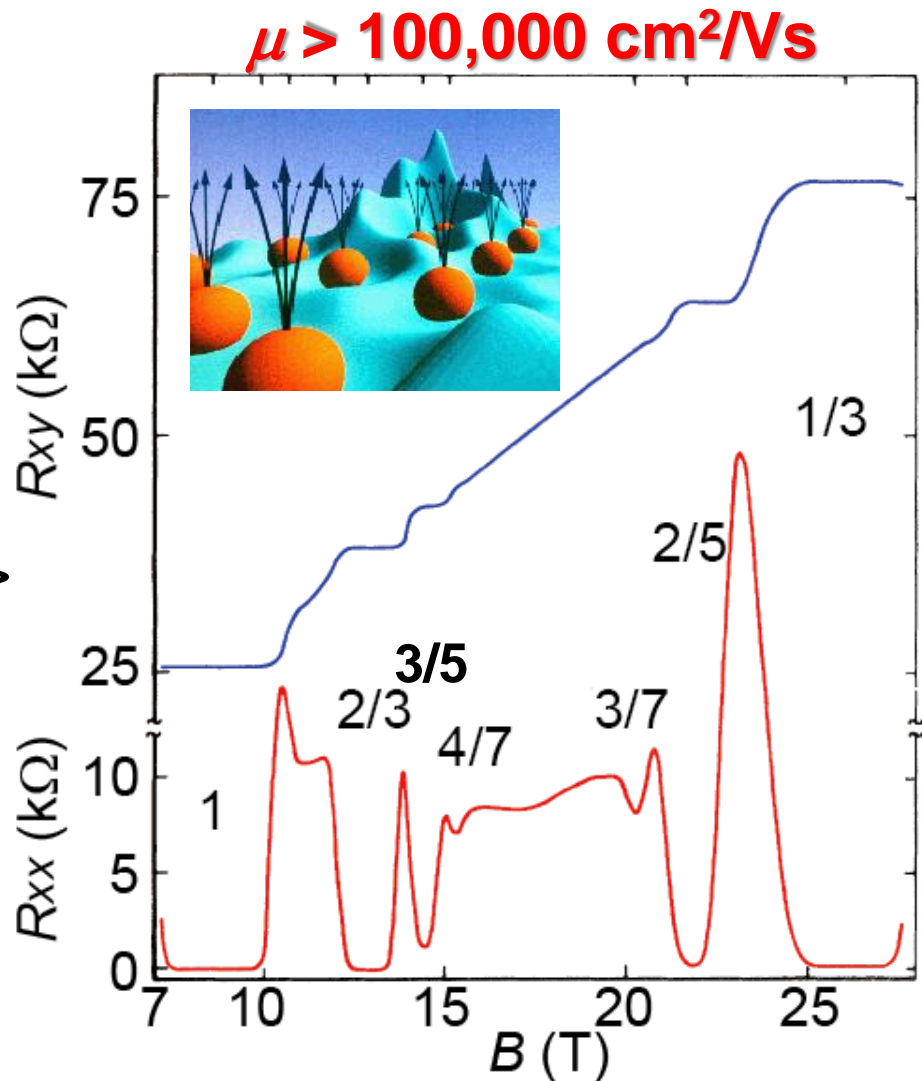
K. v. Klitzing, Physica **126B**, 242 (1984)

# Fractional quantum Hall effect



$$\Psi = \prod_{i < j} (z_i - z_j)^m \exp \left[ - \sum_k |z_k|^2 / 4l^2 \right]$$

$(\nu = 1/m)$

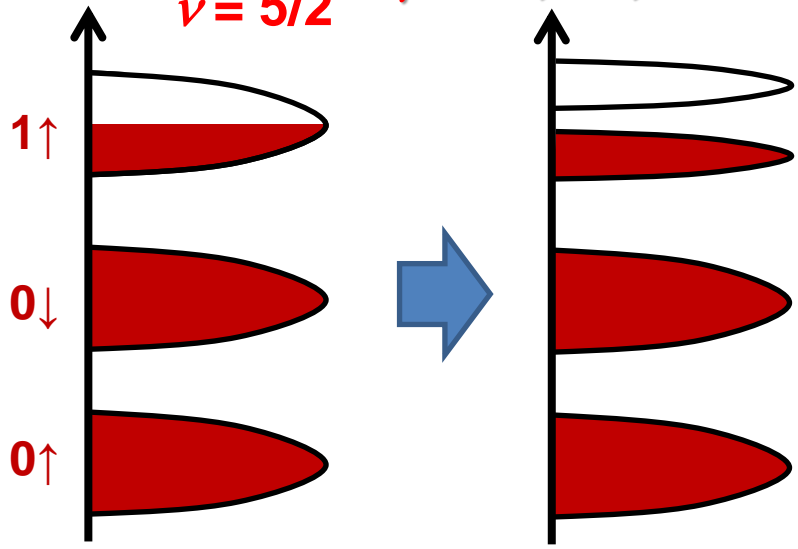


A. M. Chang *et al.*, Phys. Rev. Lett. **53**, 997 (1984)

# Even-denominator fractional quantum Hall effect

$\mu > 10,000,000 \text{ cm}^2/\text{Vs}$

$\nu = 5/2$

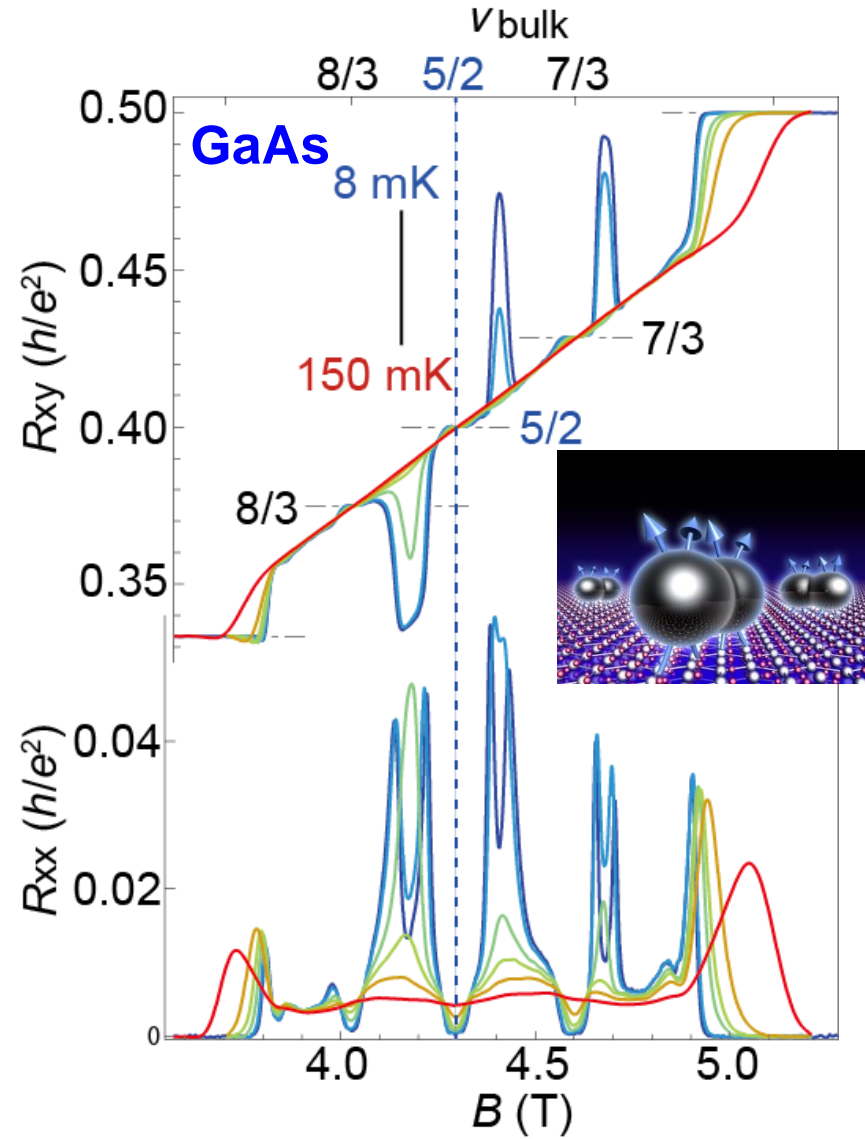


Pfaffian state

$$\Psi = \prod_{i < j} (z_i - z_j)^2 \text{Pf} \left[ \frac{1}{(z_i - z_j)} \exp \left[ - \sum_k |z_k|^2 / 4l^2 \right] \right]$$

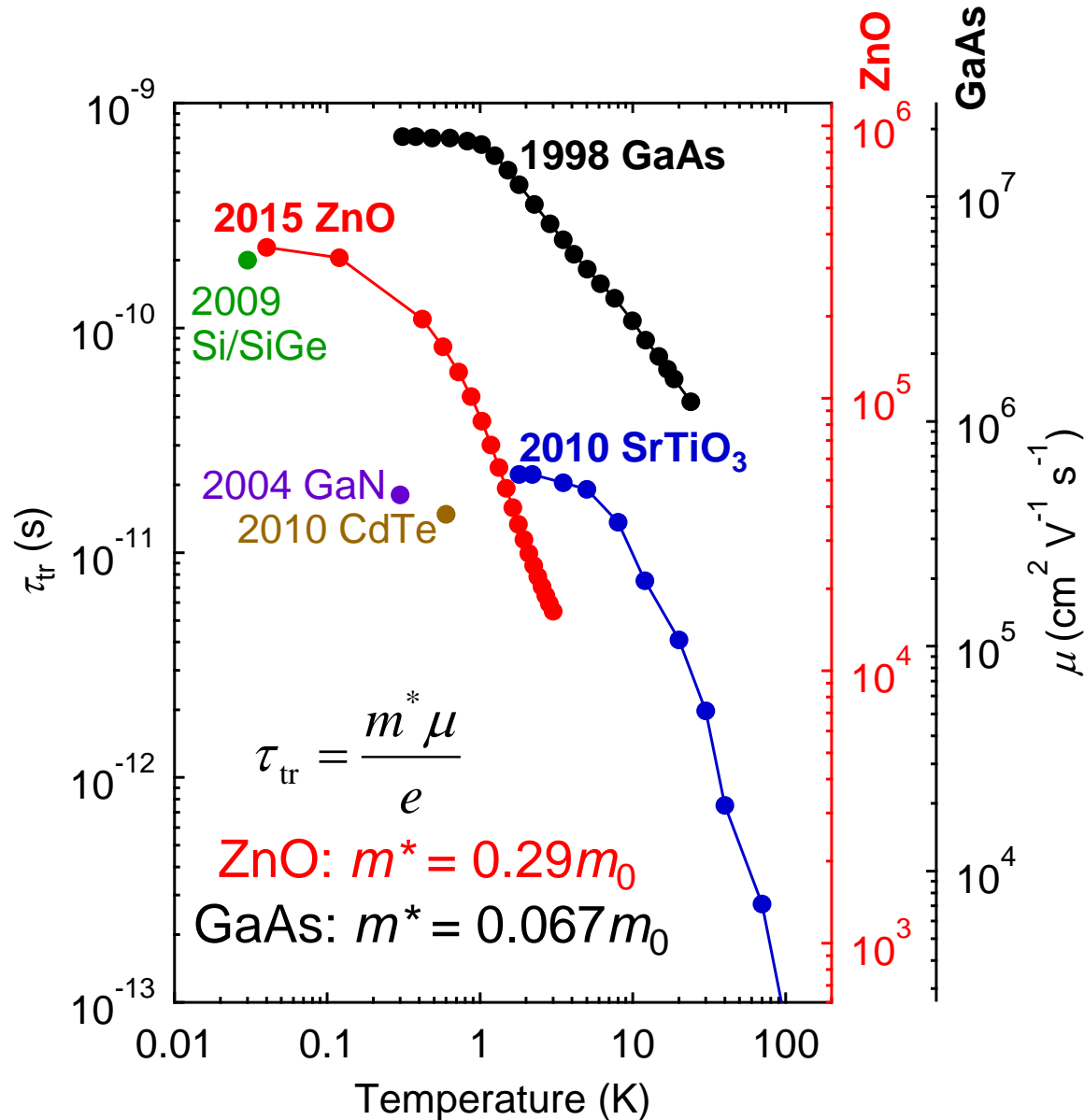
$$\left( \text{Pf} \frac{1}{(z_i - z_j)} = \frac{1}{z_1 - z_2} \frac{1}{z_3 - z_4} \frac{1}{z_5 - z_6} \dots \right. \\ \left. - \frac{1}{z_1 - z_3} \frac{1}{z_2 - z_4} \frac{1}{z_5 - z_6} \dots + \dots \right)$$

**Fragile and competing with other phases**

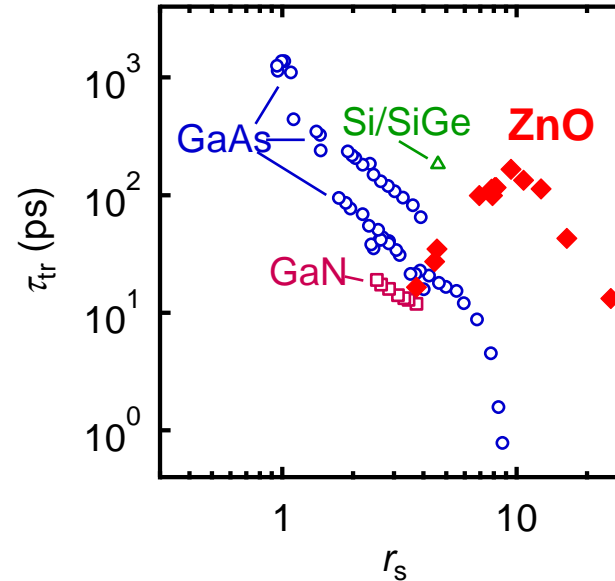
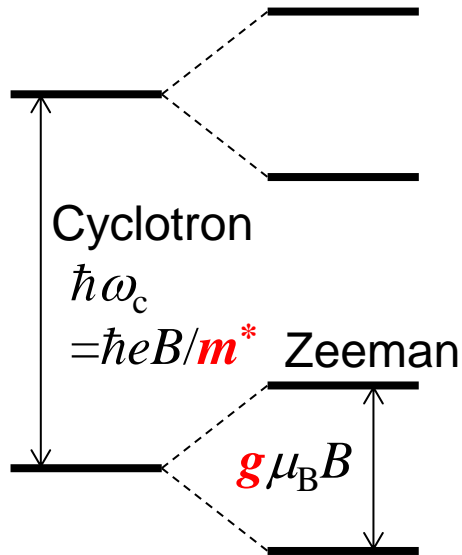


J. B. Miller et al., Nat. Phys. 3, 561 (2007)

# High mobility electrons in oxides



# Comparison of materials parameters 7

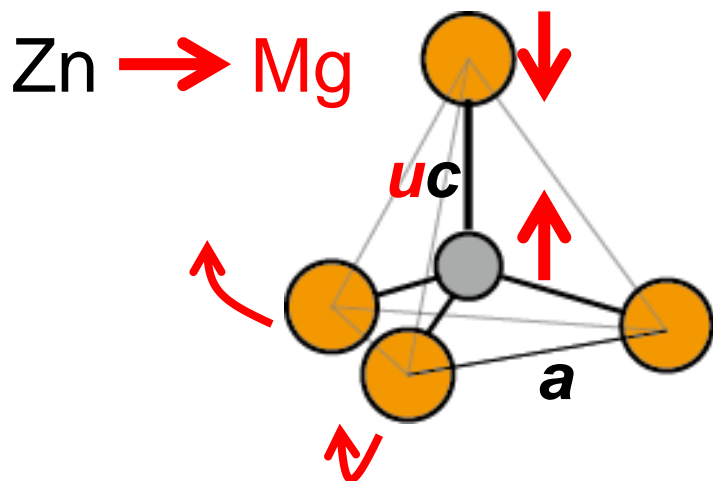
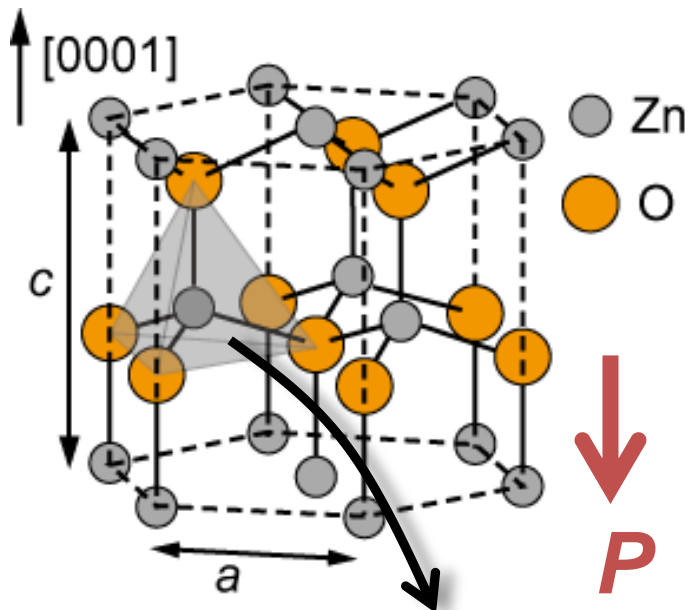


	GaAs	ZnO
$m^*/m_0$	0.069	0.29
g-factor	-0.44	2
$\varepsilon$ (dielectric constant)	13	8.5
<b>(Zeeman)/(Cyclotron)</b>	<b>0.015</b>	<b>0.29</b>
<b><math>r_s</math> (Coulomb/Fermi energy)</b>	<b><math>1.8/\sqrt{n}</math></b>	<b><math>11.9/\sqrt{n}</math></b>
<b>Landau level mixing (Coulomb/Cyclotron)</b>	<b><math>2.6/\sqrt{B}</math></b>	<b><math>17.2/\sqrt{B}</math></b>

$n$  ( $10^{11}$  cm $^{-2}$ )  
 $B$  (T)

# Polarization-induced 2DEG

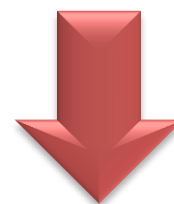
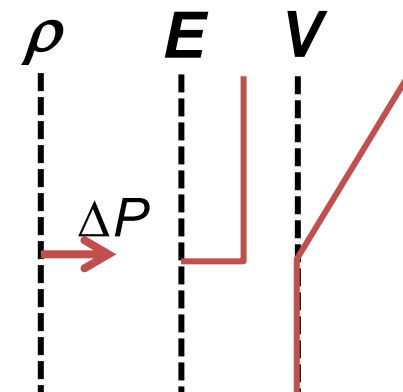
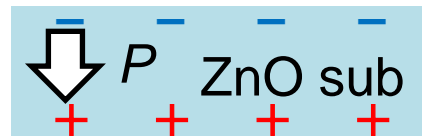
ZnO: Wurtzite



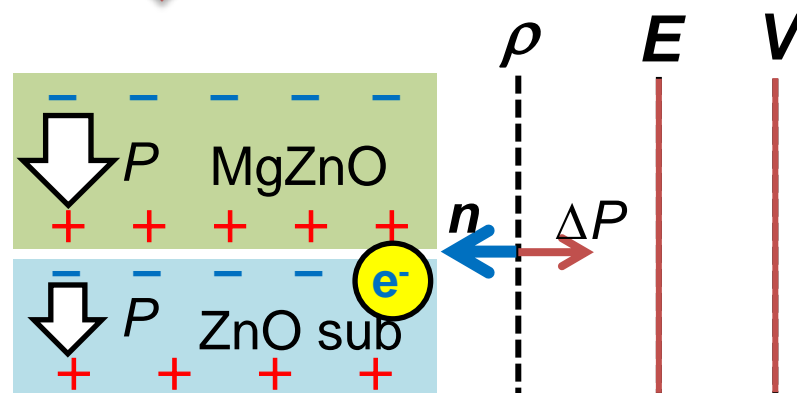
Zn surface



O surface

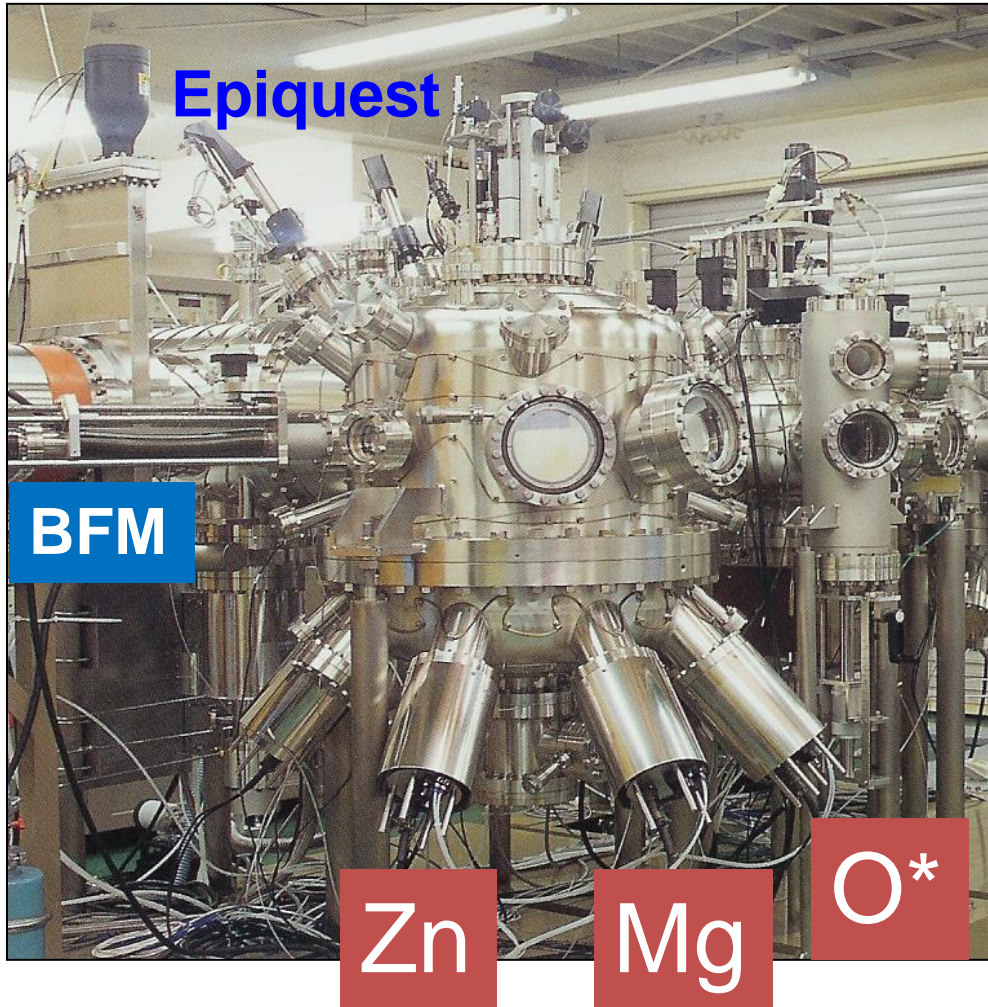


*Electronic reconstruction*





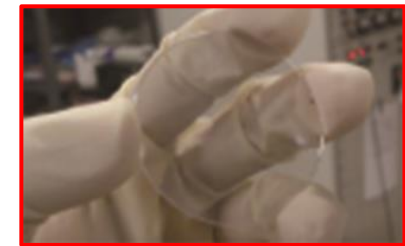
# Molecular beam epitaxy



• Sources Zn:7N Mg:6N

• ZnO single crystal substrate

Tokyo Denpa



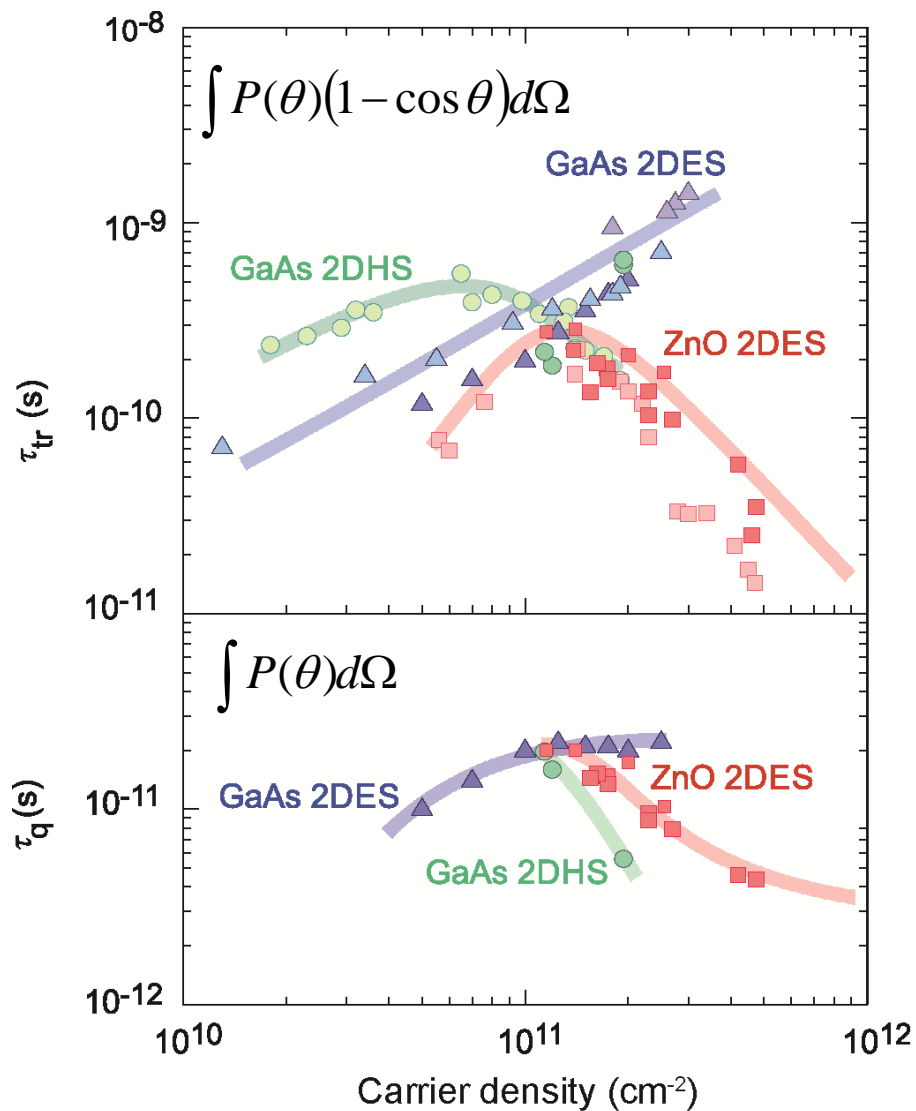
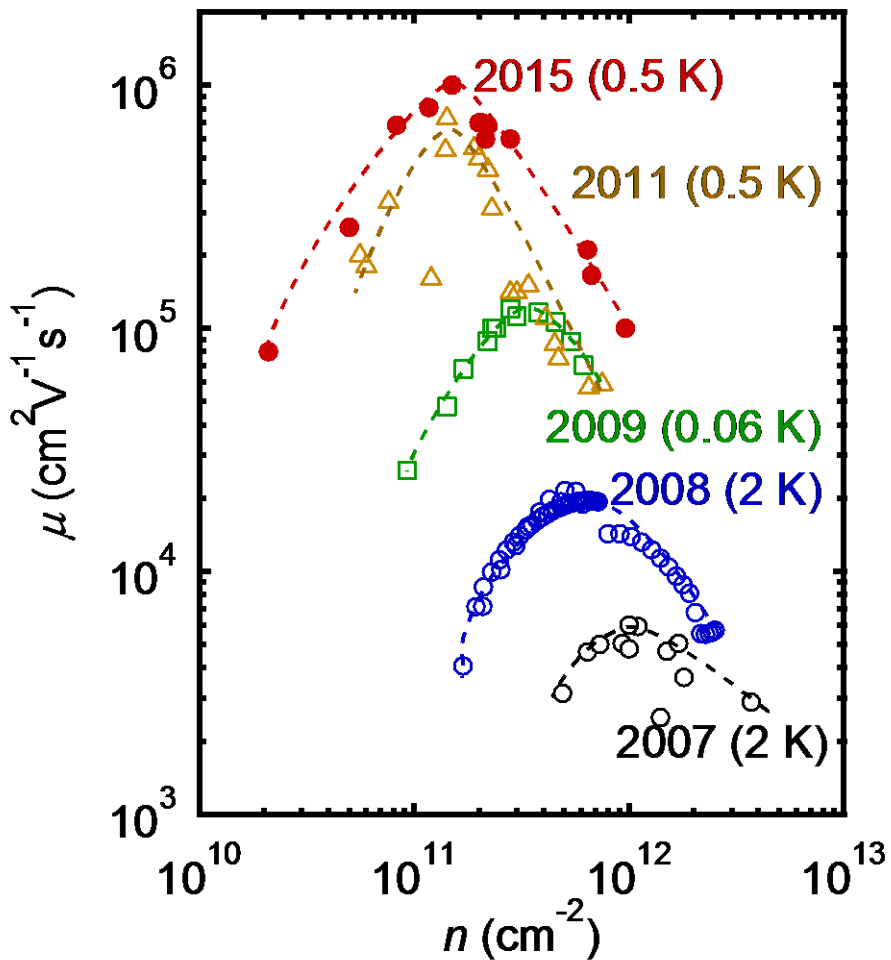
K. Maeda *et al.*, Semicond. Sci. Technol. **20**, S49 (2005)

• Pure Ozone

Meidensha Co.



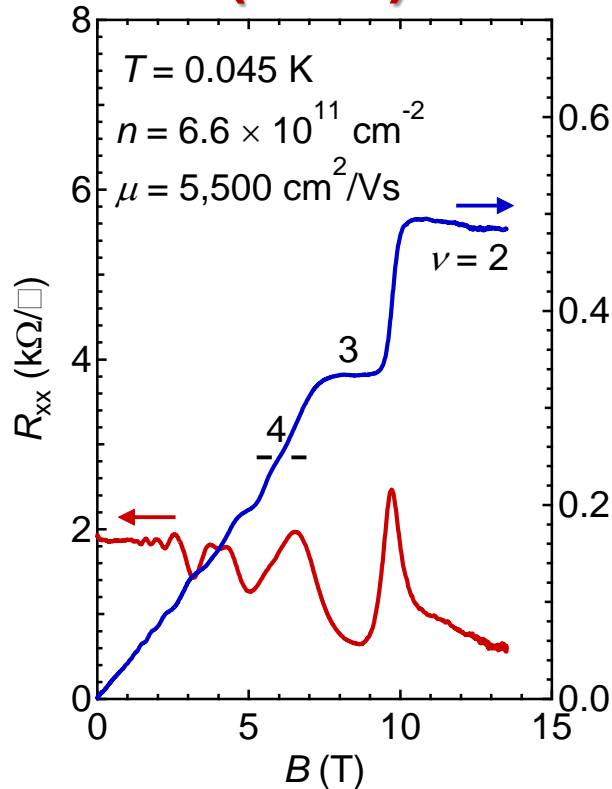
$\mu > 1,000,000 \text{ cm}^2/\text{Vs}$



# Quantum Hall Effects in ZnO

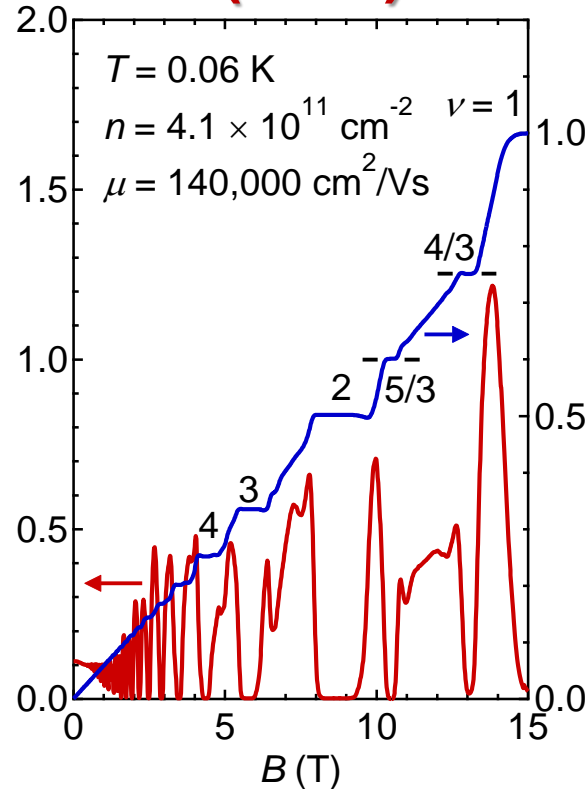
11

## Integer QHE (2007)



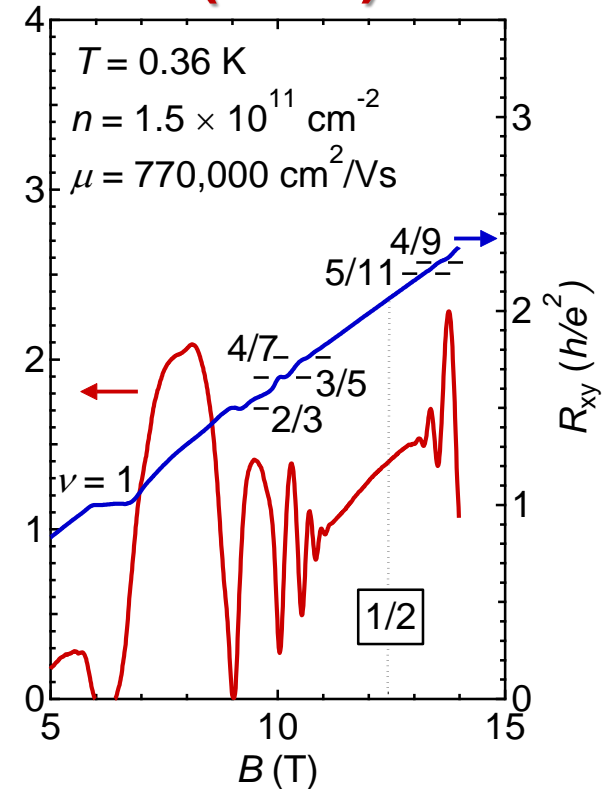
A. Tsukazaki *et al.*,  
Science **315**, 1388 (2007)

## Fractional QHE (2010)

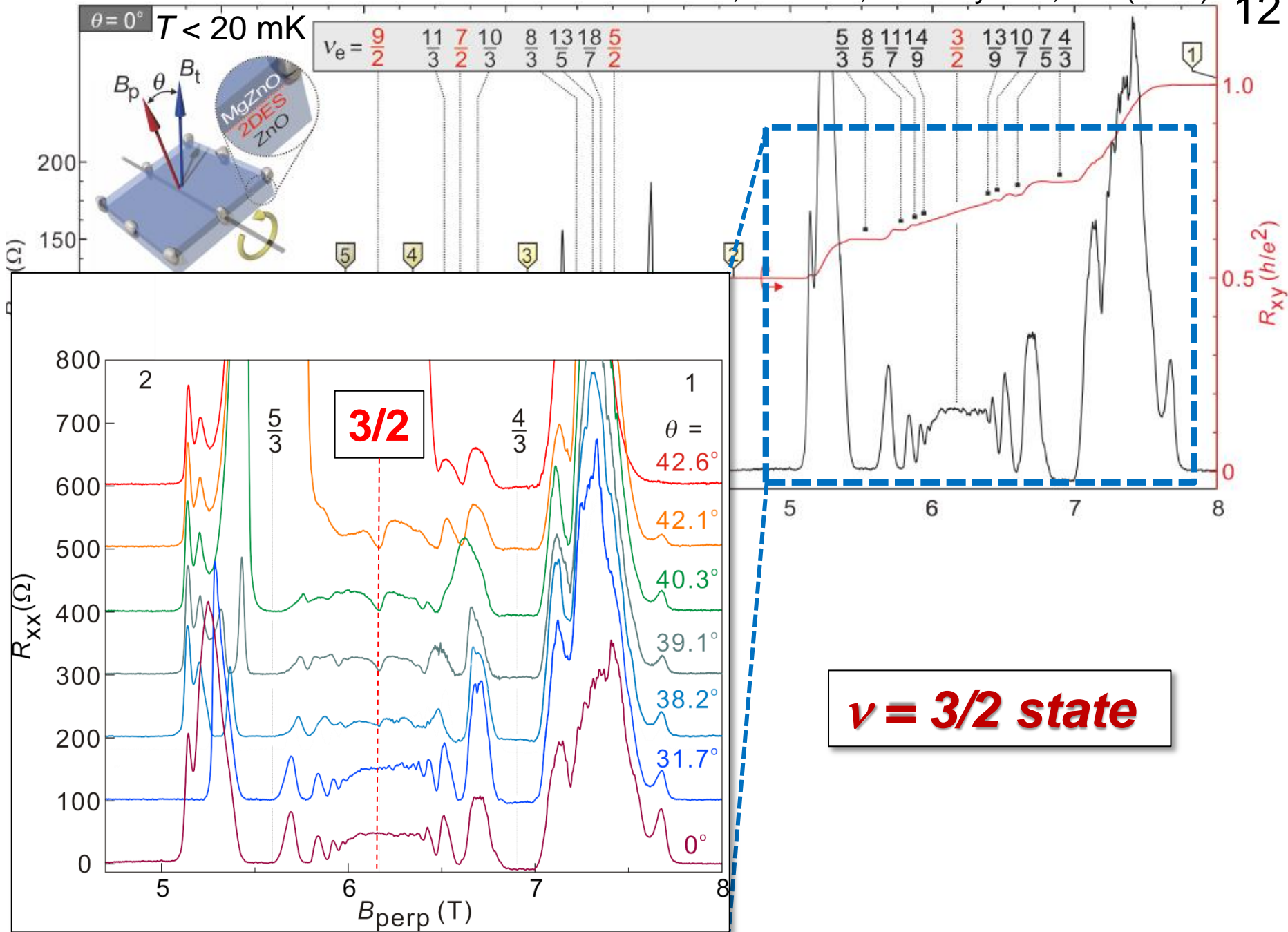


A. Tsukazaki *et al.*,  
Nature Mater. **9**, 889 (2010)

## Fractional QHE ( $\nu < 1$ ) (2012)



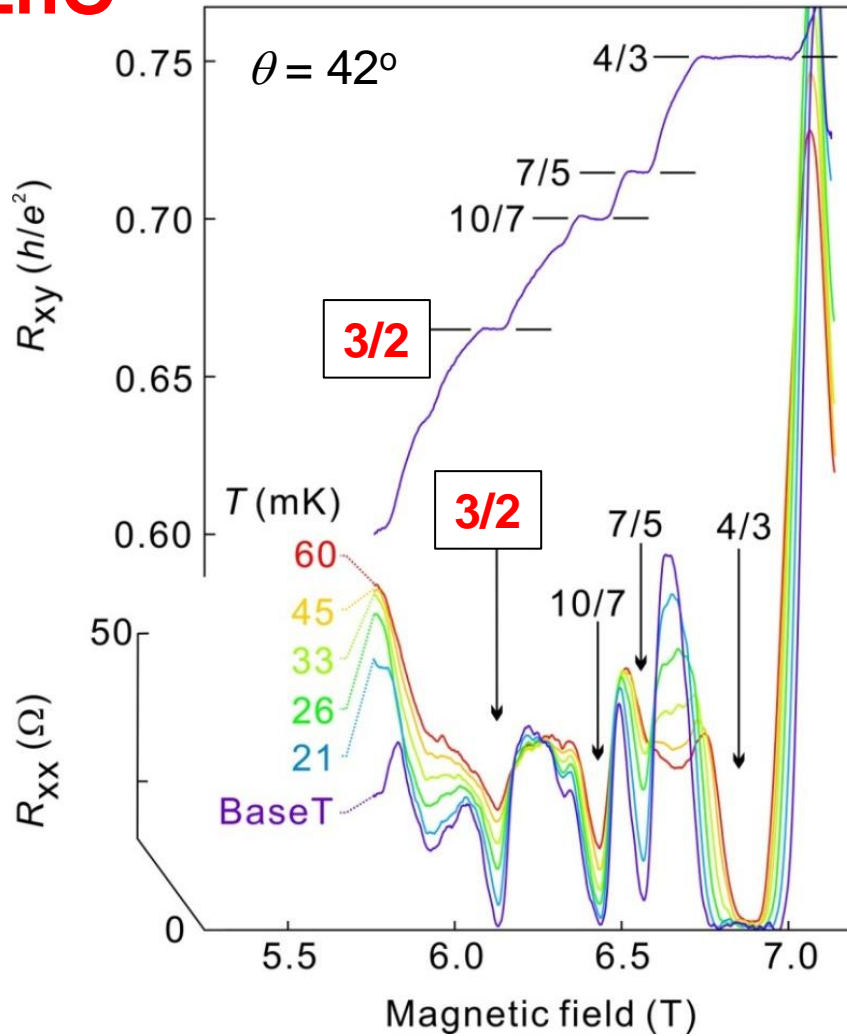
D. Maryenko & YK *et al.*,  
Phys. Rev. Lett. **108**, 186803 (2012)





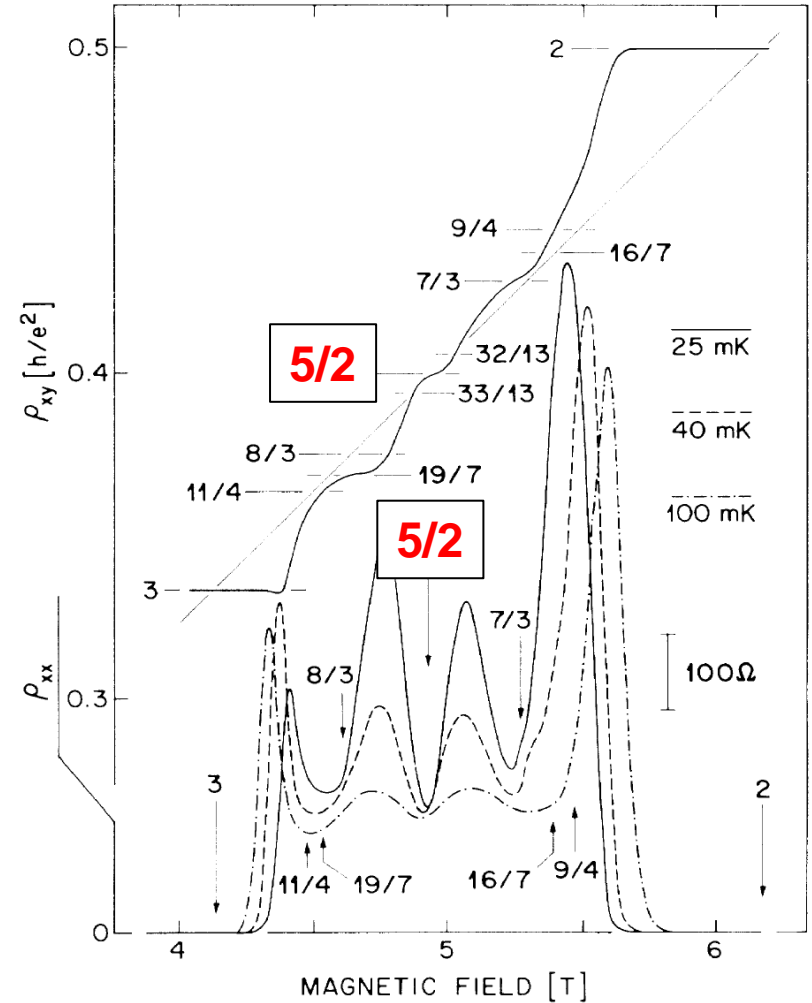
# Even-denominator fractional QHE in ZnO 13

ZnO



**Large electron correlation**  
**Spin degree of freedom**

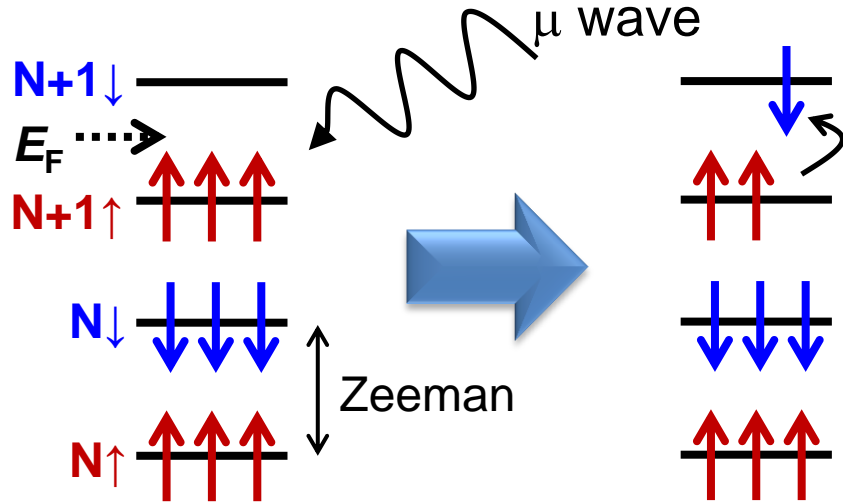
GaAs



R. Willet et al., *Phys. Rev. Lett.* **59**, 1776 (1987)

# Electron spin resonance in integer QHE

Odd-integer state

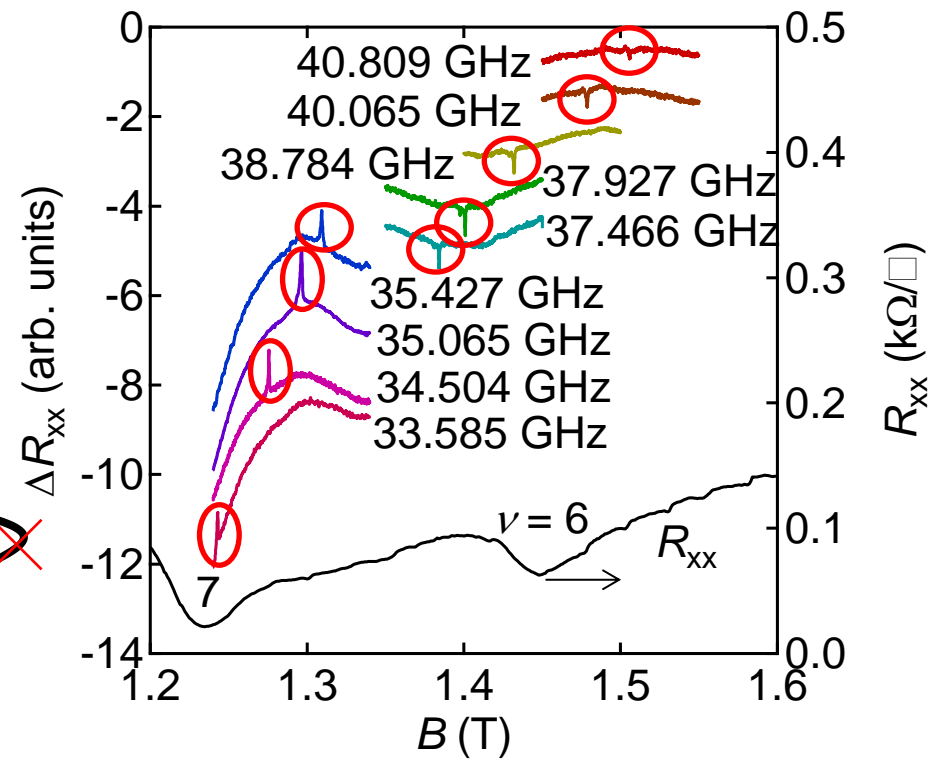
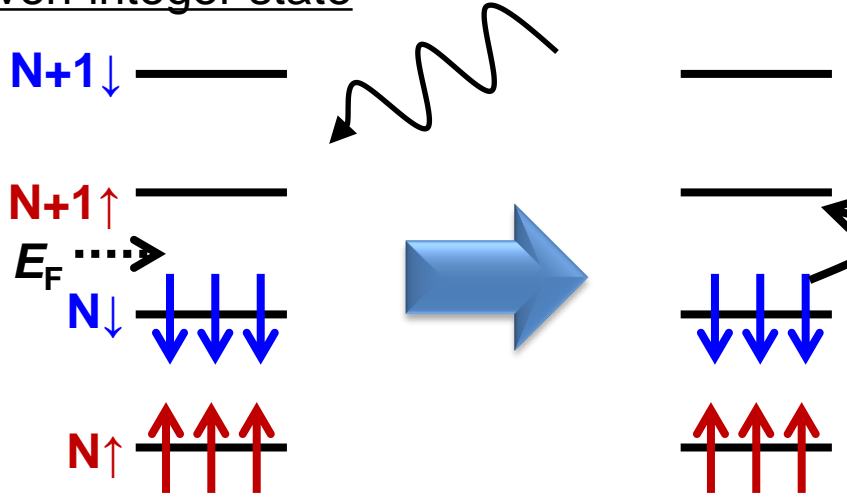


Acknowledgement:  
S. Teraoka, A. Oiwa, S. Tarucha

Y. Kozuka *et al.*, PRB **87**, 205411 (2013)

Under  $\mu$  wave **ZnO 2DEG**

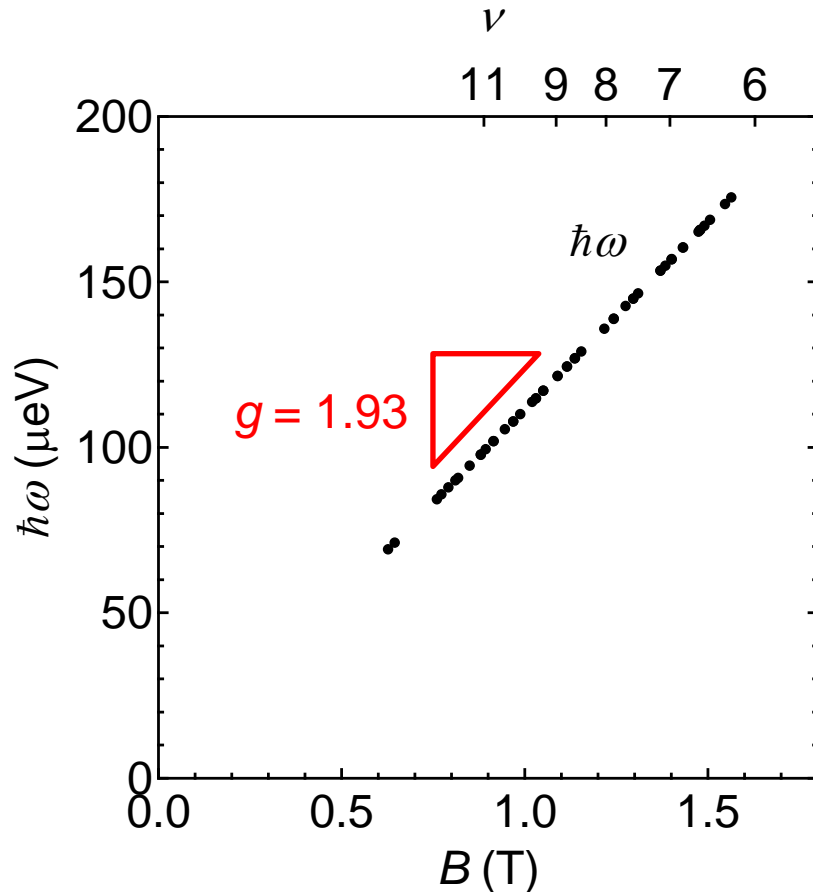
Even-integer state



# ESR in even-integer QHE

## ZnO

ESR appears independent of  $\nu$

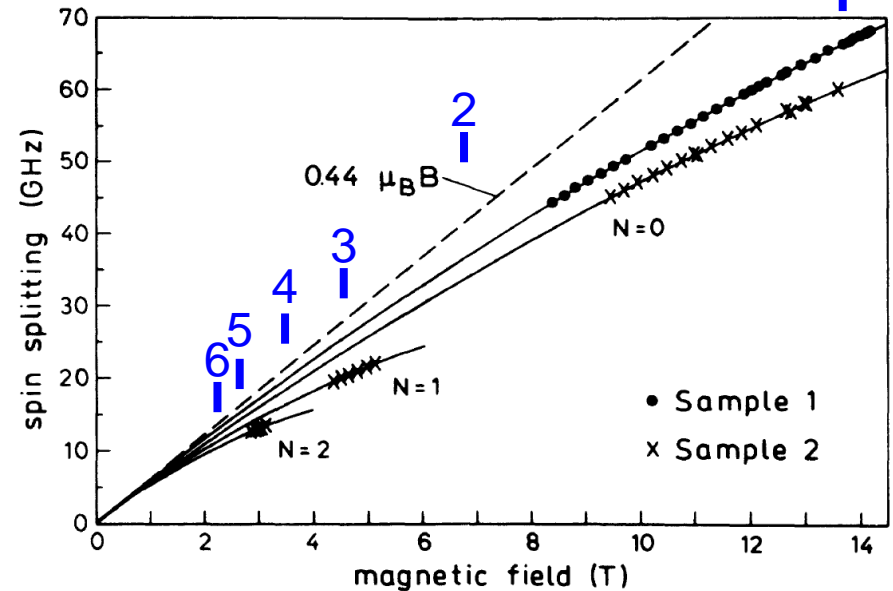


Y. Kozuka *et al.*, PRB **87**, 205411 (2013)

## GaAs

Only near odd  $\nu$

$\nu=1$

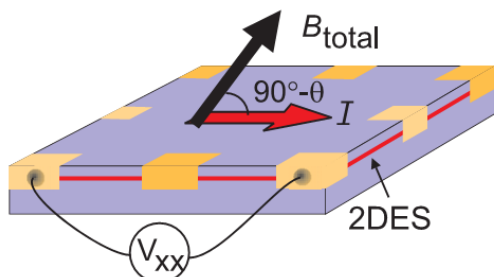


M. Dobers *et al.*, Phys. Rev. B **38**, 5453 (1988)

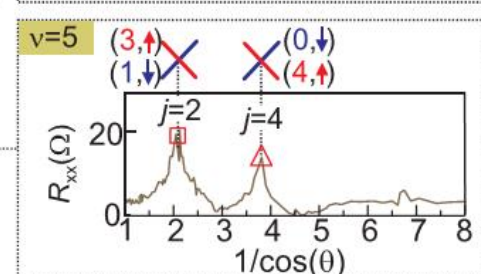
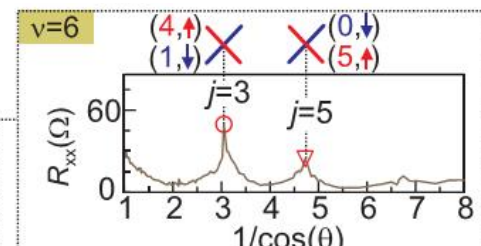
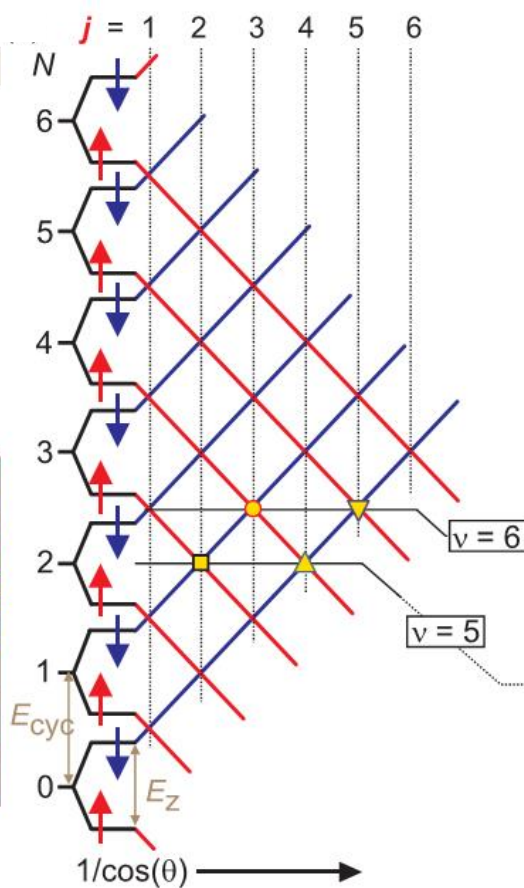
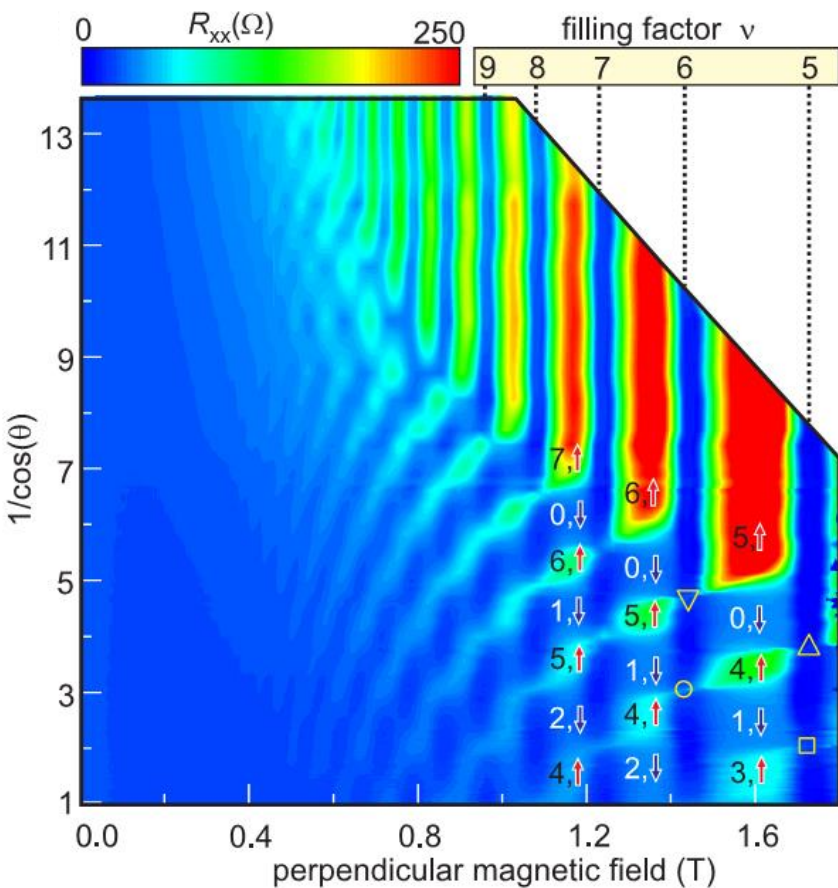


**Partial spin polarization even for even-integer states**

# Detecting spin susceptibility $g^* m^*$



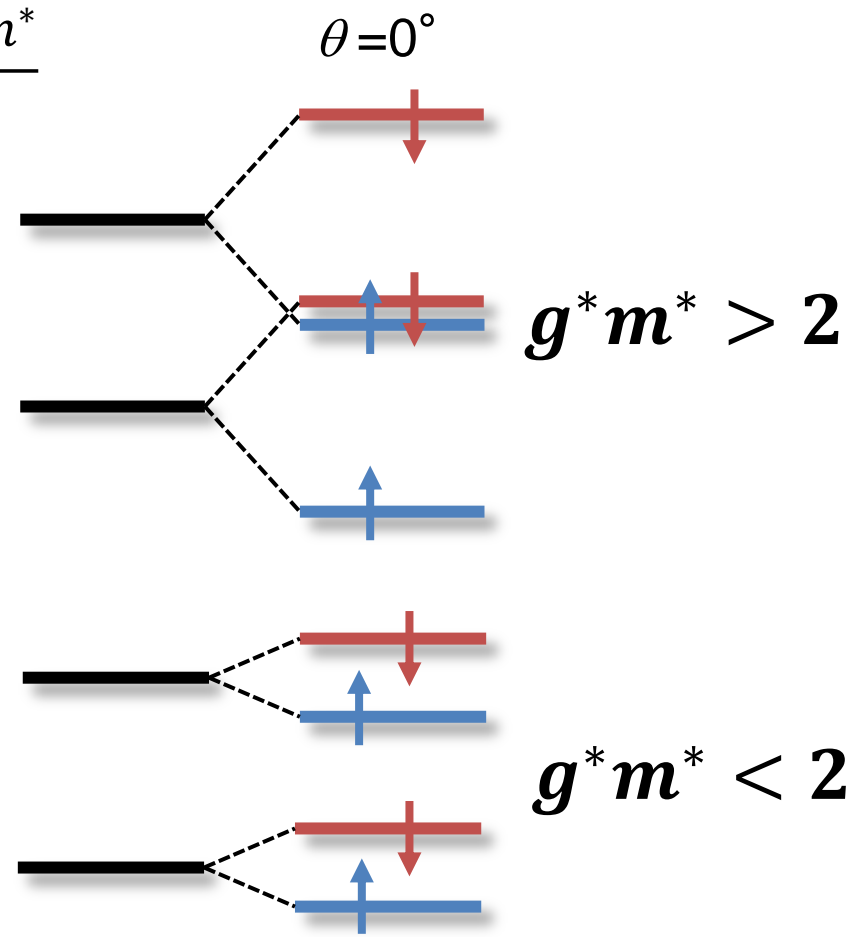
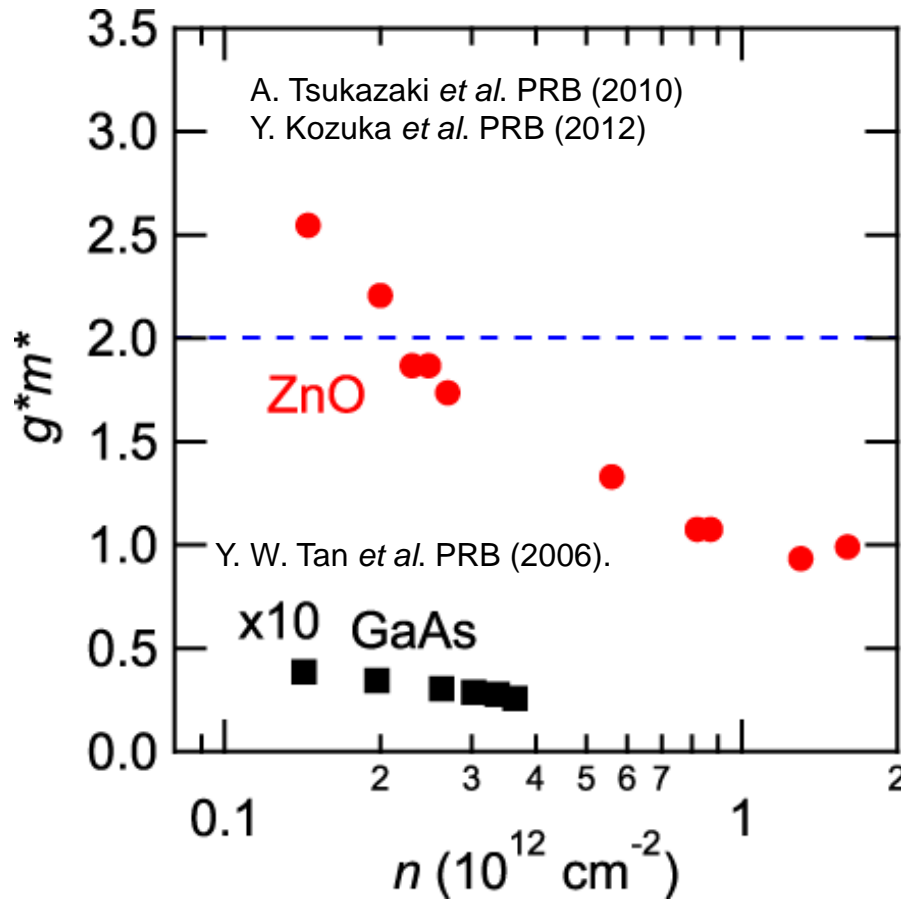
Coincidence:  $\frac{g^* m^*}{2} = j \cos(\theta)$



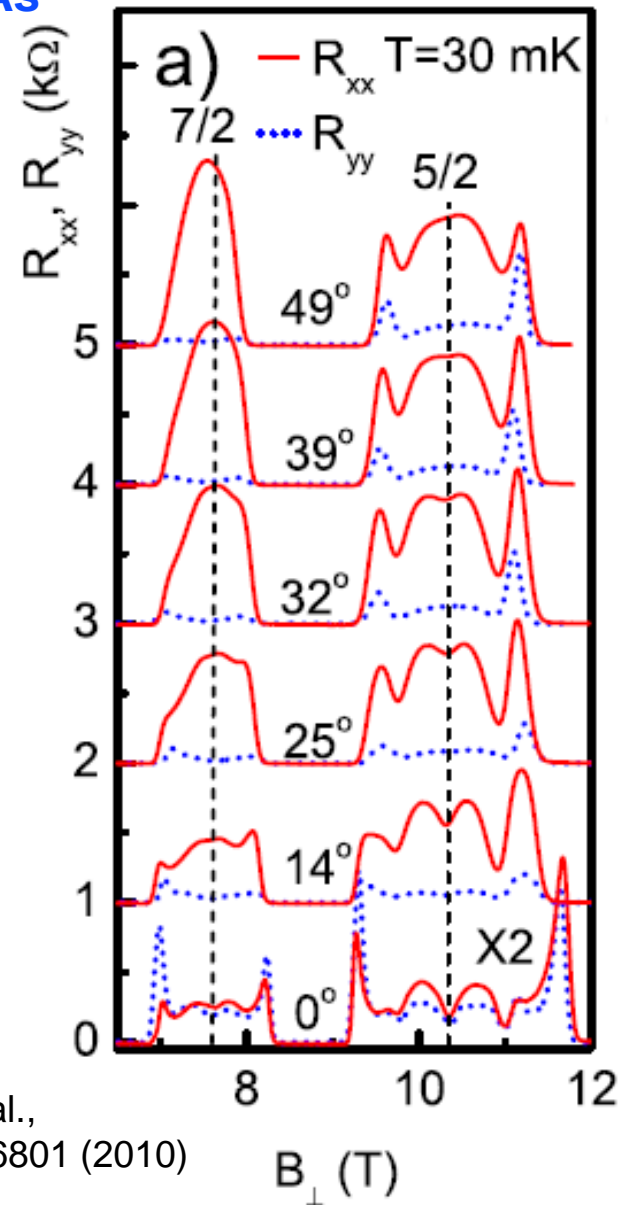
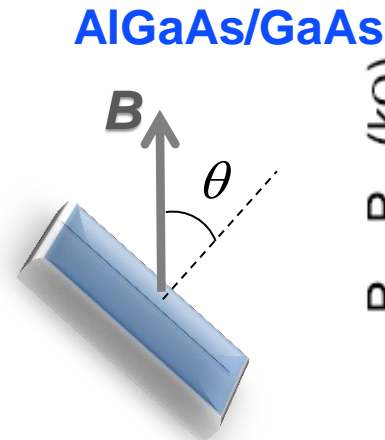
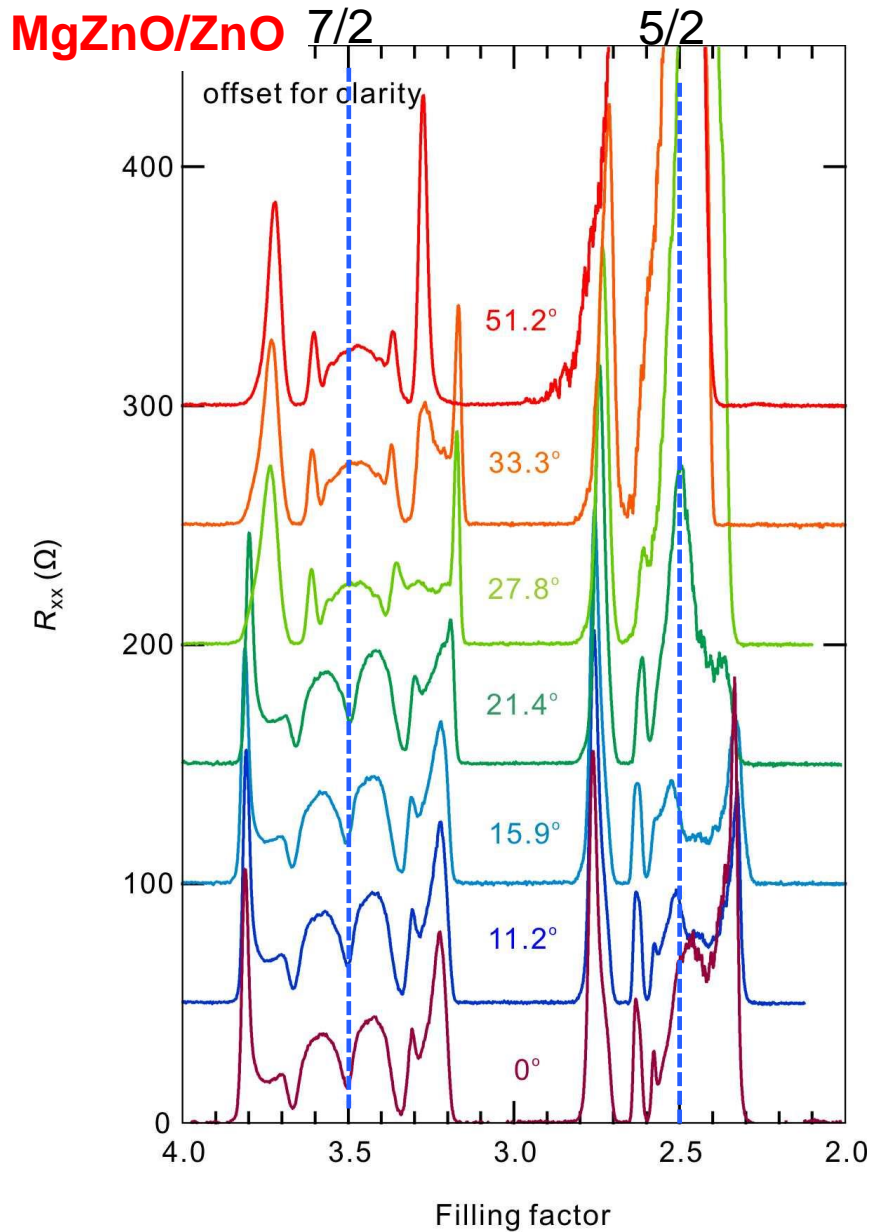


# Spin transition in integer QHE

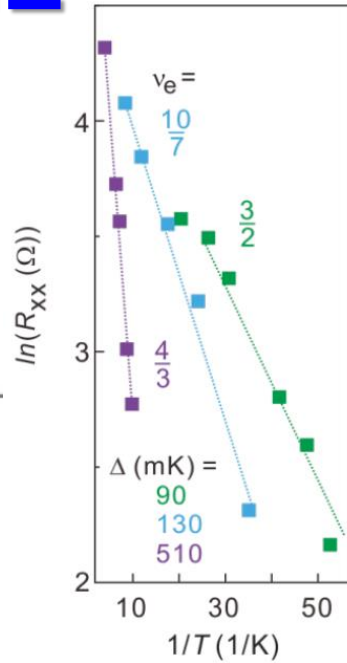
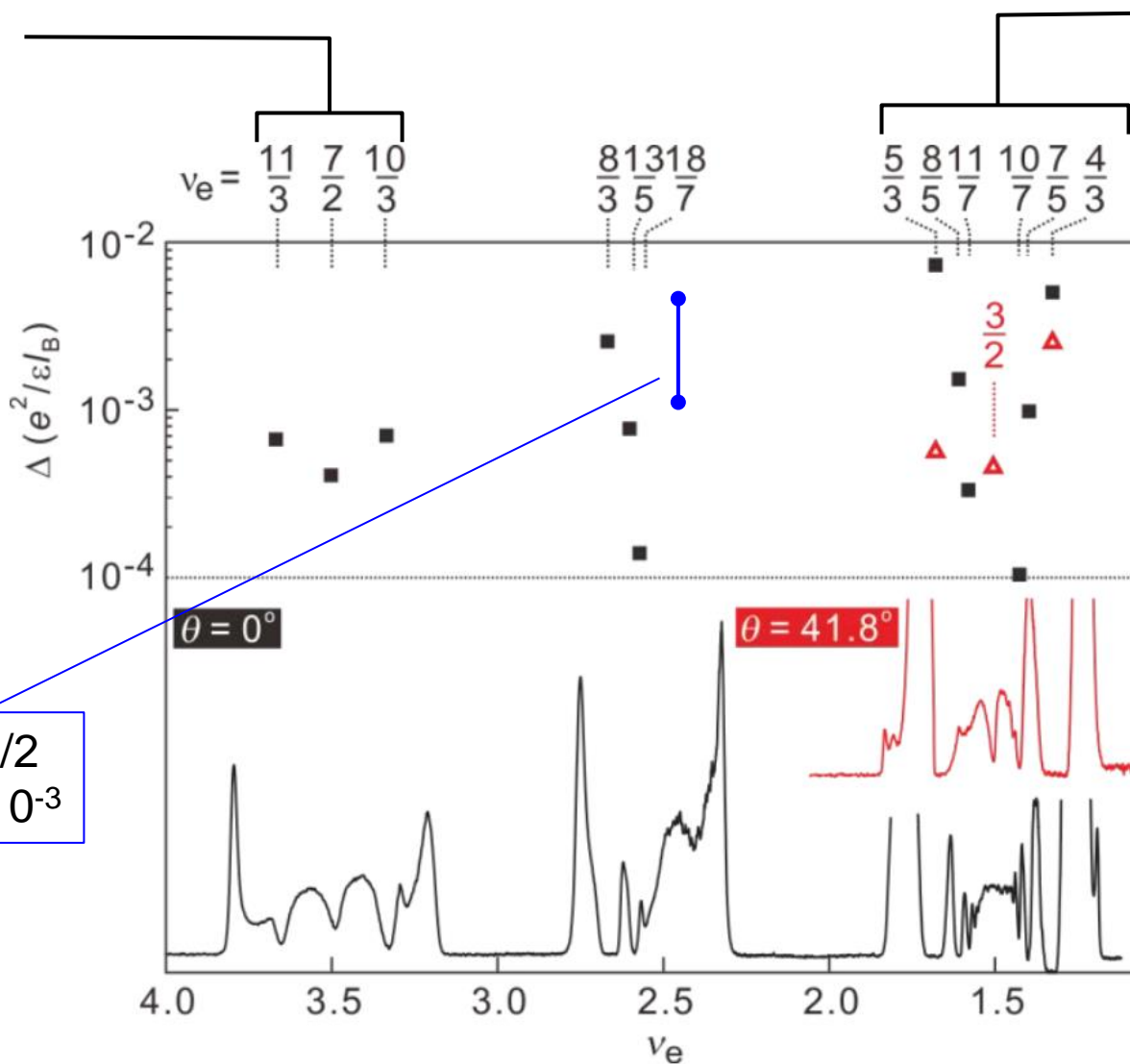
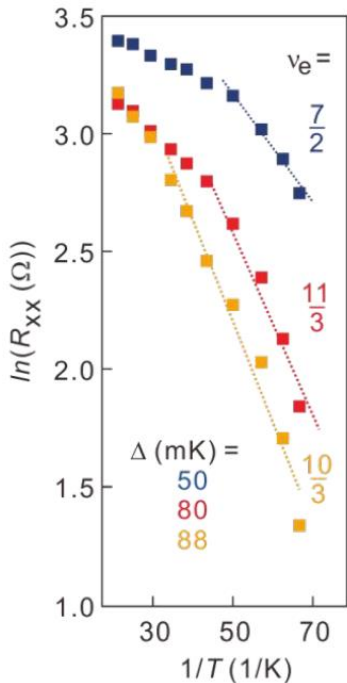
Zeeman/Cyclotron ratio  $\frac{\Delta E_z}{\Delta E_{cyc}} = \frac{g^* m^*}{2}$



# Vanishing $\nu = 7/2$ at high angles



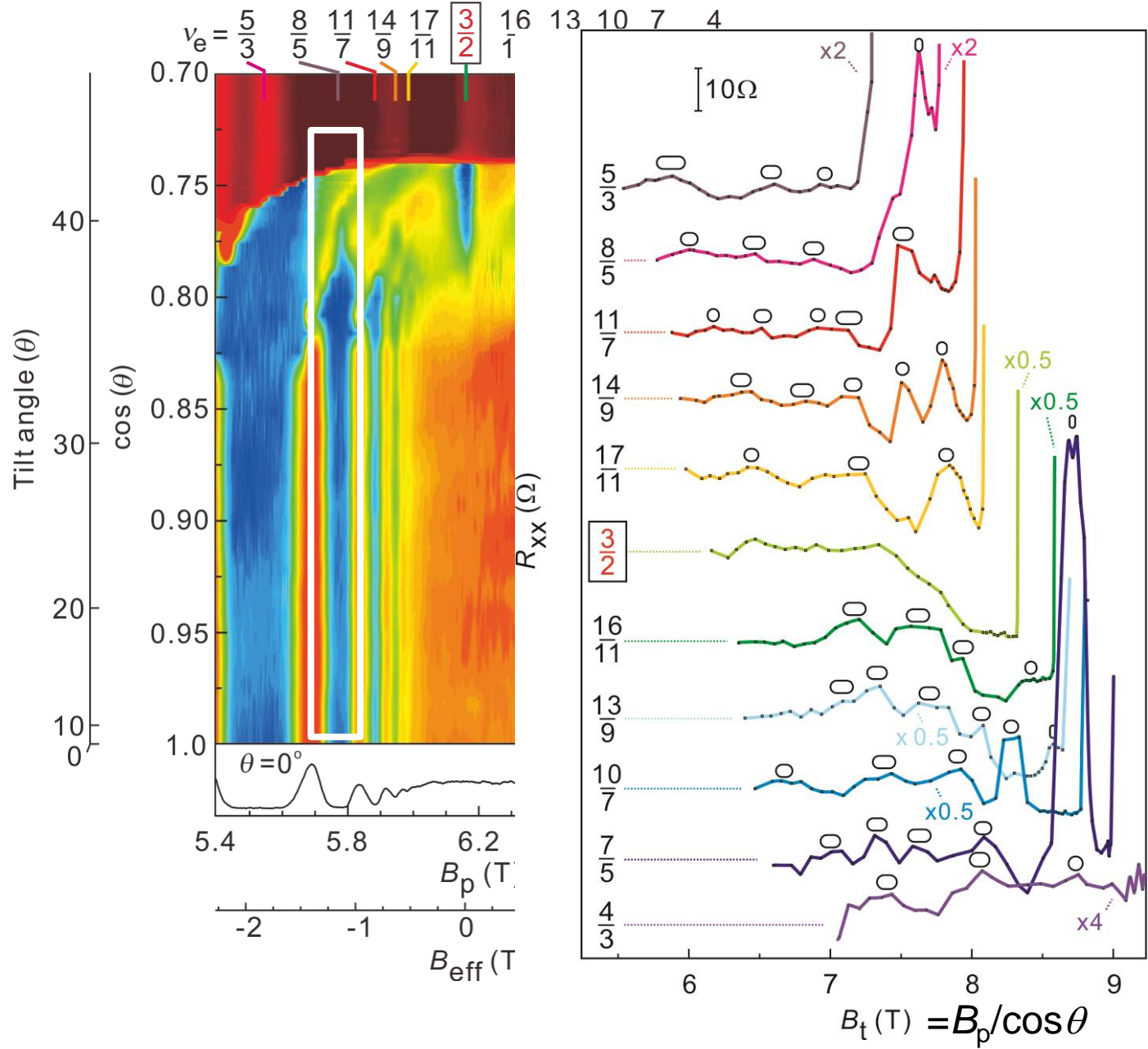
# Activation energies of FQHE



cf. GaAs  $\nu = 5/2$   
 $\Delta_{5/2} = 1 - 5 \times 10^{-3}$

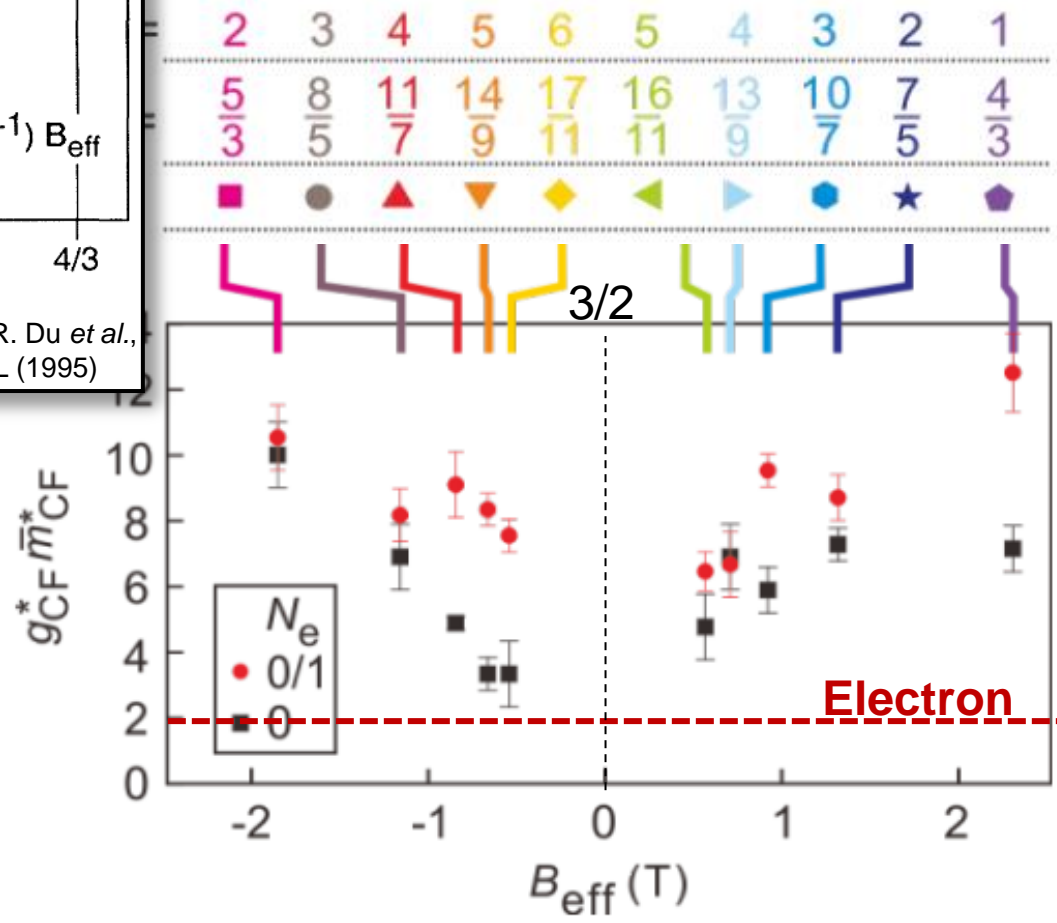
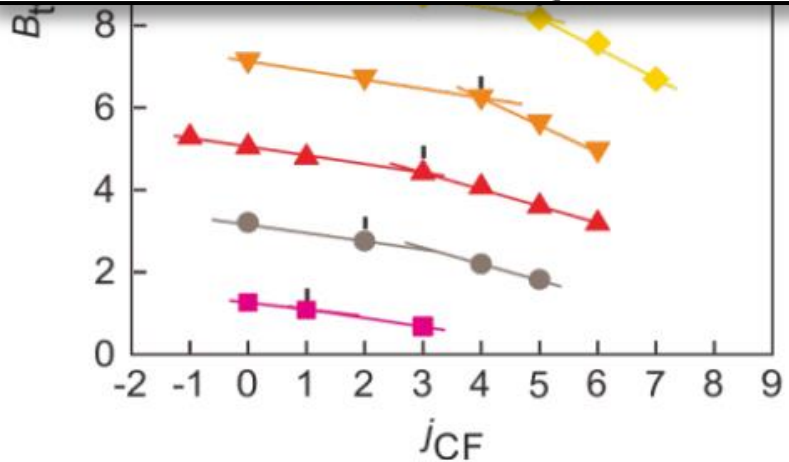
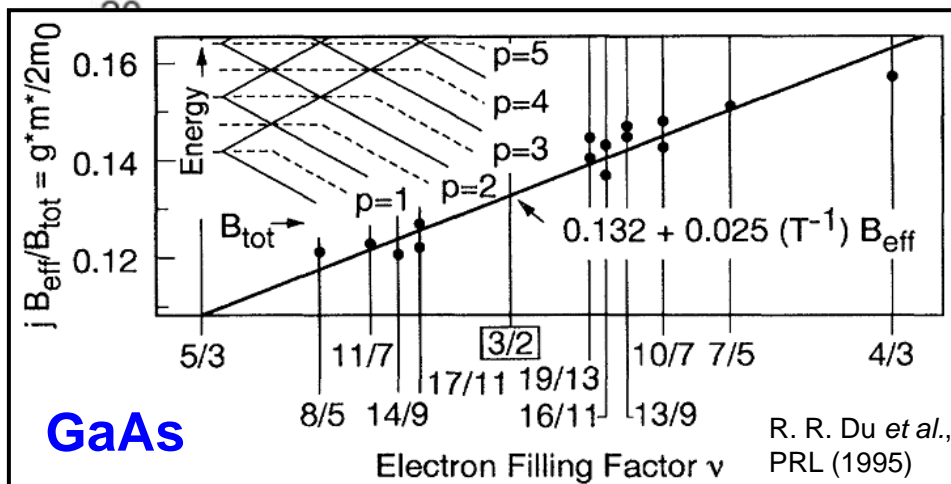
W. Pan et al.,  
 Phys. Rev. Lett.  
**106**, 206806 (2011)

# Spin susceptibility of composite Fermion 22



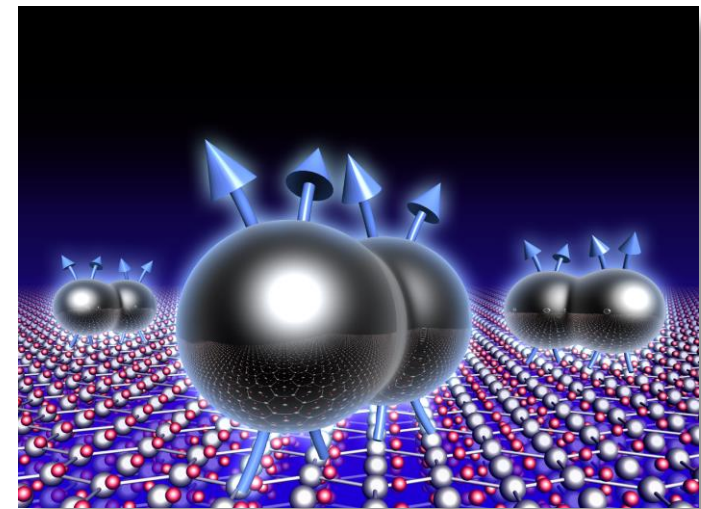
# Spin susceptibility of composite Fermion 23

$$g_{CF}^* \mu_B B_t = j_{CF} \hbar \omega_{CF} \Rightarrow B_t / B_{eff} = j_{CF} \frac{2m_0}{g_{CF}^* m_{CF}^*}$$



# Conclusion

- Electron mobility  $\sim 1,200,000 \text{ cm}^2/\text{Vs}$
- Even denominator fractional quantum Hall state  
 $\nu = 3/2$
- Strong electron correlation
- Large spin polarization
- Landau level mixing



***Qualitatively different composite Fermion properties***