

# On the low-field insulator-quantum Hall conductor transitions

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The low-field insulator-quantum Hall conductor (I-QH) transitions in the integer quantum Hall effect (IQHE) have attracted much attention. According to the global phase diagram (GPD) suggested by Kivelson, Lee and Zhang, [1] in the IQHE the I-QH transitions are between the insulating state and  $\nu=1$  quantum Hall state, where  $\nu$  represents the Landau level filling factor. On the other hand, it is shown that at low magnetic fields a two-dimensional (2D) system can enter quantum Hall states with arbitrary  $\nu$  from the insulating state and hence the low-field I-QH transitions do not always follow the GPD [2,3]. It is argued that the low-field I-QH transitions inconsistent with the GPD are not phase transitions, but are crossovers from weak localization to Landau quantization under finite temperatures and/or sizes [4]. Since weak localization and Landau quantization are important when  $\mu B < 1$  and  $\mu B > 1$ , respectively, a crossover occurs near a magnetic field  $B \sim 1/\mu$ . Here  $\mu$  corresponds to the mobility. Huckestein's argument can explain why the low-field I-QH transitions inconsistent with the GPD usually occur when the ratio  $\rho_{xy}/\rho_{xx} \sim \mu B$  is close to 1, where  $\rho_{xy}$  and  $\rho_{xx}$  are the Hall and longitudinal resistivities. However, D. N. Sheng *et al.* [5] and C. F. Huang *et al.* [6] showed that the low-field I-QH transitions can have properties of phase transitions even when they do not obey the selection rules of GPD.

To further study the low-field I-QH transitions, we performed a magneto-transport study on a 2D GaAs electron system containing self-assembled InAs quantum dots. Figure 1 shows the curve  $\rho_{xy}(B)$  at the temperature  $T=0.52$  K and the curves of  $\rho_{xx}(B)$  at  $T=0.52-1.60$  K when the gate voltage  $V_g=-0.07$  V. We can see in Fig. 1 that the sample enters the quantum Hall state of  $\nu=4$  directly from the low-field insulator as  $B=B_c \equiv 0.9$  T, and hence we observed a low-field I-QH transition inconsistent with the GPD. When  $B < B_c$ , the sample behaves as an insulator since  $\rho_{xx}$  increases as  $T$  decreases. On the other hand, as shown in Fig. 1, Shubnikov-de Haas (SdH) oscillations can be identified when  $B > B_s \sim 0.45$  T. The inset of Fig. 1 shows the curves between the magnetic fields  $B_s$  and  $B_c$ .

Since the insulating behavior and SdH oscillations are features of low-field localization and Landau quantization, respectively, the region between  $B_s$  and  $B_c$  corresponds to the crossover

in the Huckestein's argument. The crossover contains the point  $B_a$  at which  $\rho_{xy}/\rho_{xx}\sim 1$  when  $T=0.52\text{K}-1.60\text{K}$ , but  $B_a$  is *not* the critical point of the I-QH transition and the crossover covers 0.45 T in  $B$  rather than only a small region near  $B_a$ . At the critical magnetic field  $B_c$ , actually  $\rho_{xy}/\rho_{xx}$  is about  $1.5>1$ . From our study, therefore, a crossover from the low-field localization to Landau quantization can cover a wide range with respect to the magnetic field rather than only a small range around the critical point of an I-QH transition. With increasing the magnetic field, the crossover can be followed by the low-field I-QH transition inconsistent with the global phase diagram. In such a transition, in fact, at the critical point the relation that  $\rho_{xy}/\rho_{xx}\sim 1$  can fail.

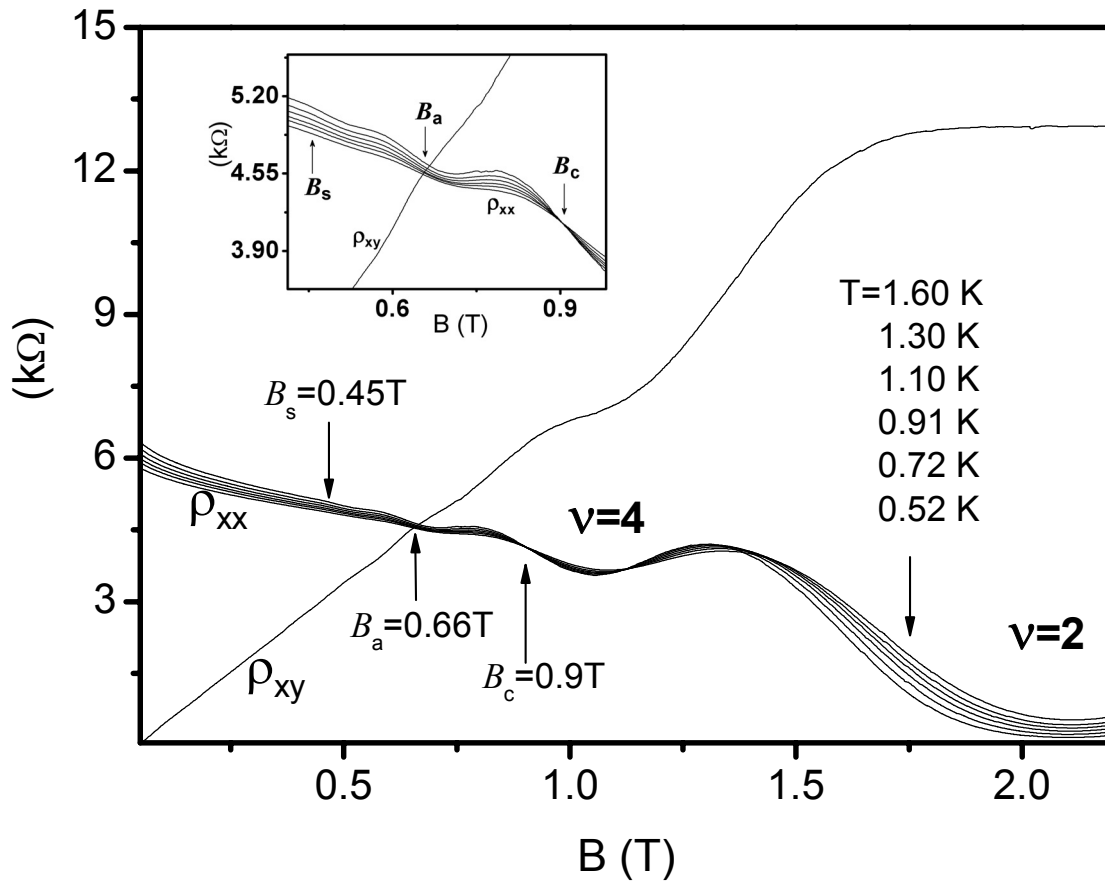


Figure 1 The curves of  $\rho_{xx}(B)$  at  $T = 0.52 - 1.60$  K. The curve  $\rho_{xy}(B)$  at  $T=0.52$  K. The inset shows the curves between the magnetic fields  $B_s$  and  $B_c$ .

#### References:

- [1] S. Kivelson, D.-H. Lee and S.C. Zhang, Phys. Rev. B **46**, 2223 (1992).
- [2] S.-H. Song *et al.*, Phys. Rev. Lett. **78**, 2200 (1997).
- [3] C. H. Lee *et al.*, Phys. Rev. B **58**, 10629 (1998).
- [4] B. Huckestein, Phys. Rev. Lett. **84**, 3141 (2000).
- [5] D. N. Sheng *et al.*, Phys. Rev. B **64**, 165317 (2001).
- [6] C. F. Huang *et al.*, Phys. Rev. B **65**, 045303 (2002).