

Quantum Fluctuations and Criticality in Pr based Spin Ice Systems

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Content

■ Introduction

- Spin Ice on Pyrochlore
- Coulomb Phase and Monopoles
- Quantum version of spin ice

■ Quantum Fluctuation Effects in Pr based Spin Ices

- Quantum monopolar fluctuations in $\text{Pr}_2\text{Zr}_2\text{O}_7$
- Interplay between spin ice and conduction electron,
Chiral Spin Liquid Behavior and Quantum Criticality in $\text{Pr}_2\text{Ir}_2\text{O}_7$

Spin Ice : Pyrochlore Magnet

Nearest-neighbor **FM** coupled **<111>** **Ising** Spins

Classical Spins

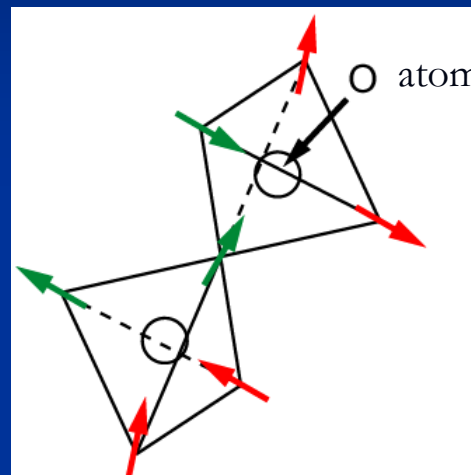
**No Magnetic Order
at $T > 0$**

“Spin Ice”

M.J. Harris, S. Bramwell *et al.*, (1997)

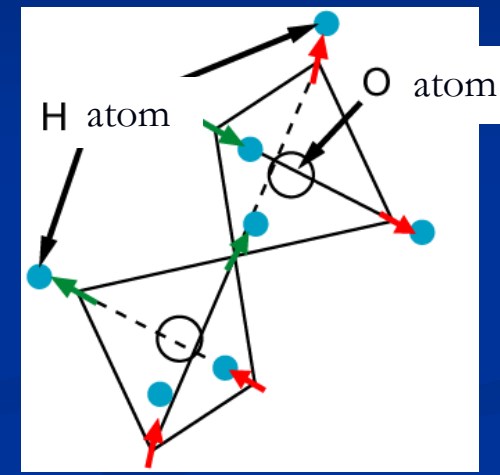
**Disordered State w/
Residual Entropy**
 $S_0 \sim R/2 \ln(3/2)$

A. Ramirez *et al.*, (1997)

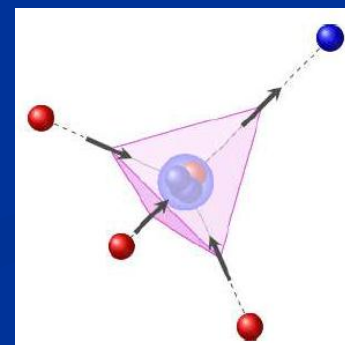


“2-in, 2-out”

$${}_4C_2 = 6 \text{ fold}$$



“H₂O ice”



Low lying Defect
“3-in 1-out” state
Monopole

$$\Delta = 2J_{ff}$$

Castelnovo *et al.* (2008).

Coulomb Phase, Pinch point

Coulomb Phase: quantum dimer system, Heisenberg AF on pyrochlore,...

In Spin Ice, 2-in 2-out can be considered as a divergence free condition:

$$\vec{\nabla} \cdot \vec{M} = 0$$

It leads to power law spin-spin correlation ~

$$\vec{\nabla}_{r'} \cdot \vec{\nabla}_r \frac{1}{r - r'}$$

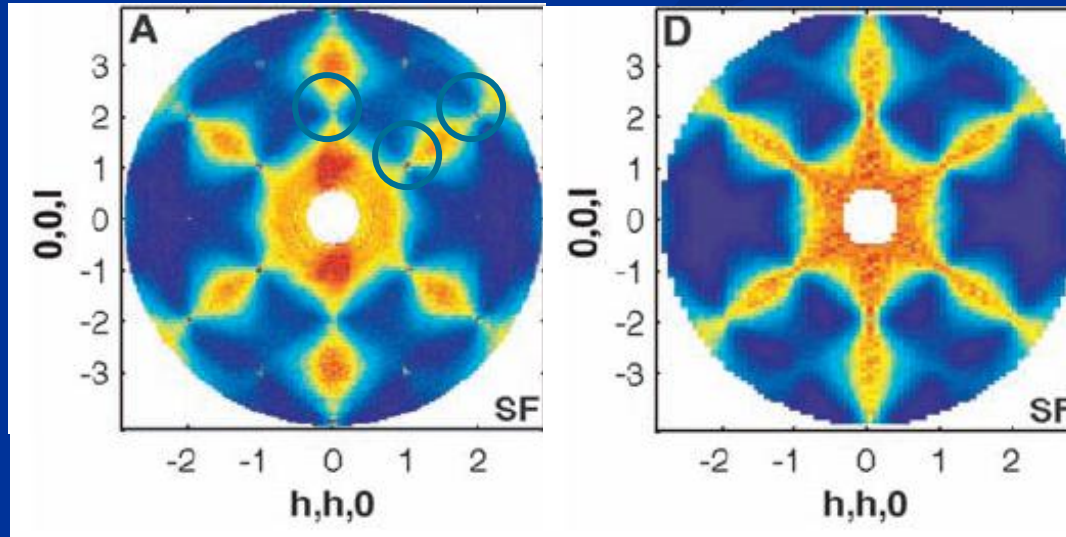
Result in 'pinch point' singularity in scattering experiment.

Ice rule breaking states correspond to creation of magnetic monopole/ width.

Spin Ice $\text{Ho}_2\text{Ti}_2\text{O}_7$, Neutron Scattering Fennell, *et al* (2009)

Experiment

Pinch Points



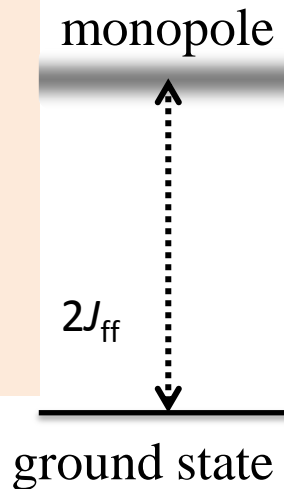
Monte Carlo simulation

“Classical” dipolar spin ice system

[1] ex. Bramwell & Gingras, Science (2001).

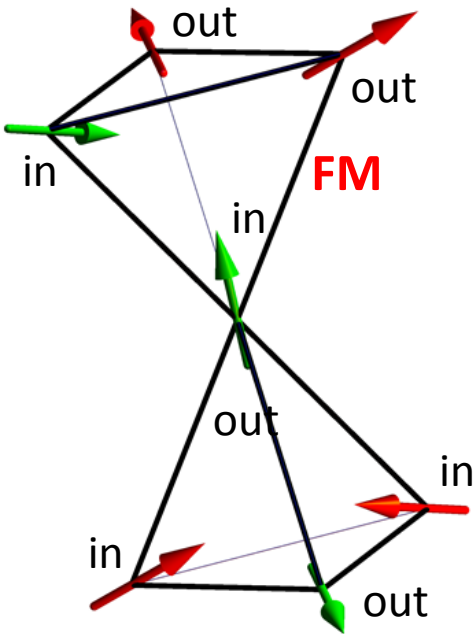
Dipolar spin ice on pyrochlore lattice¹

- Dipolar interaction, Classical \rightarrow FM coupling 1 K
ex. $\text{Dy}_2\text{Ti}_2\text{O}_7$ (Dy: large moment $10\mu_B$)
- No quantum fluctuations in
macroscopically degenerate spin ice manifold
- Monopole dynamics is only diffusive.



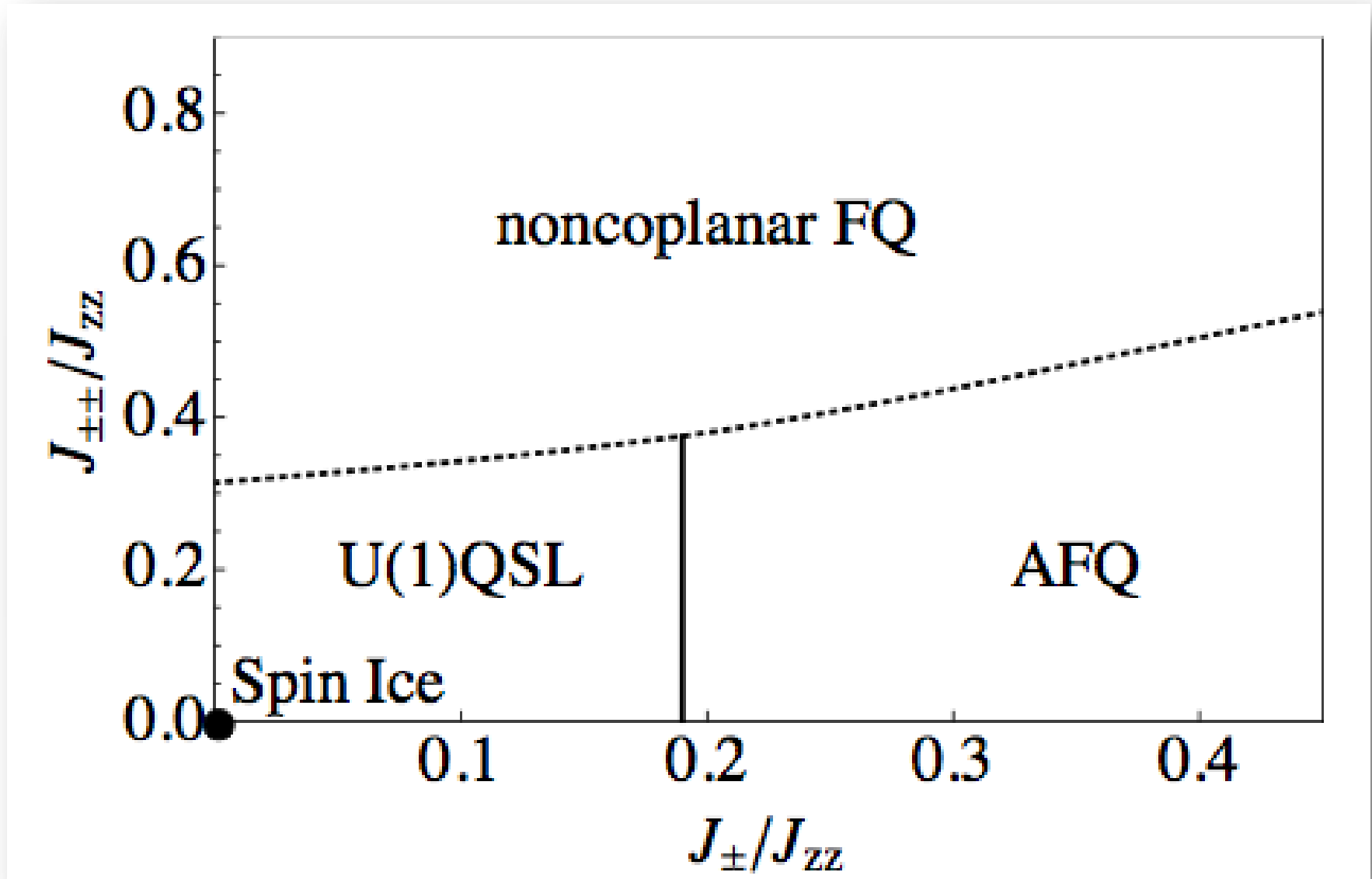
Effects of Quantum fluctuations?

Novel quantum spin liquids and/or Coherent motion of monopoles?



Quantum Spin Ice?

Theory: M. Hermele *et al.*, (2004), R. Moessner *et al.*, (2003), A. Banerjee *et al.*, (2008), S. Onoda *et al.*, (2010).



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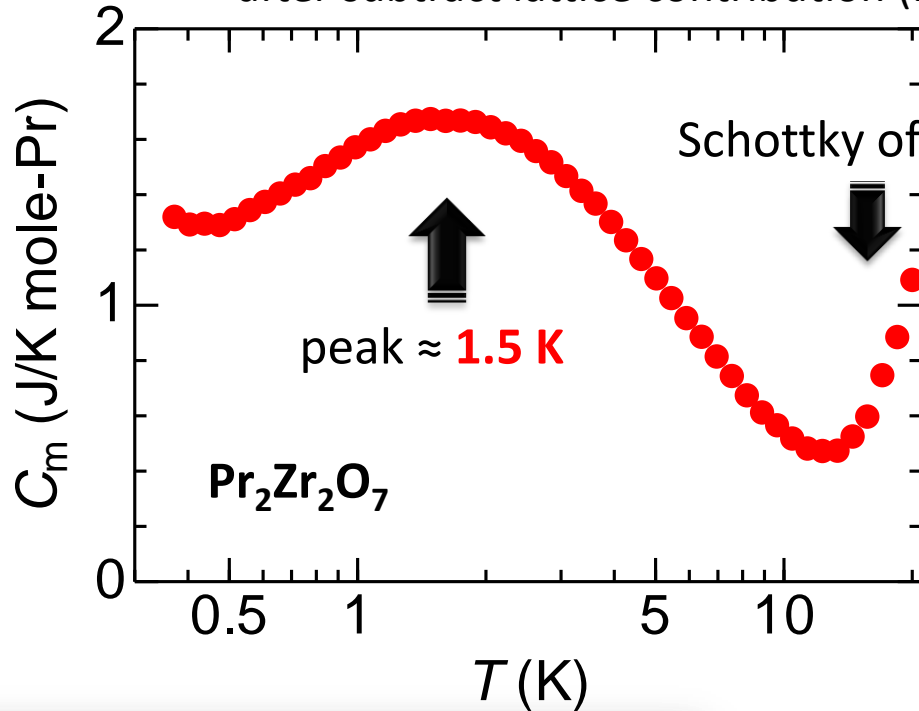
Quantum monopolar fluctuations

Specific heat

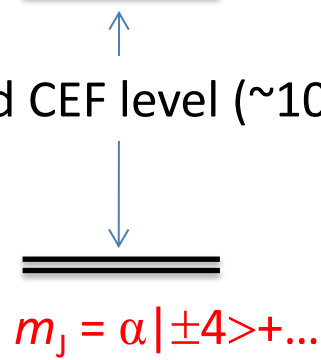
estimate of energy scale $\rightarrow \approx 1$ K

Magnetic specific heat C_m

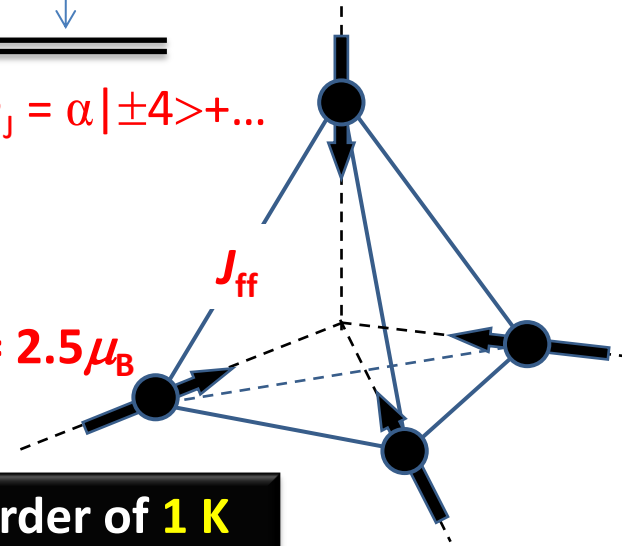
after subtract lattice contribution ($\text{La}_2\text{Zr}_2\text{O}_7$)



Pr^{3+}
 CEF confirmed by Inelastic NS.



$$p_{\text{eff}} = gJ_z = 2.5\mu_B$$

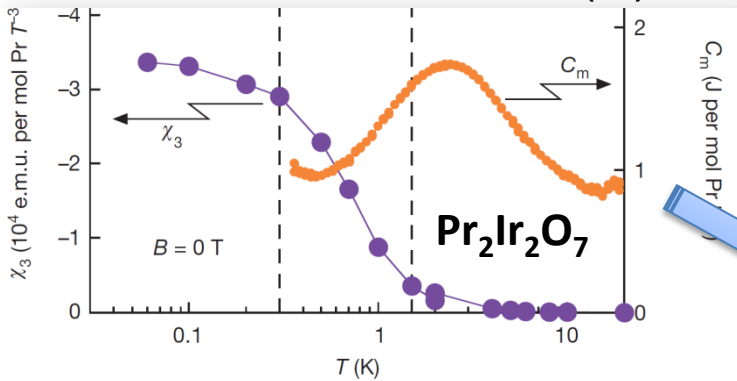


energy scale J_{ff} : order of **1 K**

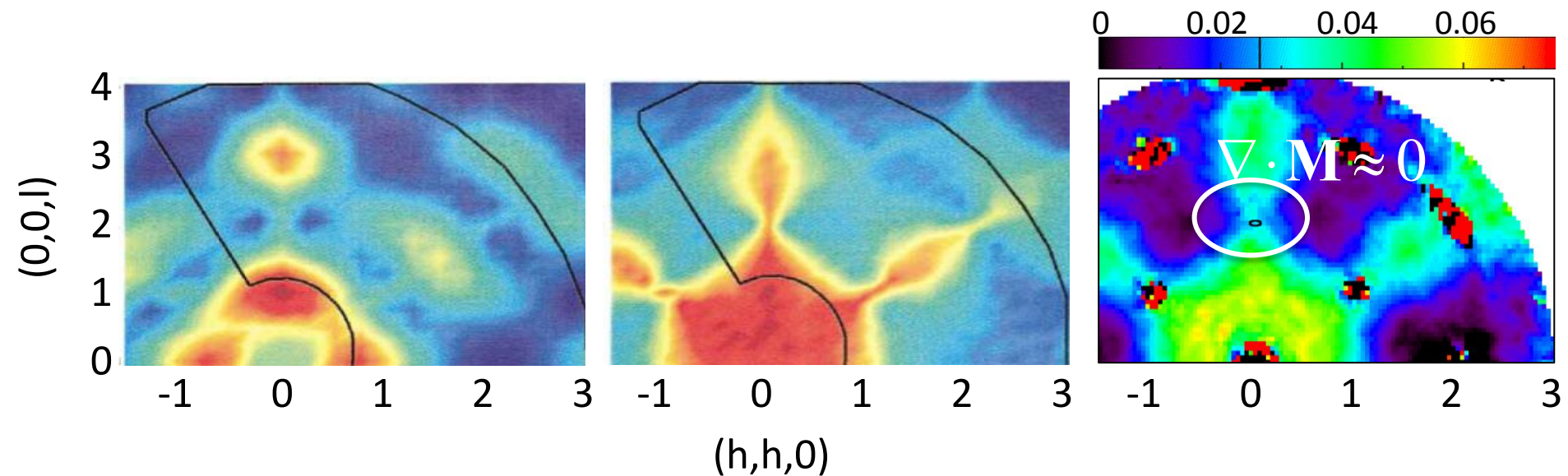
○ exchange coupling × dipolar (0.1 K)

similar to $\text{Pr}_2\text{Ir}_2\text{O}_7$ case

\rightarrow common feature in Pr-based pyrochlore



Elastic neutron scattering for $\text{Pr}_2\text{Zr}_2\text{O}_7$



Dipolar spin ice

NN spin ice

$\text{Pr}_2\text{Zr}_2\text{O}_7$

Monte Carlo Simulation

$T = 0.1 \text{ K}$

S.T. Bramwell et al. PRL (2001).

J. Wen, C. Broholm @ JHU

Measurements were performed at MACS, NCNR, NIST, USA

Background was subtracted using the data taken at $T = 15 \text{ K}$

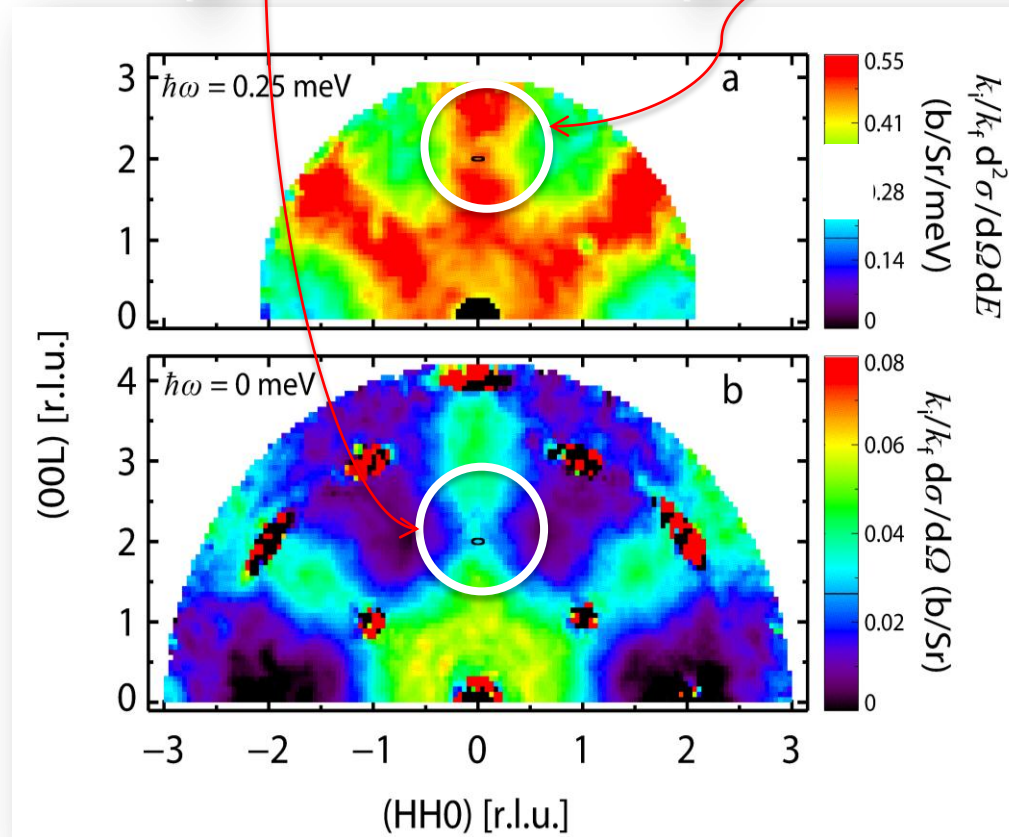
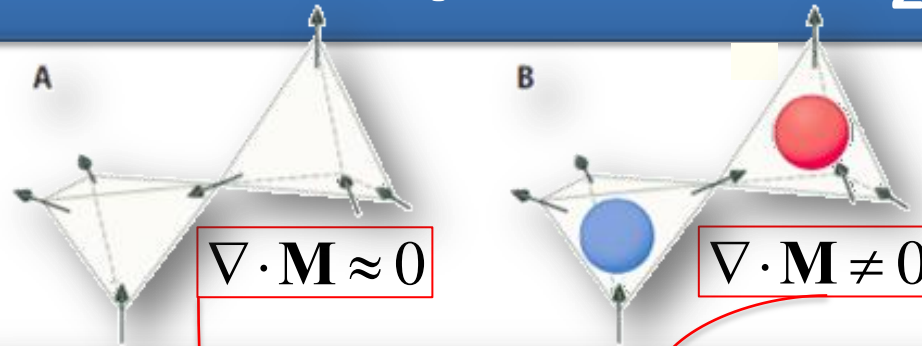
Pinch points at $[200]$, $[111]$,... \Rightarrow Coulomb Phase with NN FM coupling

Only 5 % of the total spectra weight is in the elastic channel: dynamic spin ice manifold

Quantum Monopoles in $\text{Pr}_2\text{Zr}_2\text{O}_7$

J. Wen,
C. Broholm
@ JHU

$T = 0.1 \text{ K}$

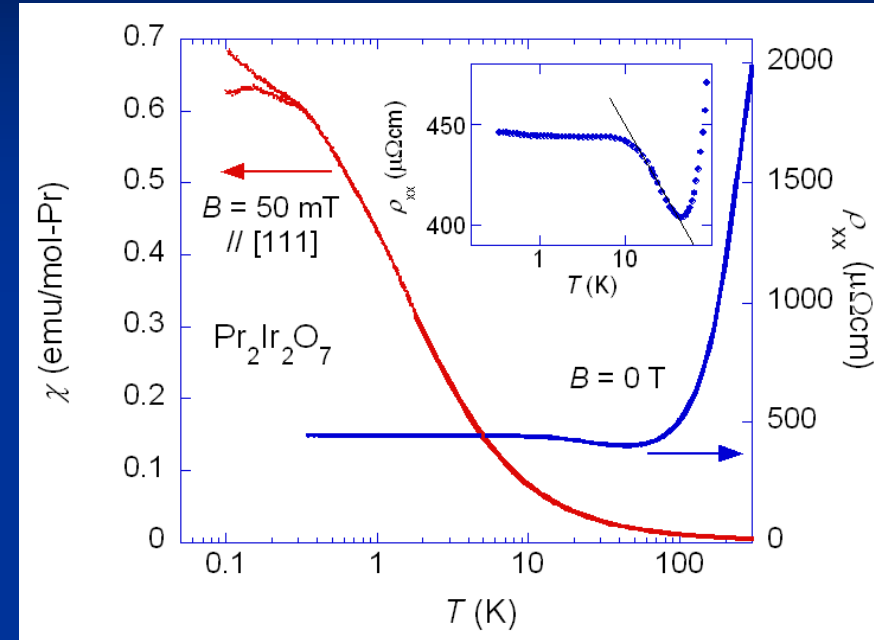
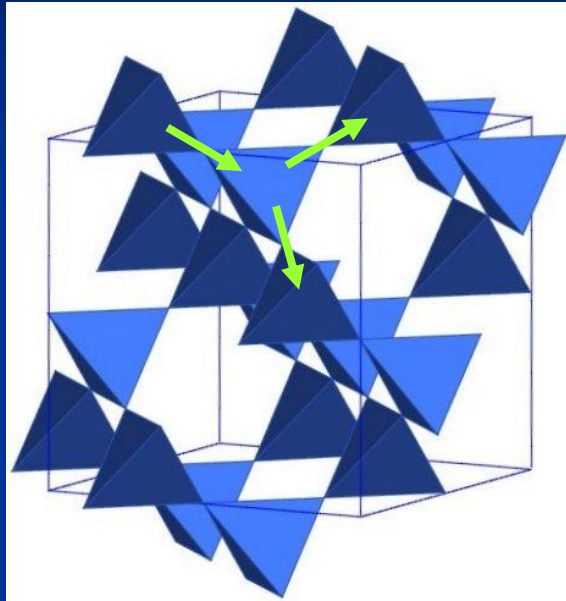


Pinch points are filled in for the inelastic map. \rightarrow Quantum dynamics of monopoles



Spin Ice + Exotic Liquids =?

Pr₂Ir₂O₇ : Geometrically Frustrated Kondo Lattice



Pr³⁺: 4 f^2 Localized **Ising** Moment
 // **<111>** (CEF by Neutron Diffraction)
 Ir⁴⁺: 5 d^5 **conduction electron**,
Pauli Paramagnetism
Spin-Orbit Coupling Effect?

Strong Frustration:

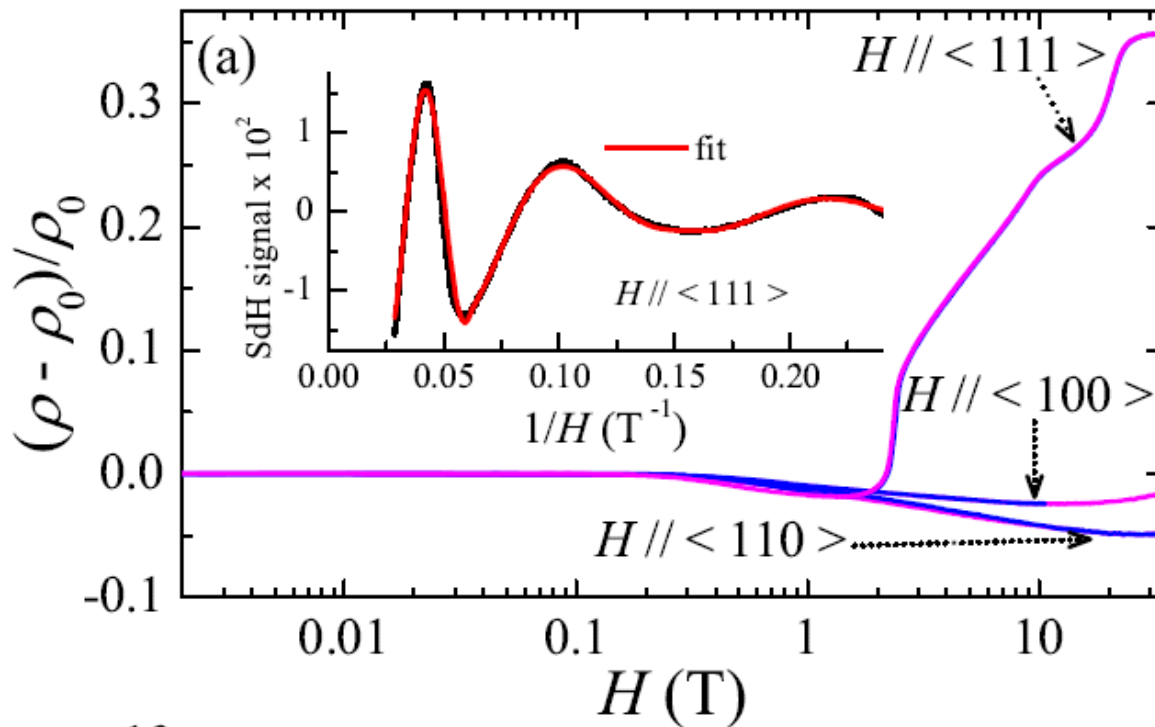
No Long Range Order

$$T_f \sim 0.3 \text{ K} \ll \theta_W \sim -20 \text{ K}$$

No freezing at > 20 mK by μSR

(D. MacLaughlin et al.)

Magnetoresistance



$T = 30$ mK

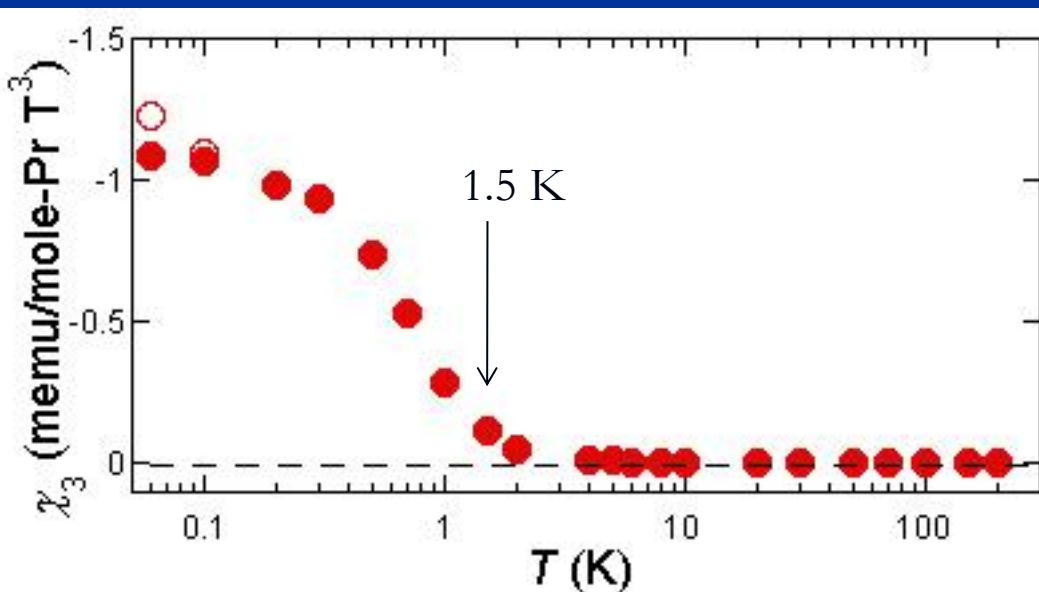
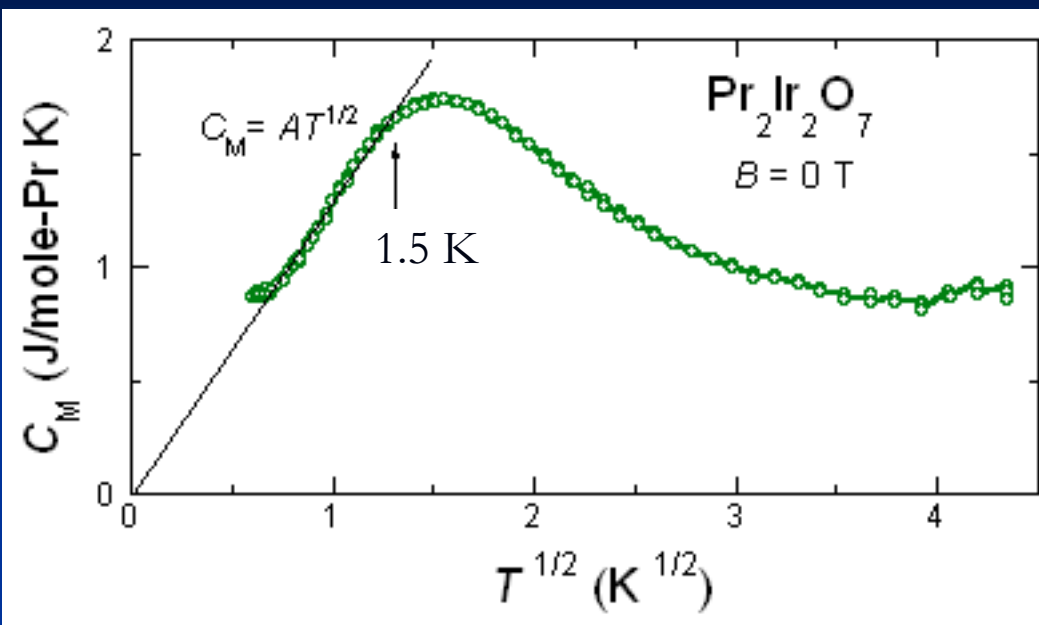
◆ $\langle 100 \rangle, \langle 110 \rangle$:
Smooth decrease

◆ $\langle 111 \rangle$:
Jump in resistance
Metamagnetism

SdH Oscillation seen for [111] fit to Lifshitz-Kosevich formula at $B > B_c$: Loss of scattering due to disordered Spin Ice State

$L \sim 500 - 800 \text{ \AA}$: coherence due to uniform [1-in,3-out] state

FM correlation below $T \sim 2J_{\text{ff}} \sim 1.5$ K



Monopole Creation

$$\Delta = 2J_{\text{ff}}$$

Broad peak at ~ 1.5 K

$$T < 1.5 \text{ K} \quad C_M = AT^{1/2}$$

$$S_M = AT^{1/2}$$

Highly degenerate state

$\chi_3(q=0)$: a steep negative increase, and saturate to a large negative value

➡ FM correlation between Ising moments

↔ ~~Quadrupole Order~~

Pr₂Ir₂O₇ : Geometrically Frustrated Kondo Lattice

$T_f \sim 0.3$ K

$2J_{ff} \sim 1.4$ K

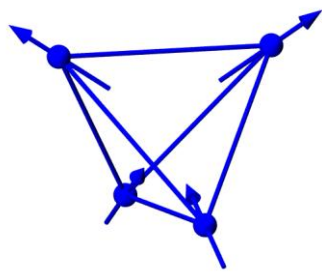
$|\theta_w| \sim 20$ K

T (K)

Partial Spin Freezing

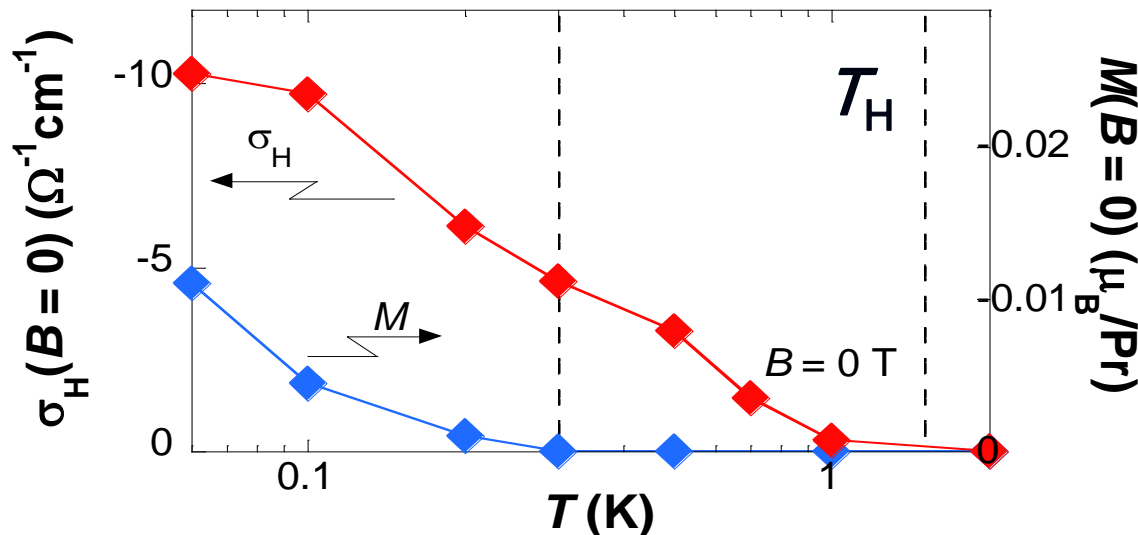
“2-in 2-out” configurations

Kondo like Behavior



Paramagnetic Spin Liquid Phase

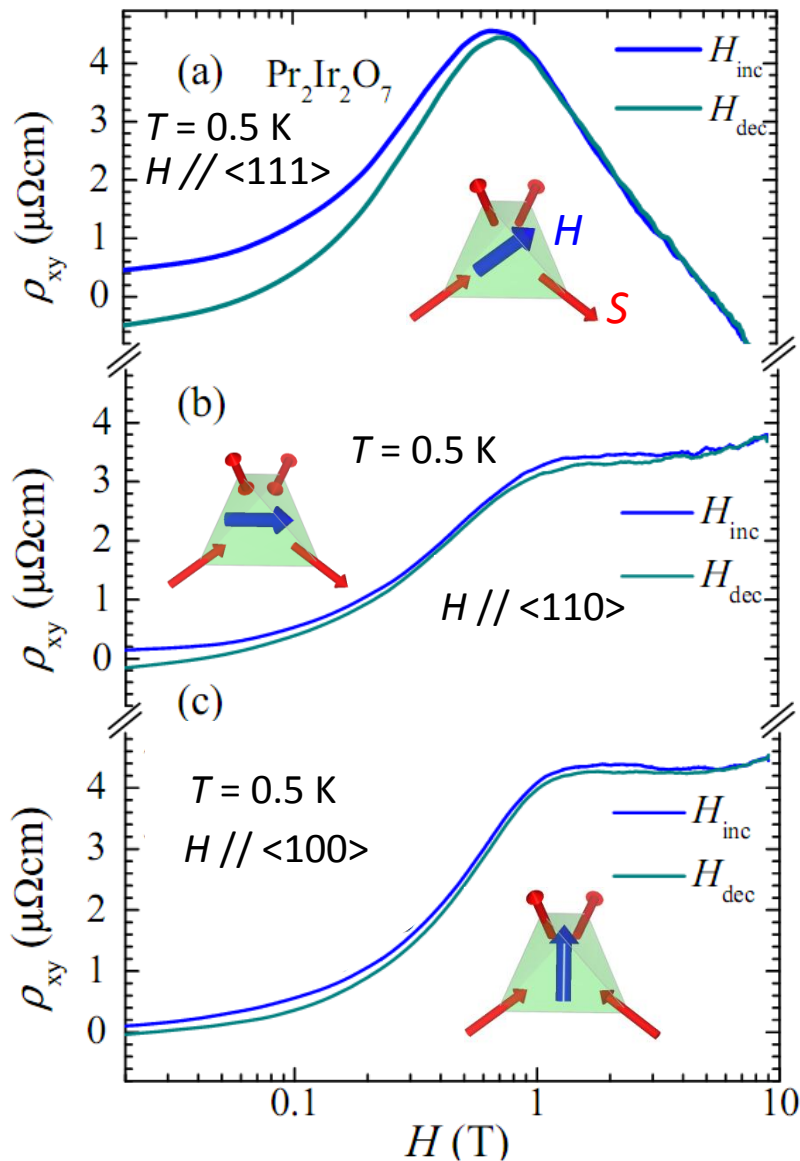
Dipolar Spin Ice (eg. Dy₂Ti₂O₇)
Spin freezing at $T < J_{ff}$



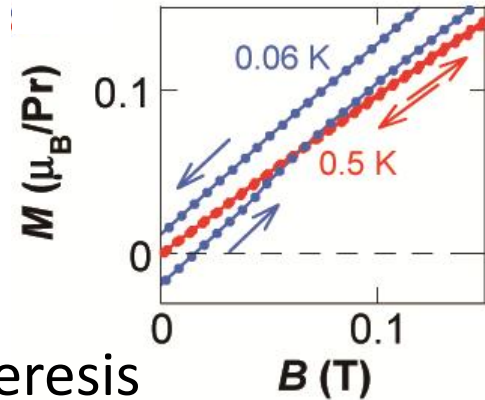
Onset of Spontaneous HE
at $T_H \sim J_{ff}$

TRS broken Spin Liquid
Phase

AHE without Magnetic Order



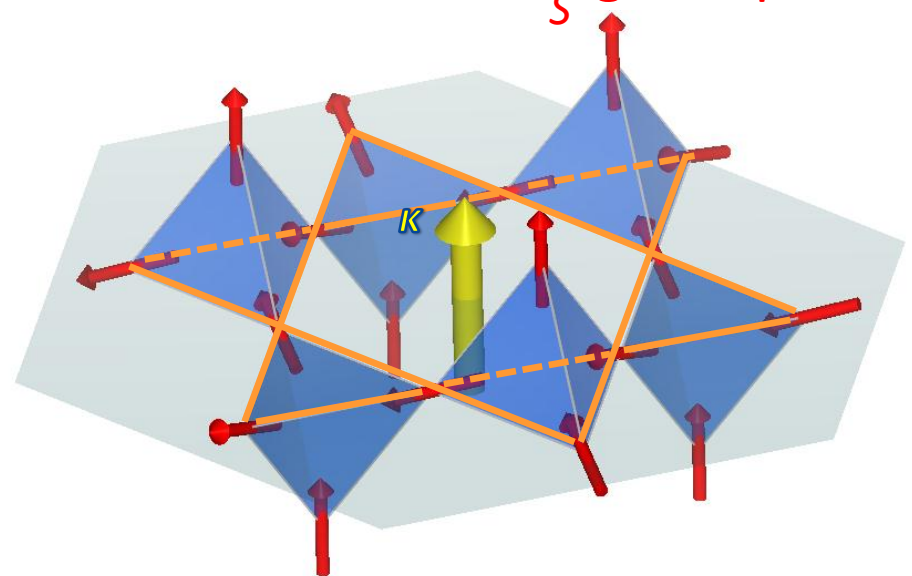
$T = 0.5 \text{ K} > T_f (\sim 0.3 \text{ K})$



$\langle 111 \rangle$: Large hysteresis

$\langle 100 \rangle, \langle 110 \rangle$: Small hysteresis

Orbital currents in the Kagome plane



Summary:

Quantum effects in Pr based Spin Ice

- Spin Liquid with Spin Ice Correlation
 - at $T < 1.5 \text{ K} \sim 2J$: Monopole creation scale
- **$\text{Pr}_2\text{Zr}_2\text{O}_7$**
 - Quantum Monopolar Fluctuations
- **$\text{Pr}_2\text{Ir}_2\text{O}_7$**
 - Chiral Spin Liquid Behavior and Quantum Criticality
 - Role of Spin Orbit Coupling in the Ir Pyrochlore Network?

