

ISSP Workshop
25 July 2006

Magnetism in Nano-Scale Systems

University of Tokyo

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Energy level structure

$$H|\Psi\rangle_i = E_i|\Psi\rangle_i$$

spin operator: (S_x, S_y, S_z) $[S_x, S_y] = iS_z$, etc

$$H = -DS_z^2 - HS_z$$

total spin S $\vec{S} \cdot \vec{S} = S_x^2 + S_y^2 + S_z^2$

$$\begin{cases} \vec{S} \cdot \vec{S} |S, M\rangle = S(S+1) |S, M\rangle \\ S_z |S, M\rangle = M |S, M\rangle, \\ M = -S, -S+1, \dots, S \end{cases}$$

$$H = -DS_z^2 - hS_z$$

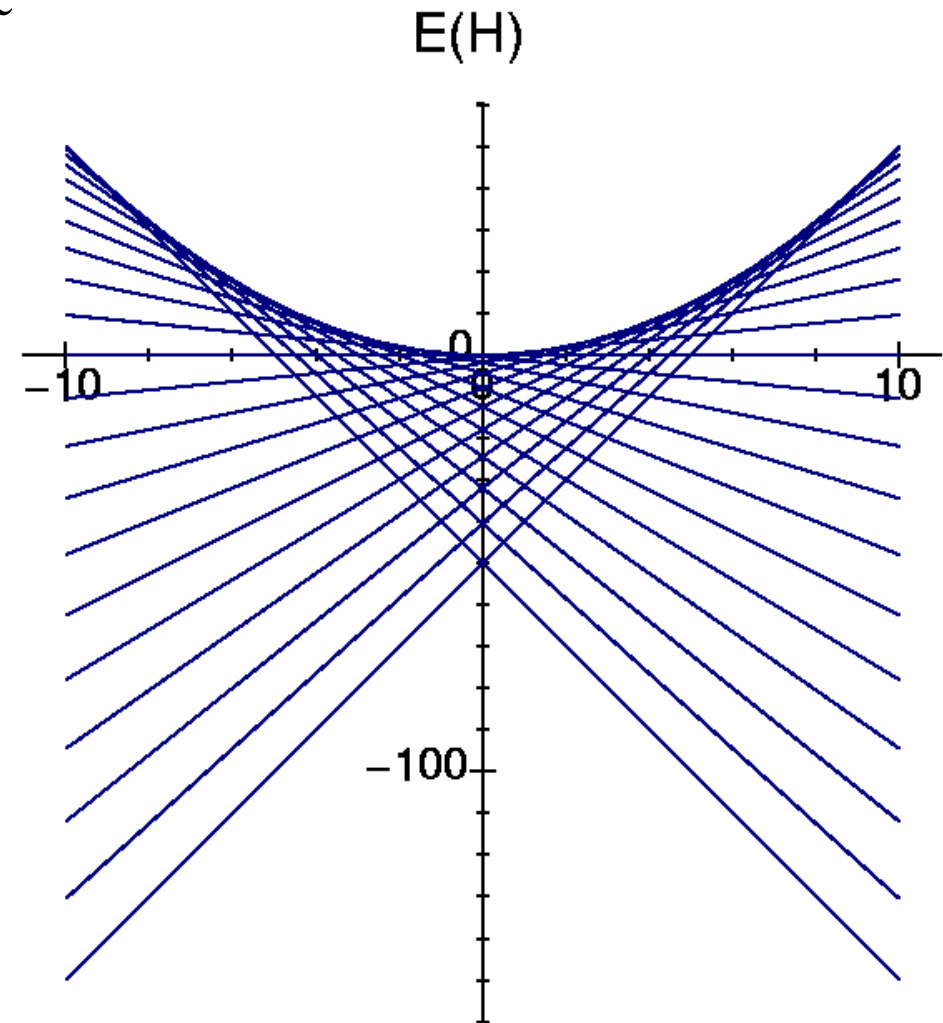
$$H|S, M\rangle_i = -DM^2 - hM |S, M\rangle_i$$

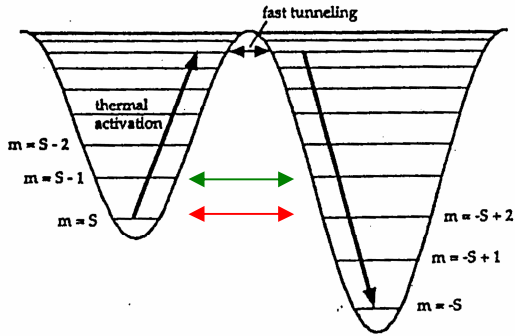
Level crossing

$$h = 0 \quad M = \pm S$$

$$-DM^2 - hM = -D(M+m)^2 - h(M+m)$$

$$h = -D(2M+m)$$





Resonance tunneling

$$H = -DS_z^2 - hS_z$$

$$H|S, M\rangle_i = -DM^2 - hM|S, M\rangle_i$$

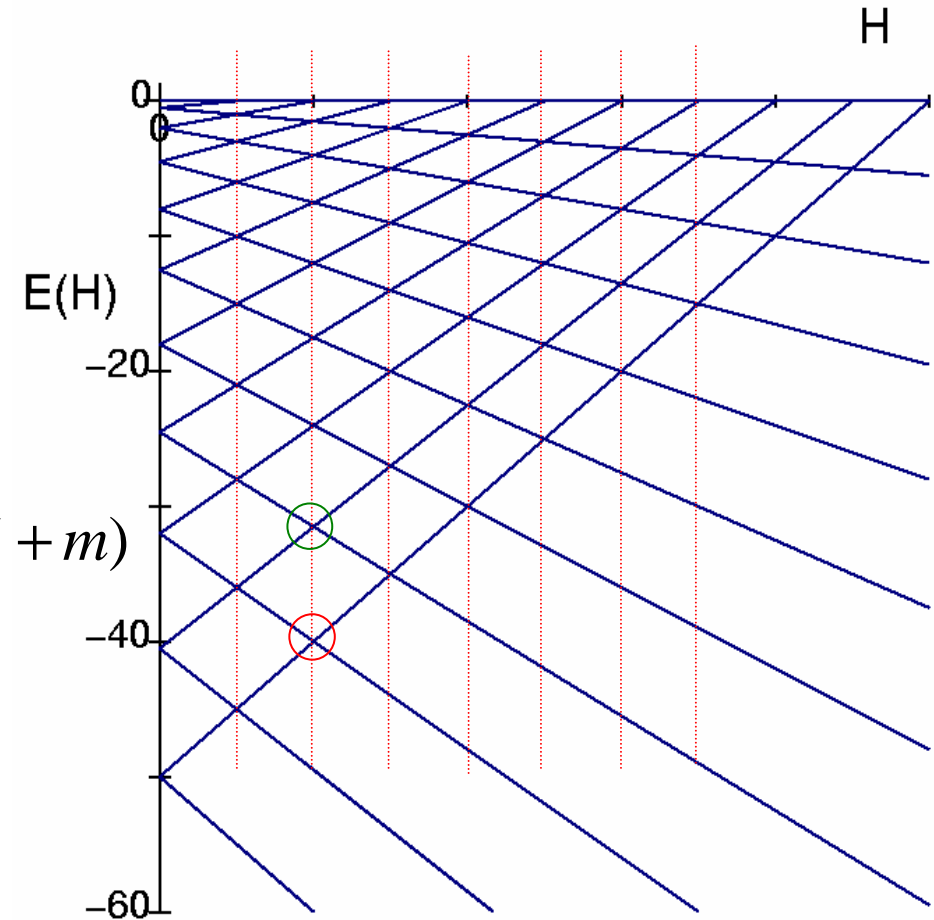
Level crossing

$$h = 0 \quad M = \pm S$$

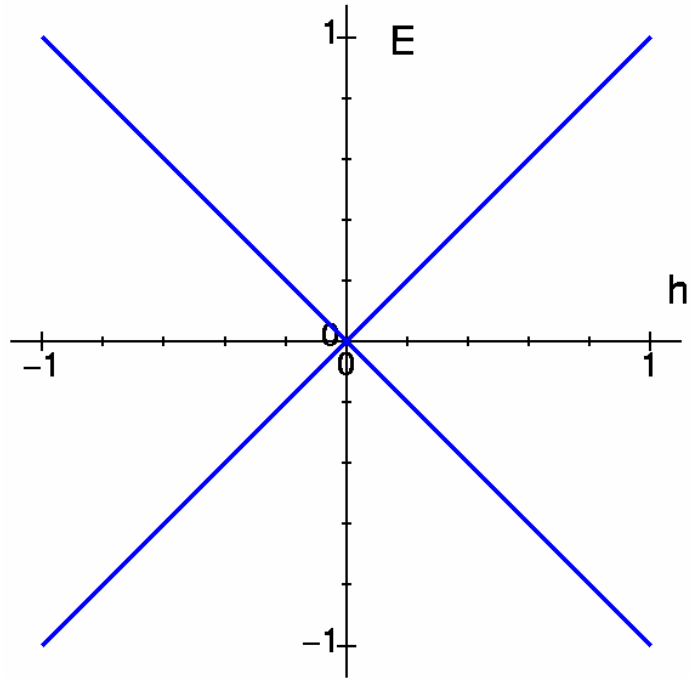
$$-DM^2 - hM = -D(M + m)^2 - h(M + m)$$

$$h = -D(2M + m)$$

Level cross at $h = Dn$



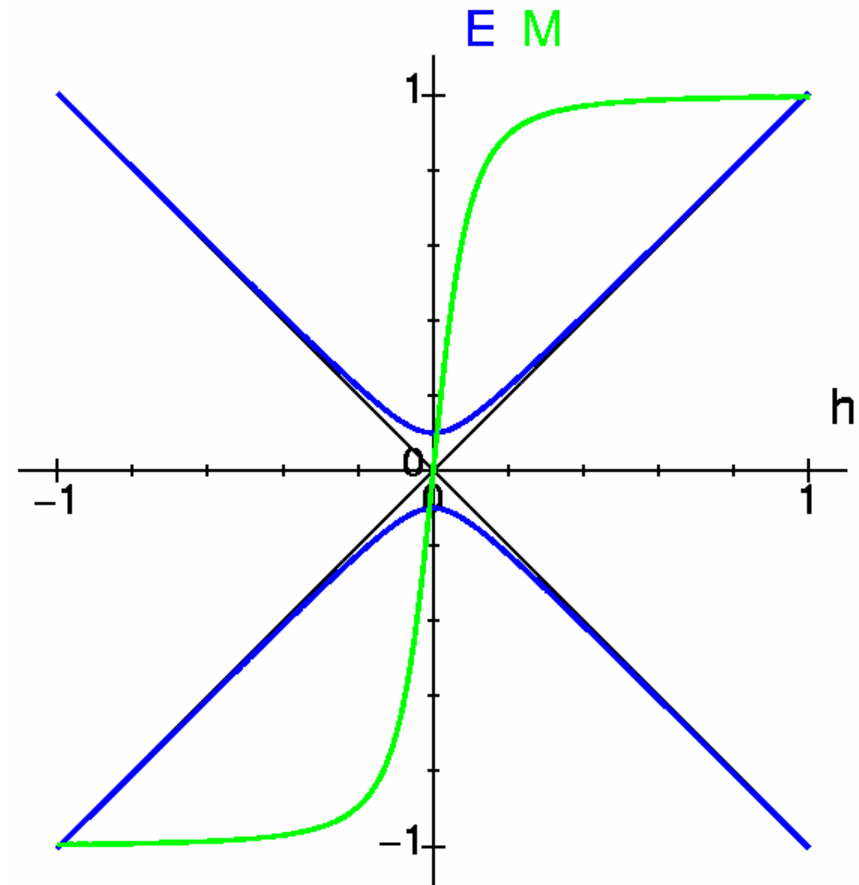
Avoided level crossing



$$[H, S_z] \neq 0$$

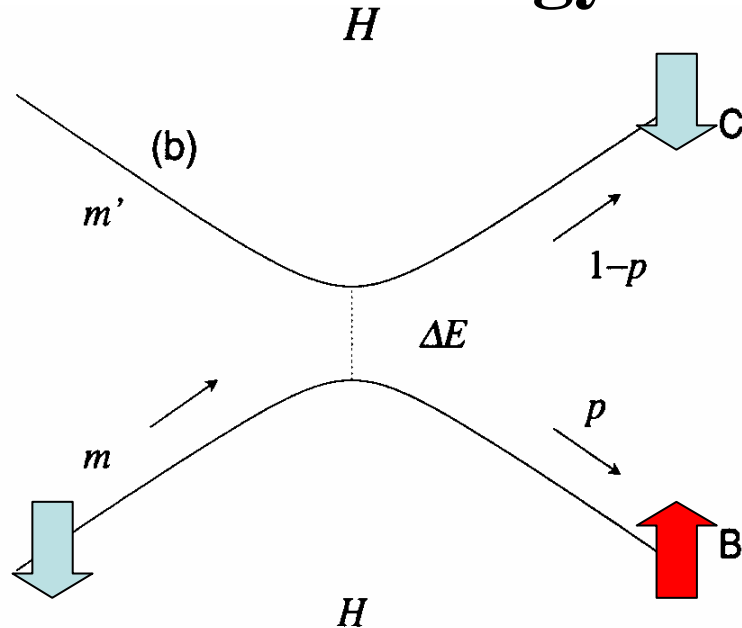
$$H = -hS_z + \Gamma S_x = \frac{1}{2} \begin{pmatrix} -h & \Gamma \\ \Gamma & h \end{pmatrix}$$

$$\begin{pmatrix} -h & \Gamma \\ \Gamma & h \end{pmatrix} \begin{pmatrix} \alpha_{\pm} \\ \beta_{\pm} \end{pmatrix} = \pm \sqrt{h^2 + \Gamma^2} \begin{pmatrix} \alpha_{\pm} \\ \beta_{\pm} \end{pmatrix}$$



Nonadiabatic Transition

Quantum Dynamics in Discrete Energy Levels



Change in Sweeping Field

SM, JPSJ 64(1995) 3207, 65(1996) 2734.
H. De Raedt et al, PRB56 (1997) 2734

$$H = -\infty \quad |\Psi\rangle = |\downarrow\rangle$$

$$H(t) = ct - h_0, \quad h_0 \rightarrow -\infty$$

$$|\Psi(t)\rangle = e_{\rightarrow}^{-i \int H(s) ds / \hbar} |\downarrow\rangle$$

$$\lim_{t \rightarrow \infty} |\Psi(t)\rangle = \alpha |\downarrow\rangle + \beta |\uparrow\rangle$$

adiabatic change $p = |\beta|^2$

non - adiabatic transition $1 - p$

Landau-Zener-Stueckelberg Mechanism

C. Zener, Proc. R. Soc. (London) Ser. A137 (1932) 696.

Resonant Tunneling

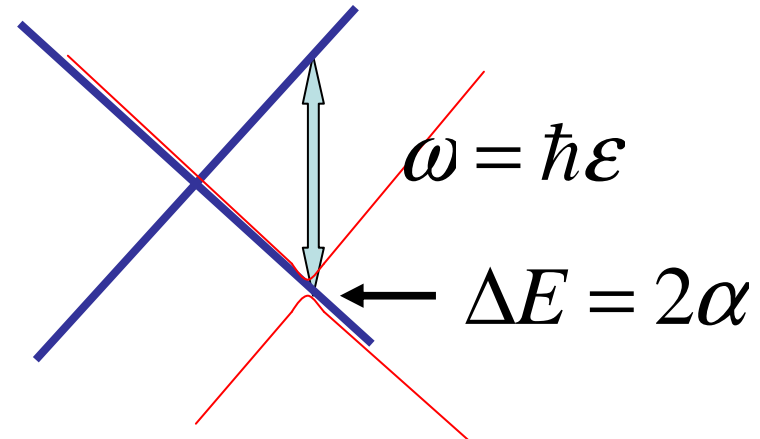
$$p = 1 - \exp\left(-\frac{\pi(\Delta E)^2}{2|M_{\text{in}} - M_{\text{out}}|v}\right)$$

Control of quantum states

- Field sweep LZS mechanism
- Quantum oscillation (tunneling resonance)
- Alternating field
 - Sx Rabi oscillation
(e.g. $\pi/2$ pulse NMR)
 - Sz Floquet phenomena
(Nontrivial resonance)

Spin-rotation pulse

Transverse oscillating field



$$i\hbar \frac{\partial}{\partial t} |\psi\rangle = H(t) |\psi\rangle$$

$$= \left(-\hbar \varepsilon S^z + \alpha (S^+ e^{i\omega t} + S^- e^{-i\omega t}) \right) |\psi\rangle$$

$$|\phi\rangle = e^{-i\omega S^z t} |\psi\rangle$$

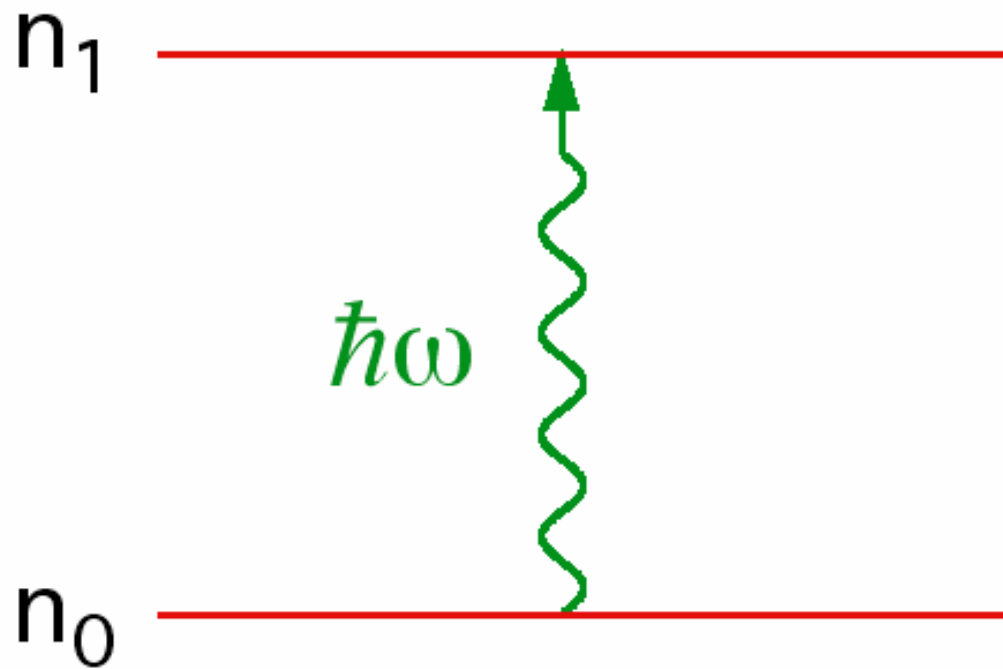
$$i\hbar \frac{\partial}{\partial t} |\phi\rangle = \left(-\hbar (\varepsilon - \omega) S^z + 2\alpha S^x \right) |\phi\rangle$$

Pulse duration τ

$$2\alpha\tau = \frac{\pi}{2} \quad \text{Rotation around the x - axis : } 90^\circ$$

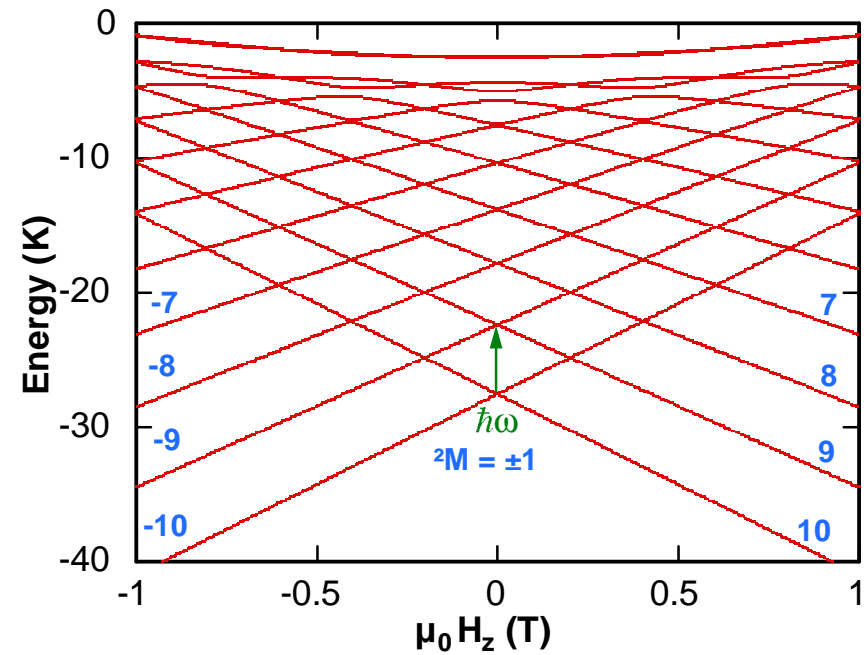
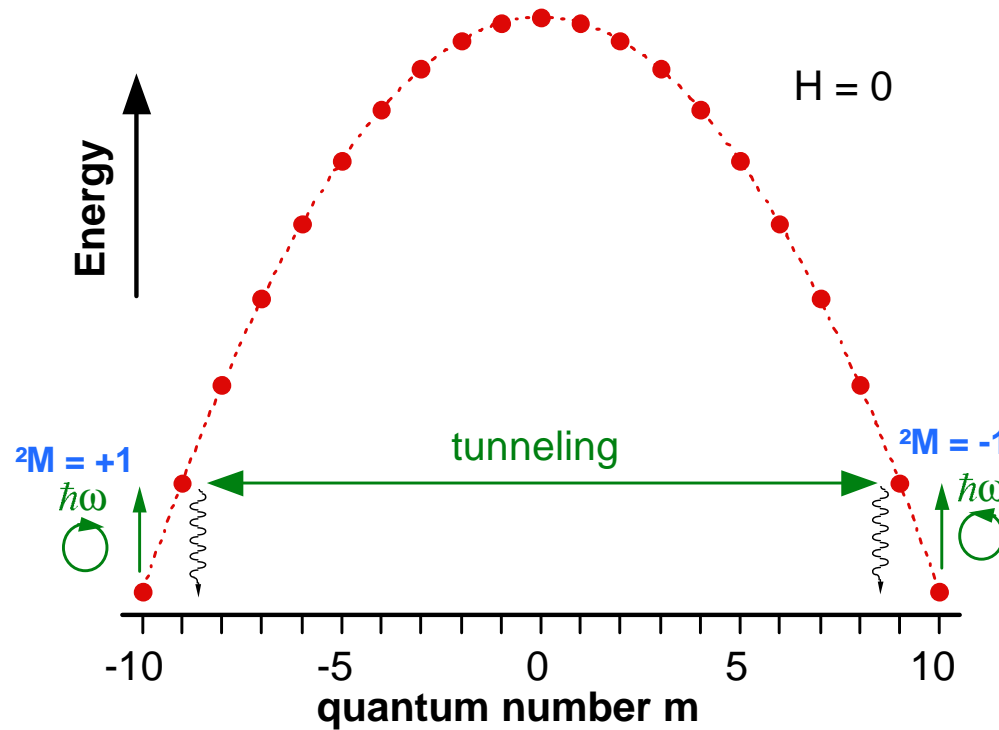
Interaction with photons

(microwaves: 1 to 115 GHz)



Photon assisted tunneling

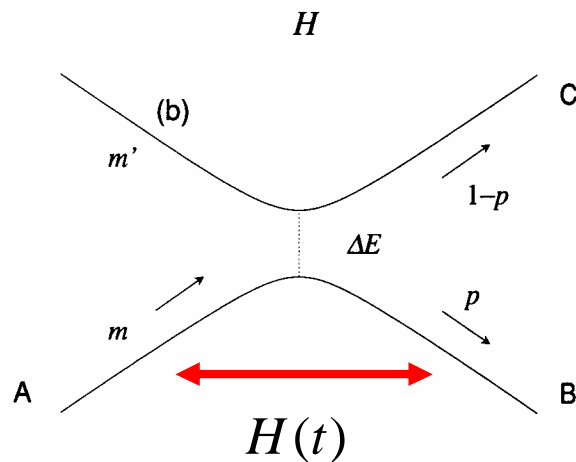
Absorption of circular polarized microwaves



Resonance on the AC field

Non-trivial Resonance

$$H(t) = -h_W \cos(\omega t) \sum_i S_i^z$$

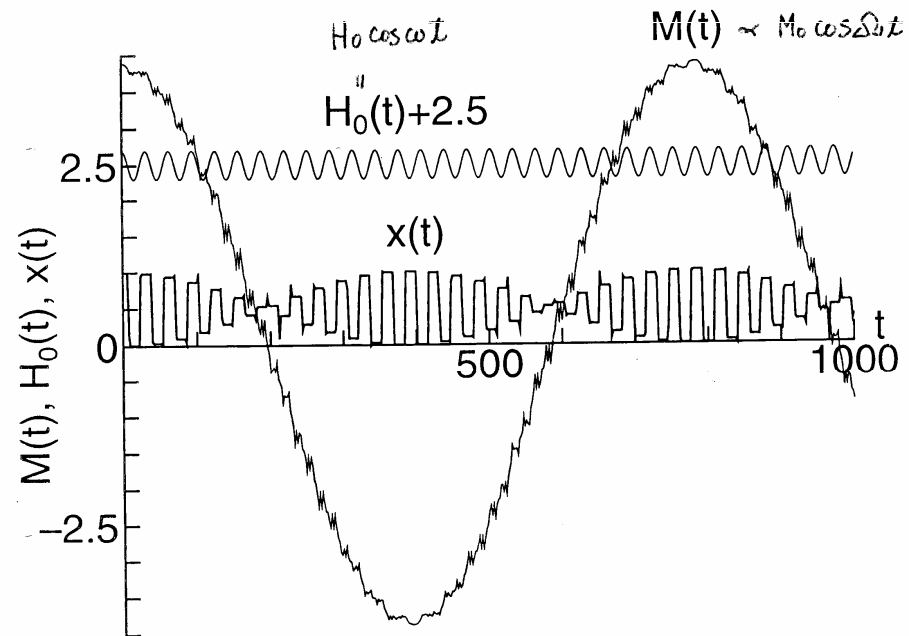


$$M(t) = M_0 \cos(\Omega t + \delta),$$

$$\Omega = \frac{\omega}{\pi} \sqrt{2p(1-\cos\alpha)}$$

$$p = 1 - \exp\left(-\frac{\pi(\Delta E)^2}{4c\Delta M}\right)$$

$$M(t) \quad \Gamma=0.5, \omega=0.2, H_0=0.2$$



Y. Kayamuma, PRB 47 (1993) 9940
SM, K. Saito, H. De Daedt,
Phys. Rev. Lett. 80 (1998) 1525.

Hz resonance

$$H(t) = -\Gamma S^x - (h + A \sin(\omega t)) S^z, \quad \vartheta(t) = \int_0^t (h + A \sin(\omega s)) ds$$

$$F = T e^{\int_0^{2\pi/\omega} H(u) du}$$

$$= T e^{\int_0^{2\pi/\omega} \frac{i}{2} \Gamma \begin{pmatrix} 0 & e^{i\vartheta(u)} \\ e^{-i\vartheta(u)} & 0 \end{pmatrix} du} \approx \exp\left(-\frac{i}{2} \Gamma \begin{pmatrix} 0 & \varepsilon \\ \varepsilon^* & 0 \end{pmatrix}\right)$$

$$\varepsilon \equiv \int_0^{2\pi/\omega} e^{i\vartheta(u)} du = e^{iA/\omega} \sum_{n=-\infty}^{\infty} (-i)^n J_n\left(\frac{A}{\omega}\right) \int_0^{2\pi/\omega} e^{i(h-n\omega)u} du$$

at $h = n\omega$

$$M(t) = \cos(\Omega t), \quad \Omega = \Gamma J_n\left(\frac{A}{\omega}\right)$$

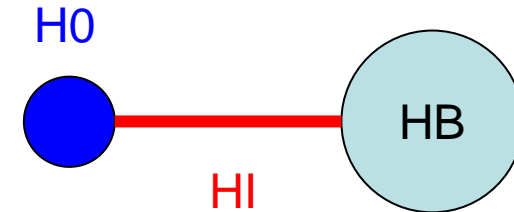
Quantum Master Equation

$$\frac{\partial}{\partial t} \rho = iL\rho = \frac{1}{i\hbar} [H_0 + H_I + H_B, \rho]$$

$$H = H_0 + H_I + H_B,$$

$$H_I = \sum_k \lambda_k (b_k^+ + b_k) X,$$

$$H_B = \sum_k \omega_k b_k^+ b_k$$



Reduction of environment

$$\sigma = p\rho = \rho_{\text{eq}} \text{Tr}_B \rho, \quad \rho_{\text{eq}} = e^{-\beta H_0} / \text{Tr}_B e^{-\beta H_0}$$

$$\begin{aligned} \frac{\partial}{\partial t} \sigma &= ipL\sigma + piL \int_0^t e^{(t-s)(1-p)iL} (1-p)iLp\rho(s) ds \\ &+ piL e^{(t-s)(1-p)iL} (1-p)\rho(0) \end{aligned}$$

e.g. Photon dissipation and pumping :

(SM., H. Ezaki, and E. Hanamura PRA 57 (1998) 2046)

$$\frac{\partial \sigma}{\partial t} = \frac{1}{i\hbar} [H_0, \sigma] - \kappa (b^+ b \sigma - 2b \sigma b^+ + \sigma b^+ b)$$

Lindblad form \rightarrow Stochastic Schrodinger Equation (antibunching, squeezing photo emission)

General formulation

$$\frac{d\rho}{dt} = \frac{1}{i\hbar} [H, \rho]$$

$$-\frac{\lambda^2}{\hbar^2} \int_0^t ds \int_{-\infty}^{\infty} d\omega e^{i\omega t} \Phi(\omega) \left\{ XX(-s)\rho(t) - e^{\beta\hbar\omega} X\rho(t)X(-s) \right. \\ \left. + e^{\beta\hbar\omega} \rho(t)X(-s)X - X(-s)\rho(t)X \right\}$$

time correlation function of the reservoir's operators $\Phi(t)$

$$\Phi(\omega) = \int_{-\infty}^{\infty} dt e^{-i\omega t} \Phi(t) = \hbar \gamma(\omega)^2 \frac{D(\omega) - D(-\omega)}{e^{\beta\hbar\omega} - 1}$$

$I(\omega) = \gamma(\omega)^2 D(\omega) = I_0 \omega^\alpha \quad \omega > 0$: the spectral density

Independent phonon bath

$$H = H_0 + H_I + H_B,$$

$$H_I = \sum_k \lambda_k (b_k^+ + b_k) X,$$

$$H_B = \sum_k \omega_k b_k^+ b_k$$

$$\frac{d\rho}{dt} = -i[H, \rho] - \lambda \left([X, R\rho] + [X, R\rho]^+ \right)$$

$$\langle k|R|m \rangle = \zeta \left(\frac{E_k - E_m}{\hbar} \right) n_\beta(E_k - E_m) \langle k|X|m \rangle,$$

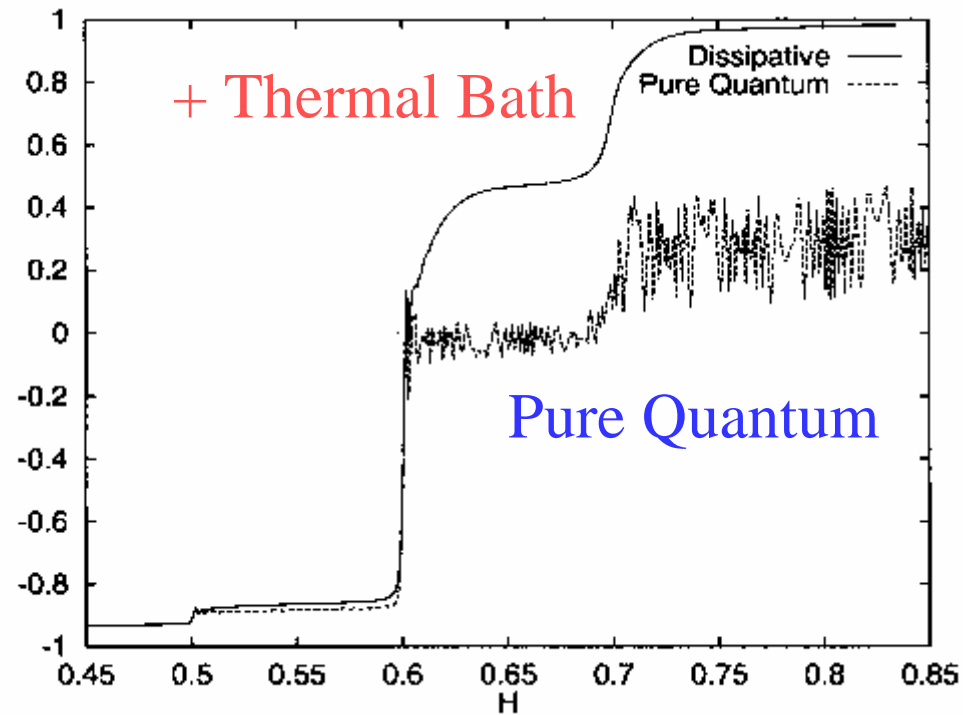
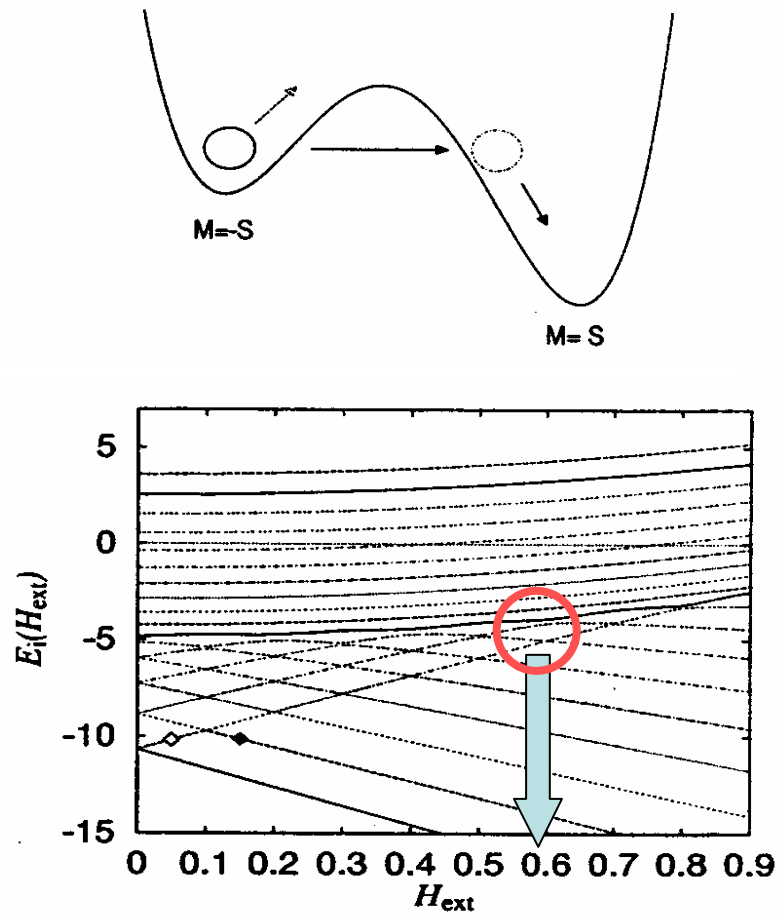
$$\zeta(\omega) = I(\omega) - I(-\omega)$$

K. Saito, S. Takesue and SM. Phys. Rev. B61 (2000) 2397

No feedback effects

Adiabatic transition and Relaxation

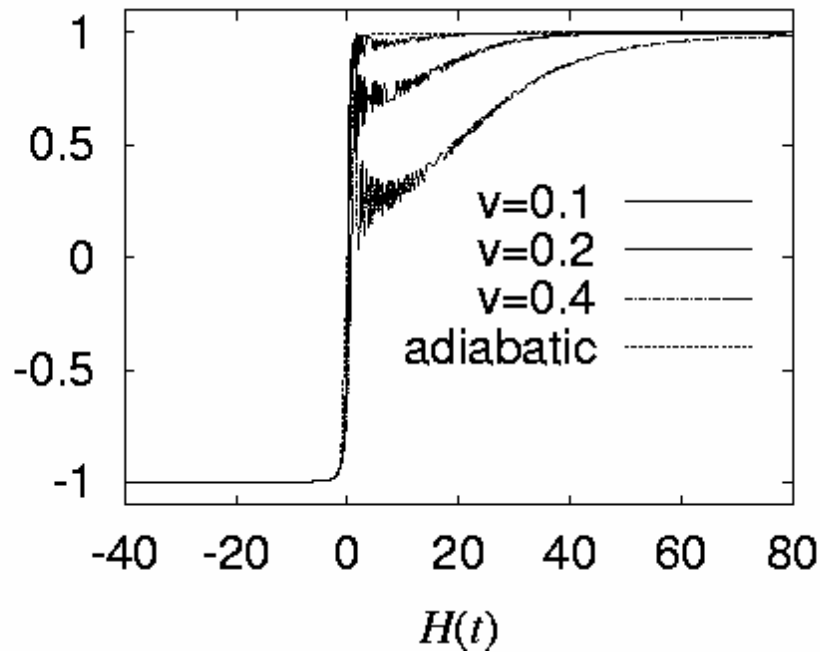
$$T \rightarrow 0$$



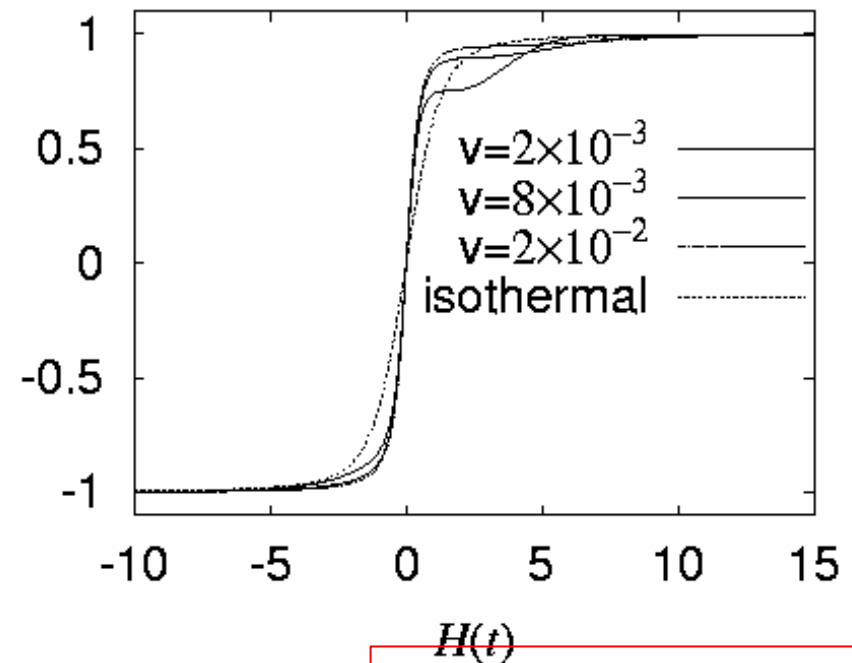
K. Saito, SM, H.de Raedt,
Phys. Rev. B60 (1999) 14553

Field sweeping with thermal bath

Fast sweeping

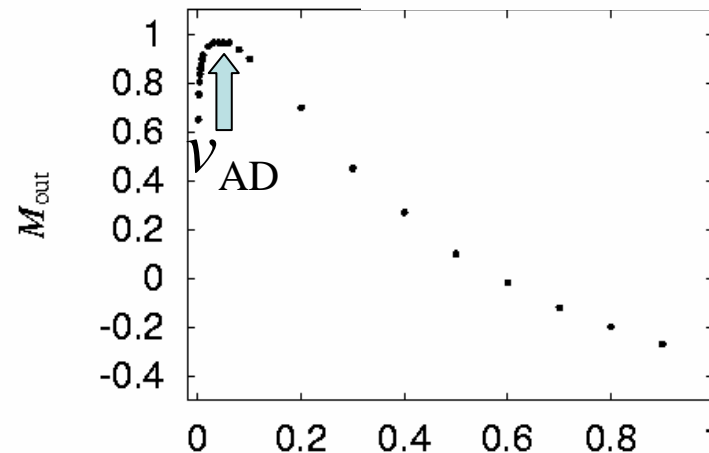


Slow sweeping



$$v_{AD} < v$$

LZS

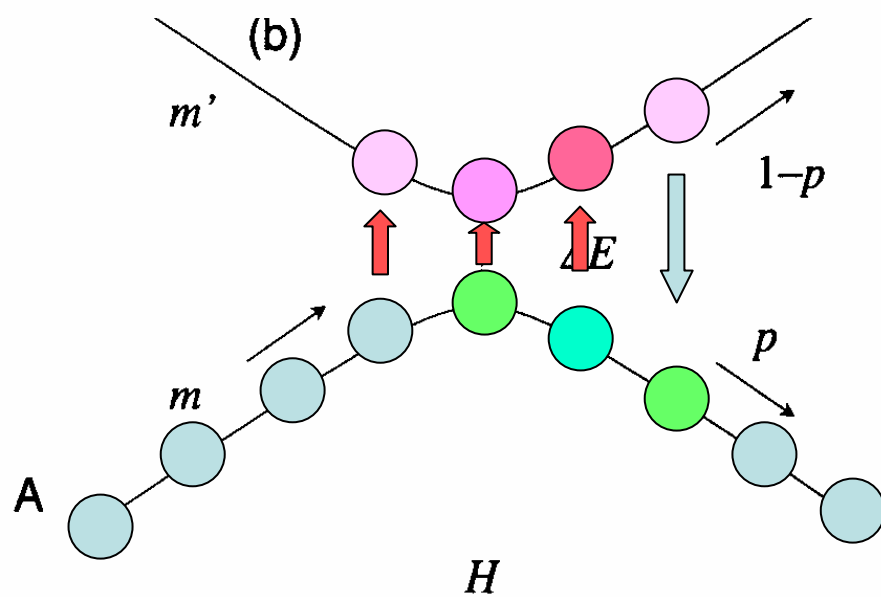
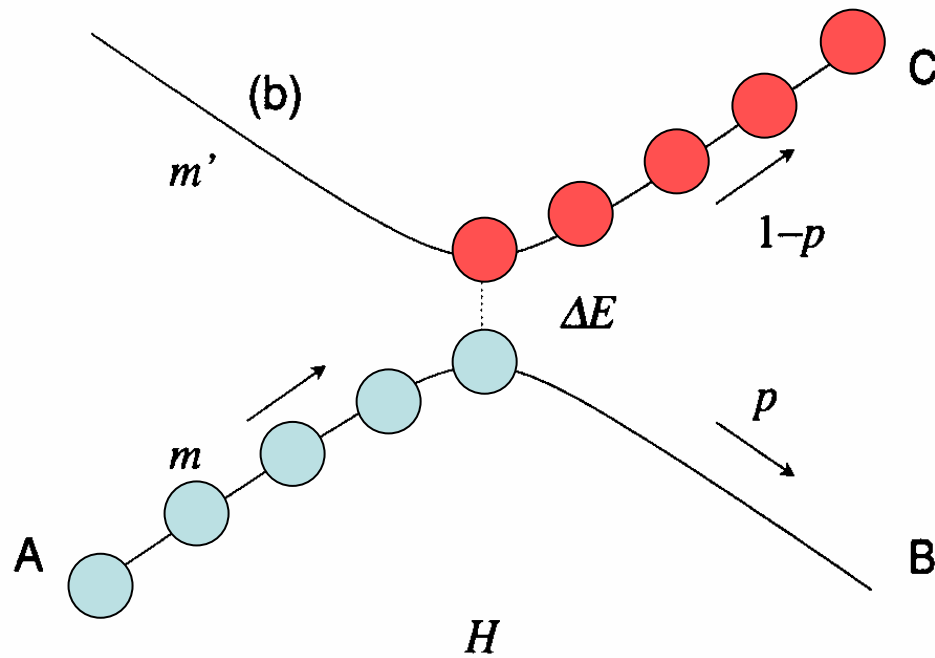


$$v_{TH} < v < v_{AD}$$

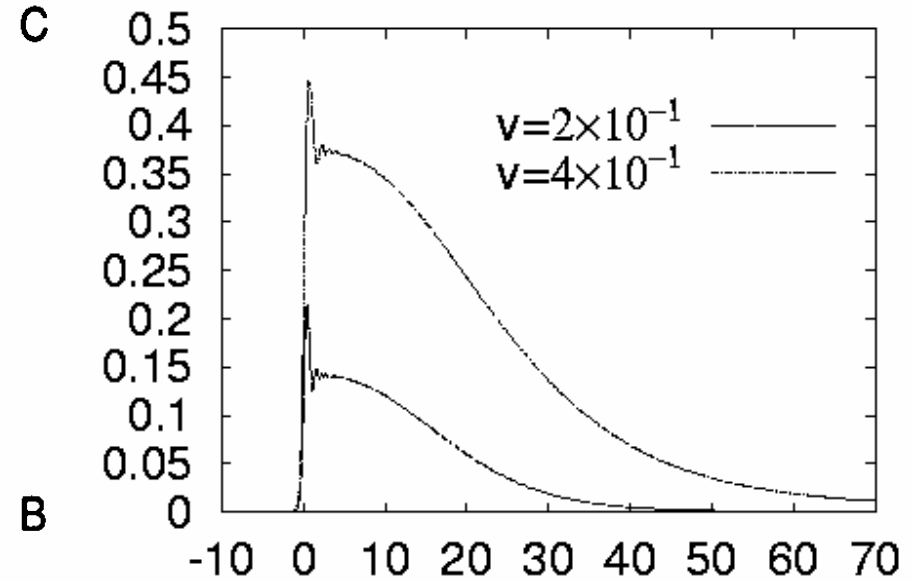
Magnetic
FoehnEffect

K. Saito & SM.
JPSJ (2001) 3385.

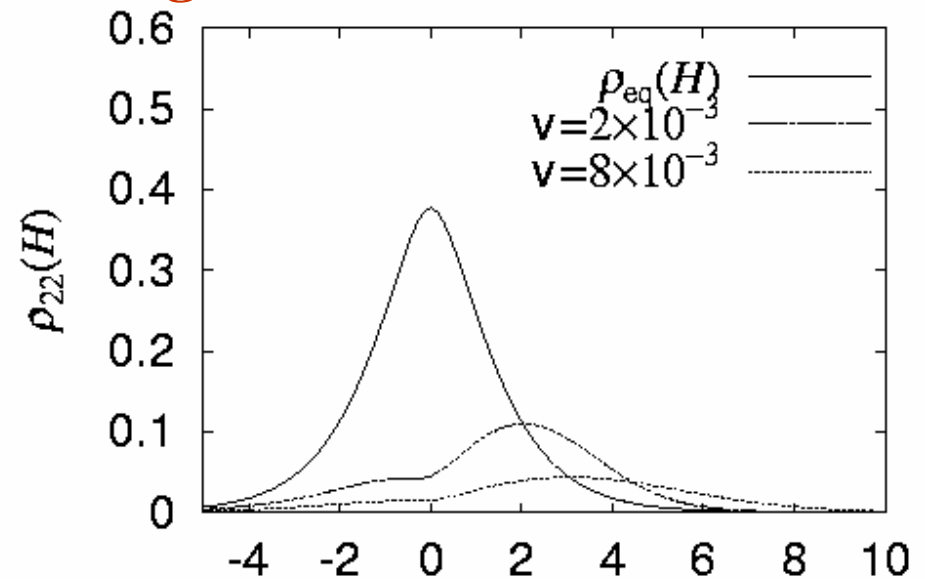
Nonadiabatic Tr. & Heat-inflow



LZ transition

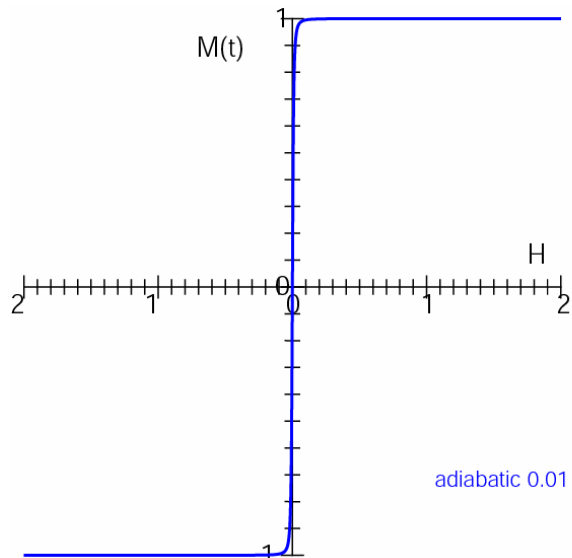
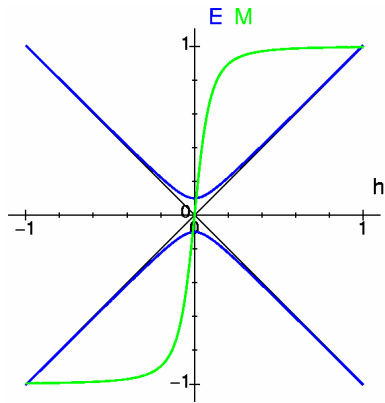


Magnetic Foehn Effect

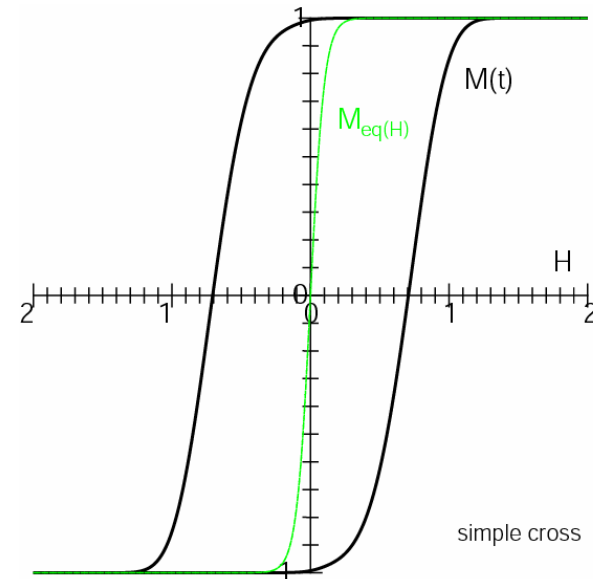
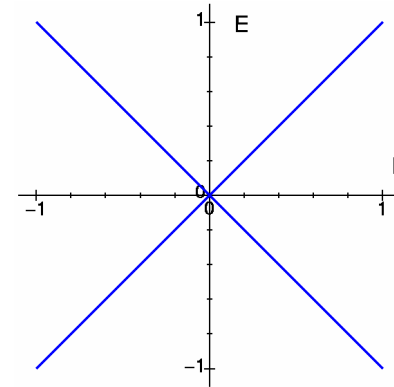


Various types of magnetization process

Adiabatic change



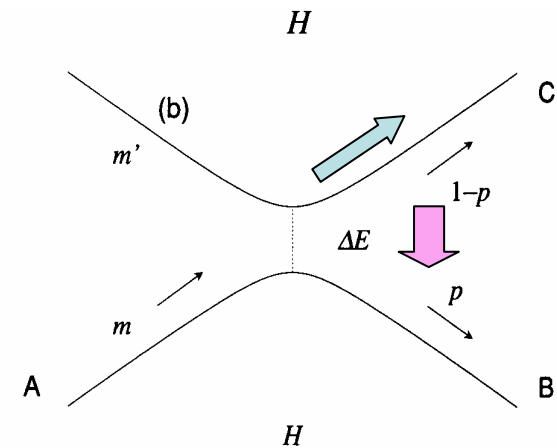
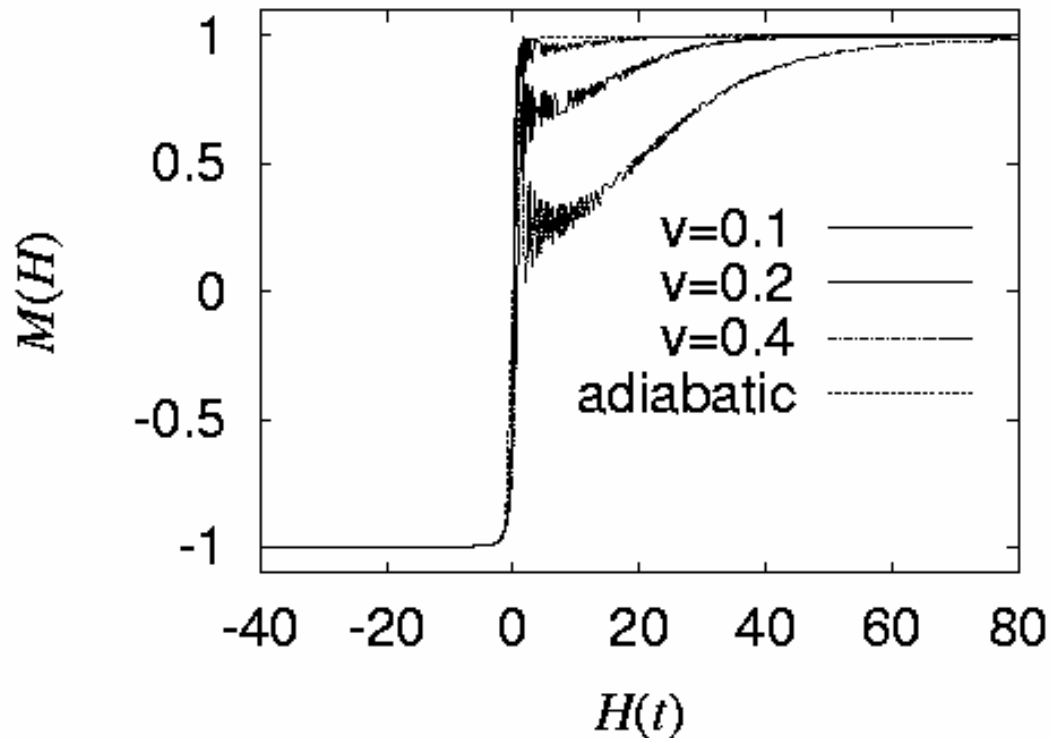
Thermal relaxation (no Gap)



Non adiabatic transition

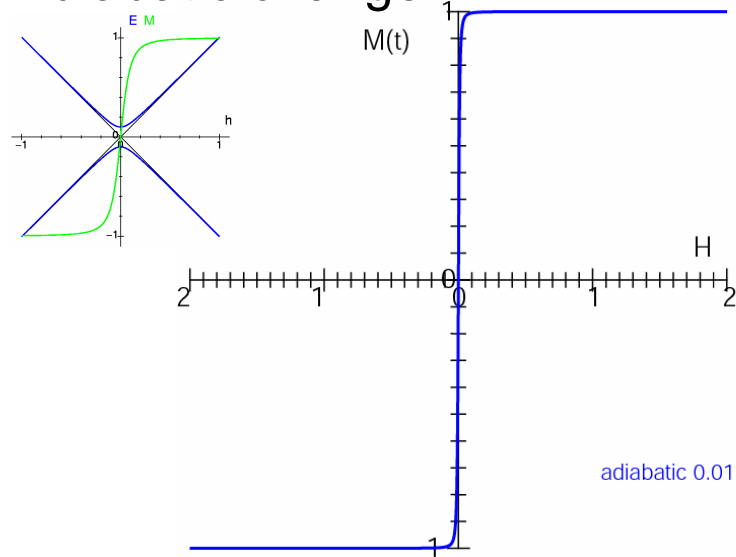
Fast sweeping

$$v_{AD} < v$$

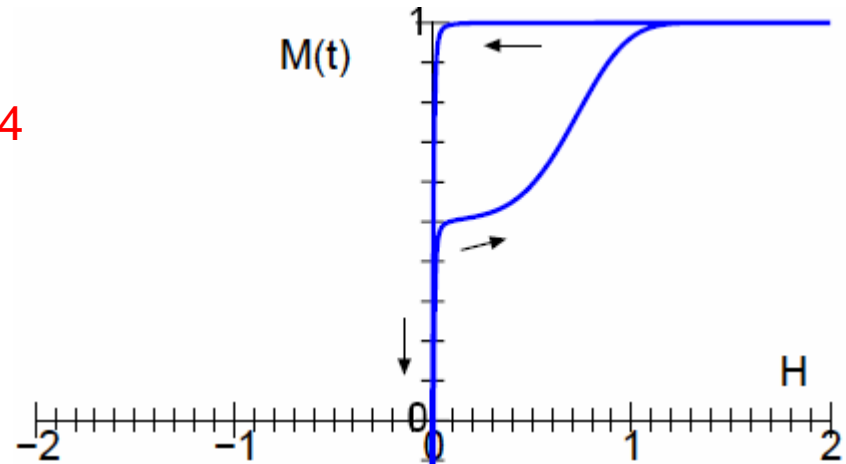


LZ transition + Thermal relaxation

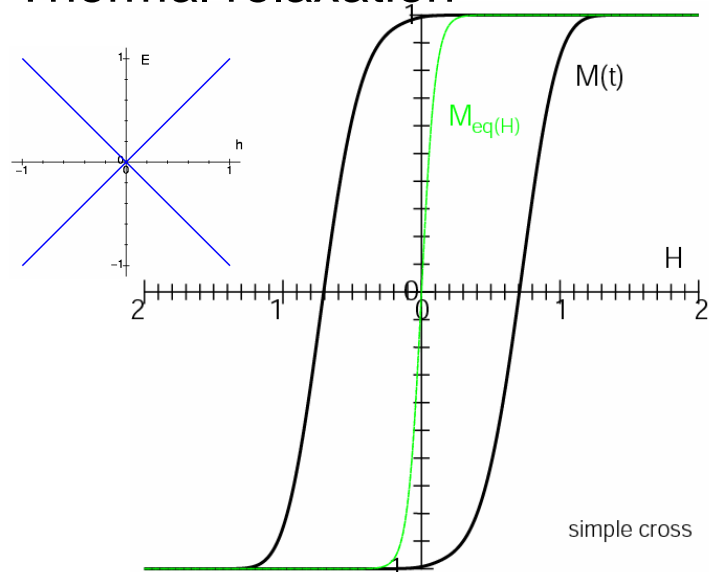
Adiabatic change



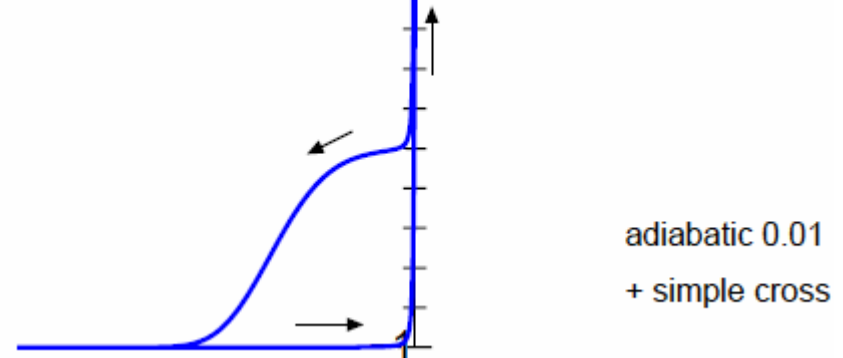
x 3/4



Thermal relaxation

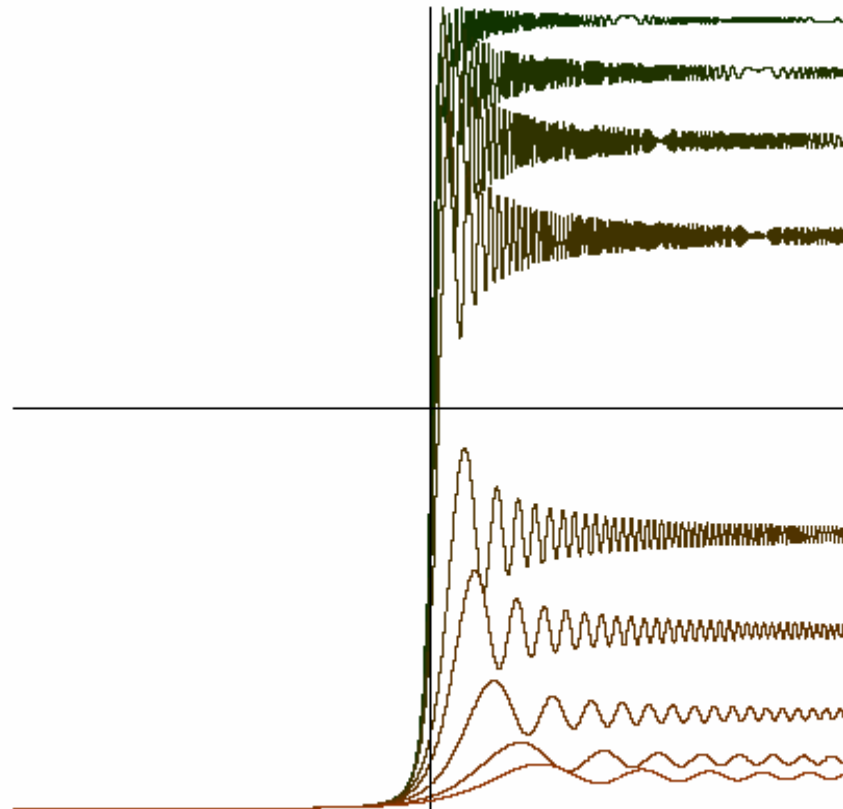


x 1/4

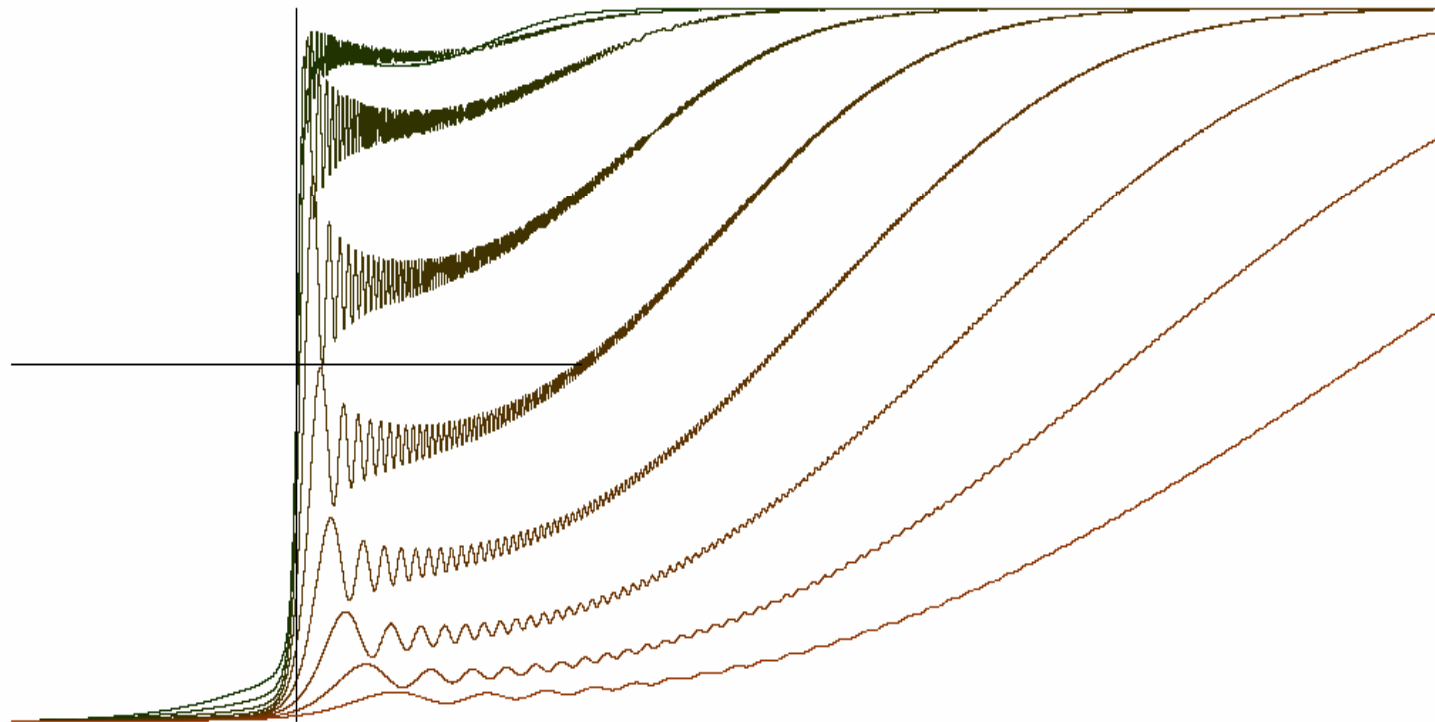


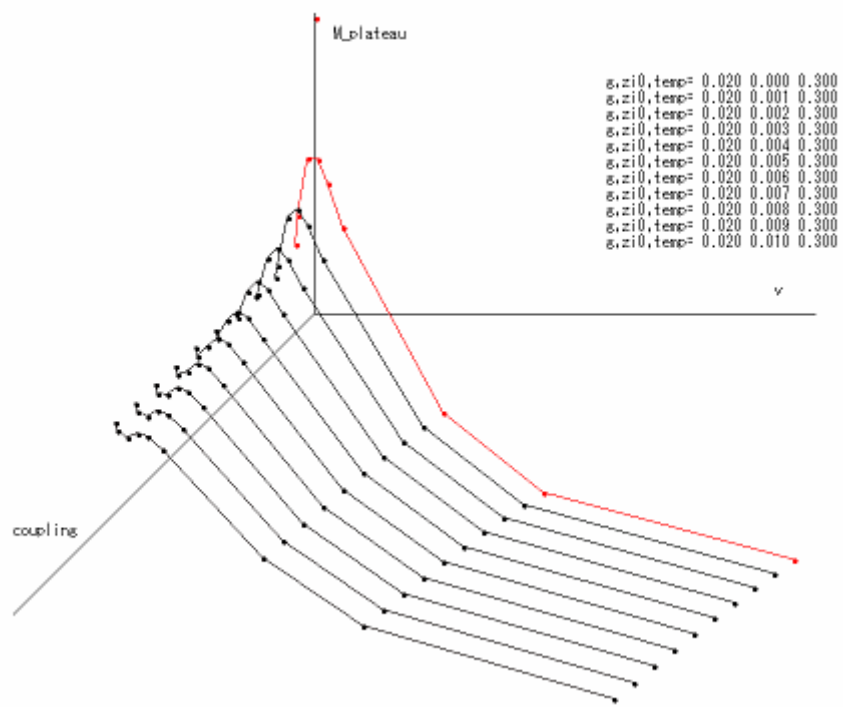
cf. Tetra-nicle(II) D. H. Hendrickson

itime0, iout, maxtime=	366300	666	g,vh,zi0,temp=	0.02000	0.00030	0.00000	0.30000
itime0, iout, maxtime=	220000	400	g,vh,zi0,temp=	0.02000	0.00050	0.00000	0.30000
itime0, iout, maxtime=	157035	285	g,vh,zi0,temp=	0.02000	0.00070	0.00000	0.30000
itime0, iout, maxtime=	110000	200	g,vh,zi0,temp=	0.02000	0.00100	0.00000	0.30000
itime0, iout, maxtime=	36630	66	g,vh,zi0,temp=	0.02000	0.00500	0.00000	0.30000
itime0, iout, maxtime=	22000	40	g,vh,zi0,temp=	0.02000	0.01000	0.00000	0.30000
itime0, iout, maxtime=	11000	20	g,vh,zi0,temp=	0.02000	0.02000	0.00000	0.30000
itime0, iout, maxtime=	5500	10	g,vh,zi0,temp=	0.02000	0.03000	0.00000	0.30000
itime0, iout, maxtime=	3666	6	g,vh,zi0,temp=	0.02000	0.03000	0.00000	0.30000



itime0, iout, maxtime=	550000	1000	g,vh,zi0,temp=	0.02200	0.00020	0.00010	0.30000
itime0, iout, maxtime=	275000	500	g,vh,zi0,temp=	0.02200	0.00040	0.00010	0.30000
itime0, iout, maxtime=	137500	250	g,vh,zi0,temp=	0.02200	0.00080	0.00010	0.30000
itime0, iout, maxtime=	68750	125	g,vh,zi0,temp=	0.02200	0.00160	0.00010	0.30000
itime0, iout, maxtime=	34348	62	g,vh,zi0,temp=	0.02200	0.00320	0.00010	0.30000
itime0, iout, maxtime=	17174	31	g,vh,zi0,temp=	0.02200	0.00640	0.00010	0.30000
itime0, iout, maxtime=	8580	15	g,vh,zi0,temp=	0.02200	0.01280	0.00010	0.30000
itime0, iout, maxtime=	4291	7	g,vh,zi0,temp=	0.02200	0.02560	0.00010	0.30000
itime0, iout, maxtime=	2148	3	g,vh,zi0,temp=	0.02200	0.05120	0.00010	0.30000
					9765		





Diagonalization of L

$$\frac{\partial}{\partial t} \rho = \frac{1}{i\hbar} [H, \rho] - \gamma ([X, R(t), \rho] + [X, R(t), \rho]^\dagger)$$

matrix $\rho(i, j)$, $(i, j = 1, \dots, N)$

↓

vector $\vec{\rho}$, $(\rho(k), k = 1, \dots, N^2)$

$$\frac{\partial}{\partial t} \vec{\rho}(t) = L \vec{\rho}(t) \quad \vec{\rho}(t) = e^{iLt} \vec{\rho}(0)$$

$$\vec{\rho}(t) = \prod_k e^{iL_k t} \vec{\rho}(0)$$

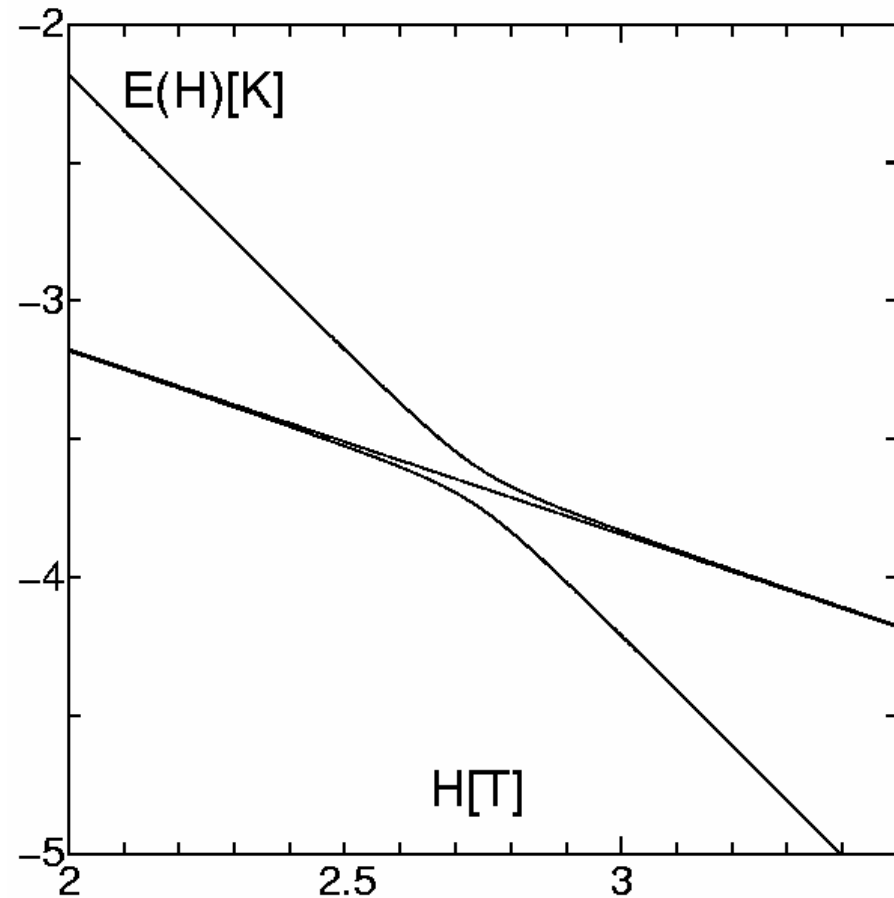
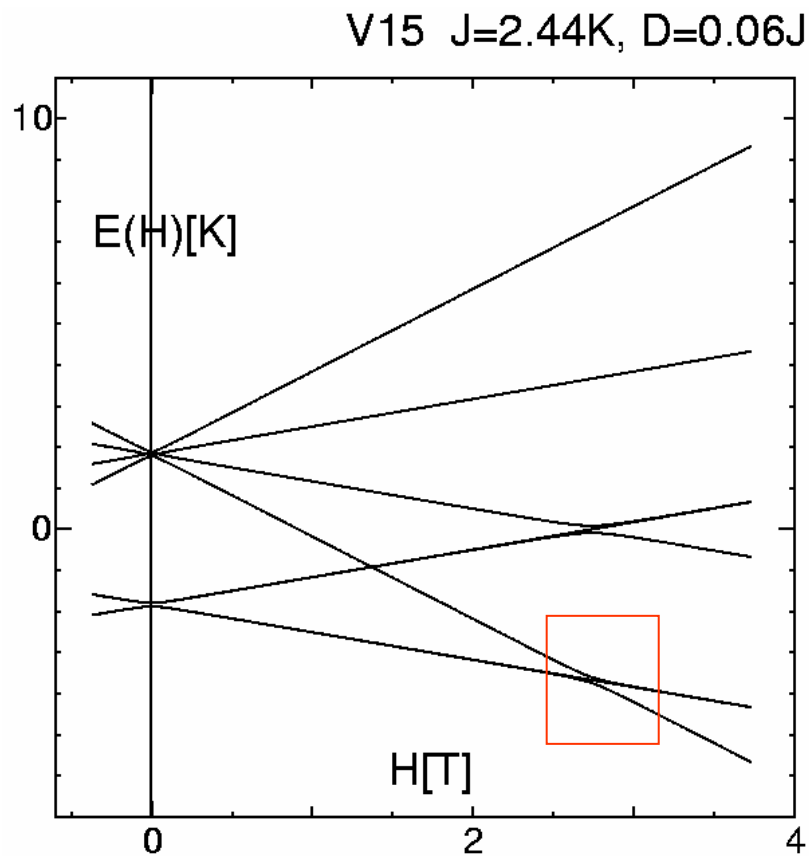
Field changes little in an interval. $H(t) \cong H(t_0)$

The spin evolves a lot in the interval (many precession).

Effects of doubly degenerate structure

Transition from $1/2 \leftrightarrow 3/2$

V15 $J=2.44K$, $D=0.06J$



Smooth magnetization process in the ground state

cf. Heisenberg spin models:

Limit of N infinity

Continuous energy levels vs. Gap

Finite system (steps like magnetization in the Heisenberg model, where $[H, M_z]=0$)

**Adiabatic change: smooth magnetization process
at $T=0$**

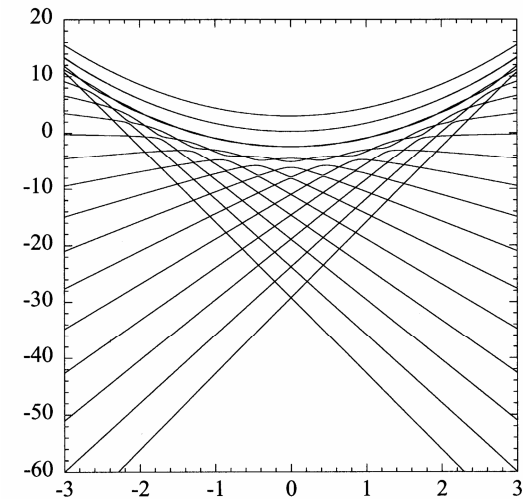
Some mixing term (quantum fluctuation)

Origin of the adiabatic change

$$[H, M_z] \neq 0$$

S: even Large S (S=10) Mn12, Fe8

$$\begin{aligned} H = & -D(S^z)^2 - hS^z \\ & + E((S^x)^2 - (S^y)^2) \\ & + C((S^+)^4 - (S^-)^4) + \text{etc.} \end{aligned}$$



S: odd (S=1/2) V15 No anisotropy & Kramers doublet

Extra-degeneracy + Dzyloshinskii-Moriya interaction

SM, & N. Nagaosa, Prog. Theor. Phys. 106 (2001) 533

Dzyaloshinskii-Moriya interaction

- V15
- Fe-rings Fe10, etc.
- Cu-Benzoate (1DH)
- SrCu₂(BO₃)₂ (SS)

$$H_{ij} = \sum_{\alpha, \beta} S_i^\alpha A_{ij}^{\alpha\beta} S_j^\beta = \sum_{\alpha} J_{ij}^{\alpha} S_i^\alpha S_j^\alpha + \vec{D}_{ij} (\vec{S}_i \times \vec{S}_j)$$

symmetric part $A_{ij}^{\alpha\beta} + A_{ij}^{\beta\alpha}$

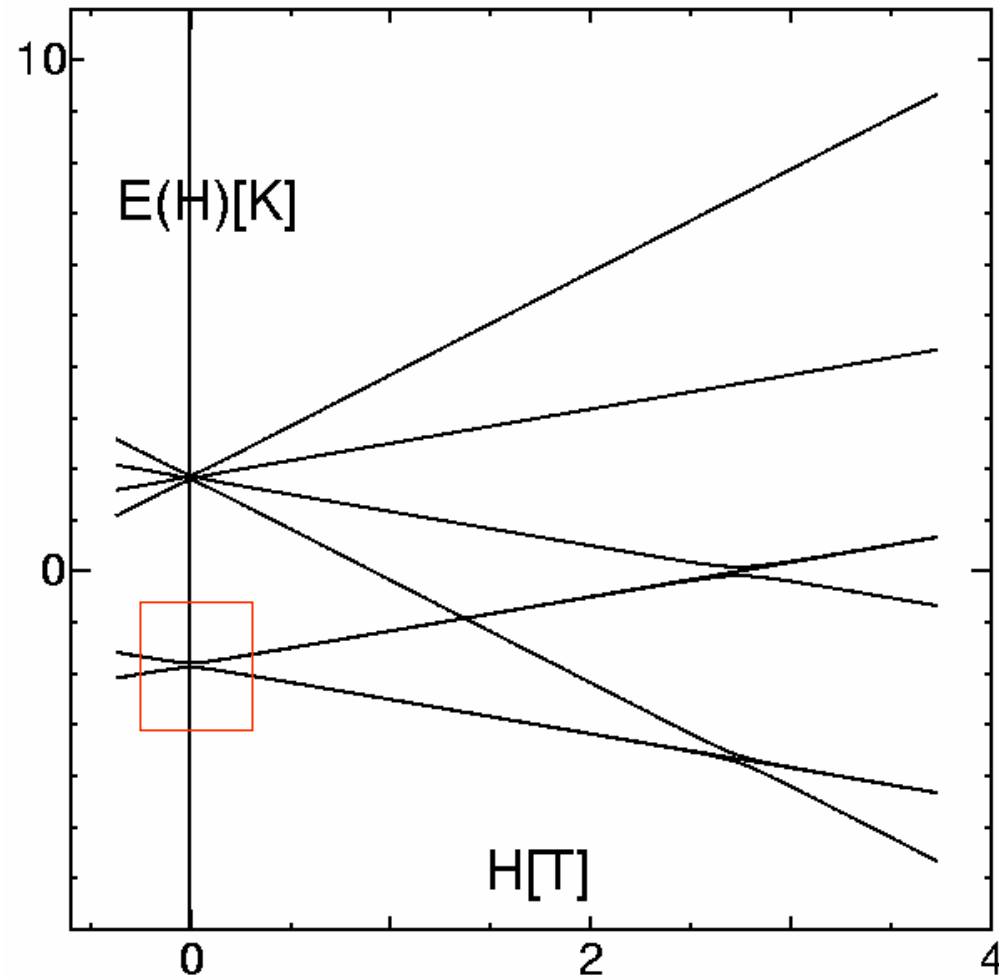
asymmetric part $A_{ij}^{\alpha\beta} - A_{ij}^{\beta\alpha}$

cf.

transverse field $H_x S_x$

DM interaction

V15 $J=2.44\text{K}$, $D=0.06\text{J}$



S: odd ($S=1/2$) V15
Kramers doublet
No tunneling?

Extra-degeneracy +
Dzyloshinskii-Moriya
interaction

SM, & N. Nagaosa,
. Theor. Phys. 106 (2001) 533

Anisotropy of DM interaction

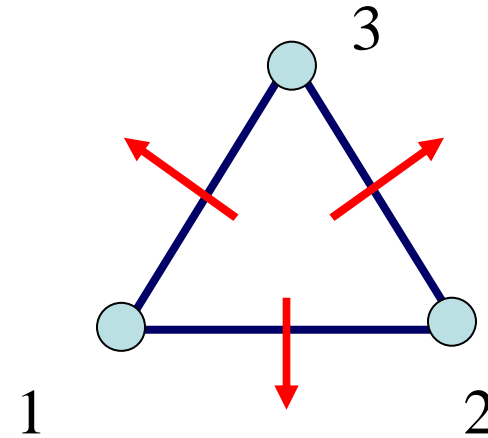
DM interaction on a triangle lattice

C_3 symmetry (axis //z)

1. $\left(\sum_{ij} \vec{D}_{ij} \right) \times \vec{z} = 0,$

2. $\vec{D}_{ij} \cdot \vec{z}$ is the same for all ij

No adiabatic change if $\vec{h} // \vec{z}$



Decoupling of states

$$H = H_0 + D_{12} (S_1^z S_2^x - S_1^x S_2^z) + D_{23} (S_2^z S_3^x - S_2^x S_3^z) + D_{31} (S_3^z S_1^x - S_3^x S_1^z) \\ + d_{12} (S_1^y S_2^z - S_1^z S_2^y) + d_{23} (S_2^y S_3^z - S_2^z S_3^y) + d_{31} (S_3^y S_1^z - S_3^z S_1^y)$$

$$H_{\text{DM}} |+++ \rangle = (x_{31} - x_{12}) | - + + \rangle + (x_{12} - x_{23}) | + - + \rangle + (x_{23} - x_{31}) | + + - \rangle$$

$$x_{ij} = D_{ij} - id_{ij}$$

$$H_{\text{DM}} | + + - \rangle = (x_{12} + x_{23}) | + - - \rangle - (x_{12} + x_{31}) | - + - \rangle + (\bar{x}_{23} - \bar{x}_{31}) | + + + \rangle$$

$$H_{\text{DM}} | + - + \rangle = (x_{12} + x_{31}) | - - + \rangle - (x_{23} + x_{31}) | + - - \rangle + (\bar{x}_{12} - \bar{x}_{23}) | + + + \rangle$$

$$H_{\text{DM}} | - + + \rangle = (x_{23} + x_{31}) | - + - \rangle - (x_{12} + x_{23}) | - - + \rangle + (\bar{x}_{31} - \bar{x}_{12}) | + + + \rangle$$

$$H_{\text{DM}}^2 | + + + \rangle = (2x_{23}^2 - 2x_{12}x_{31}) | + - - \rangle + (2x_{31}^2 - 2x_{12}x_{23}) | - + - \rangle + (2x_{12}^2 - 2x_{23}x_{31}) | - - + \rangle \\ + (|x_{31} - x_{12}|^2 + |x_{12} - x_{23}|^2 + |x_{23} - x_{31}|^2) | + + + \rangle$$

$$\text{if } x_{12} + x_{23} + x_{31} = x_{12} + e^{i2\pi/3} x_{12} + e^{i4\pi/3} x_{12} = 0$$

$$(2x_{23}^2 - 2x_{12}x_{31}) = (2x_{31}^2 - 2x_{12}x_{23}) = (2x_{12}^2 - 2x_{23}x_{31}) = 0$$

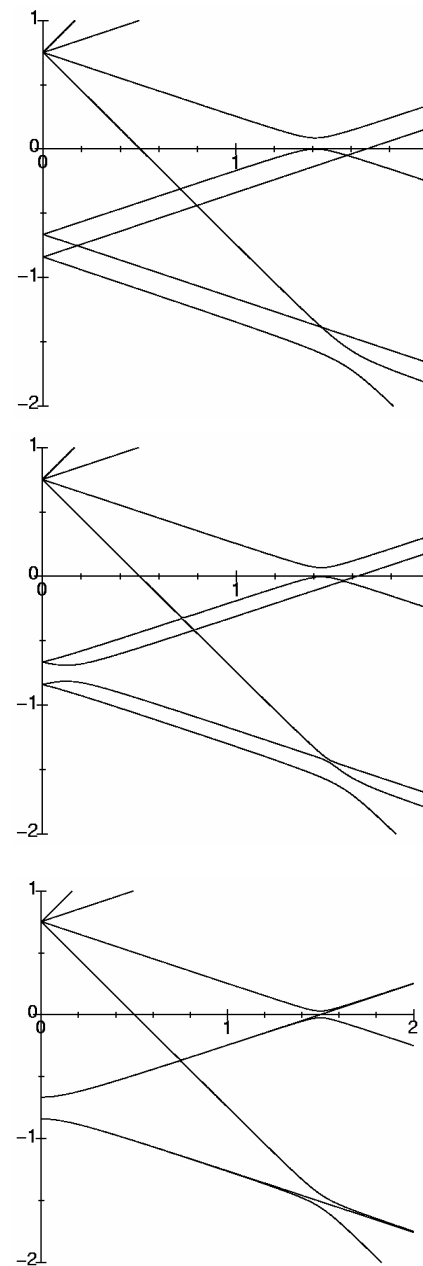
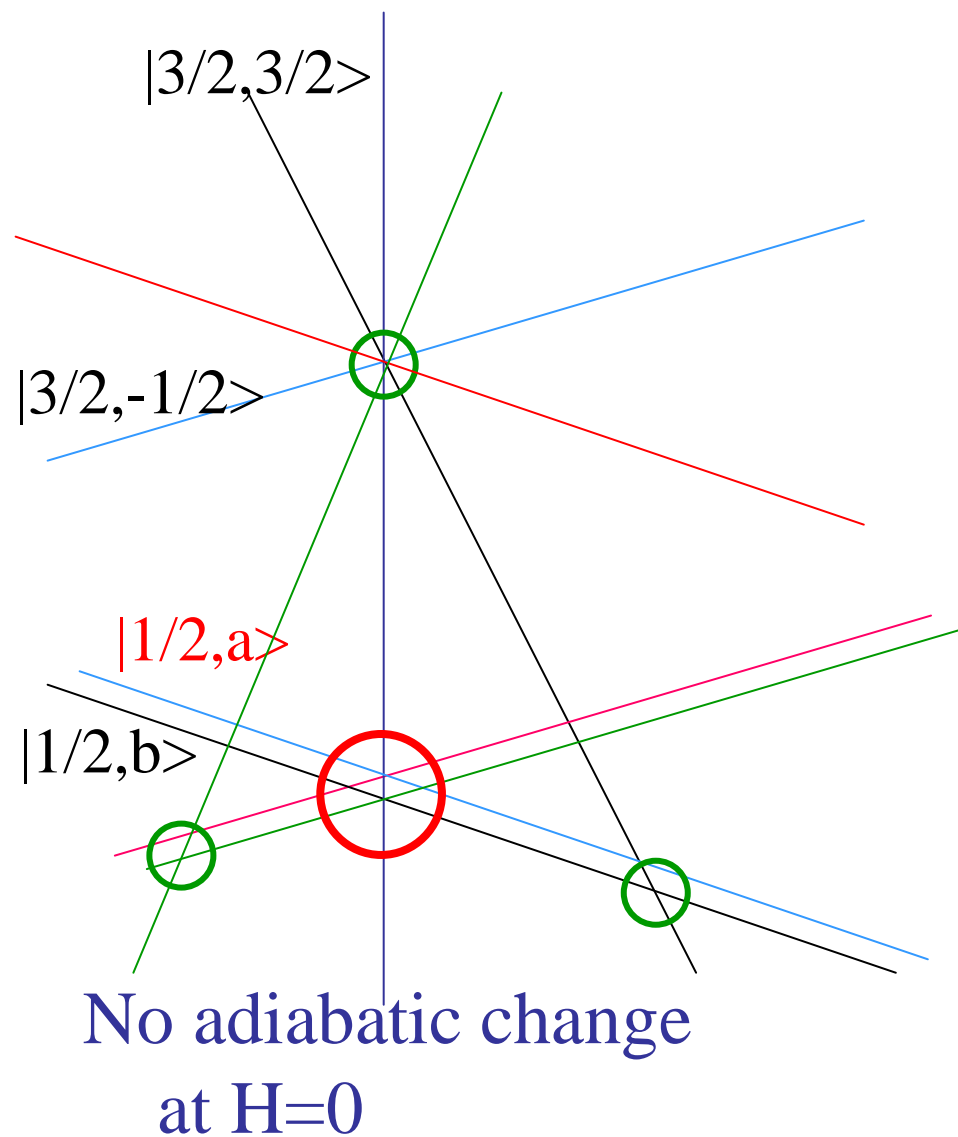
$$| + + + \rangle \Rightarrow | S = 1/2, M = 1/2 \rangle \equiv | a \rangle \Rightarrow \gamma | + + + \rangle$$

$$| - - - \rangle \Rightarrow | S = 1/2, M = -1/2 \rangle \equiv | b \rangle \Rightarrow \gamma | - - - \rangle$$

$$| S = 3/2, M = -1/2 \rangle \Rightarrow | S = 1/2, M = 1/2 \rangle \equiv | b \rangle \quad \langle a | b \rangle = 0$$

$$| S = 3/2, M = 1/2 \rangle \Rightarrow | S = 1/2, M = -1/2 \rangle \equiv | b' \rangle \quad \langle a' | b' \rangle = 0$$

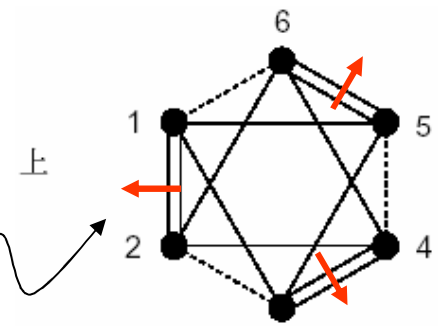
Energy structure with DM



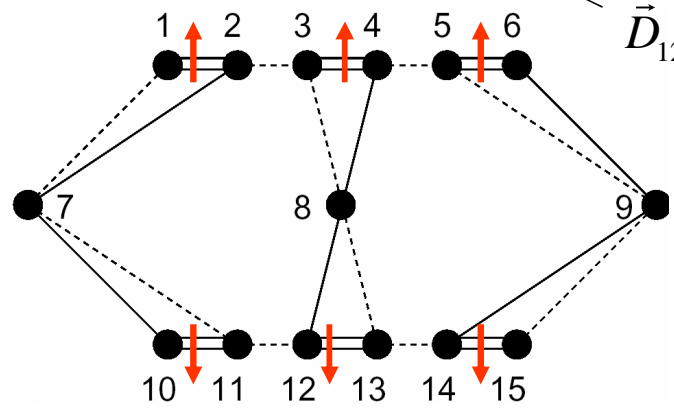
V15 structure

$$H = \sum_{\langle ij \rangle} J_{ij} \vec{S}_i \cdot \vec{S}_j + \sum_{\langle ij \rangle} \vec{D}_{ij} \cdot (\vec{S}_i \times \vec{S}_j) - H_s \sum_i S_i^x$$

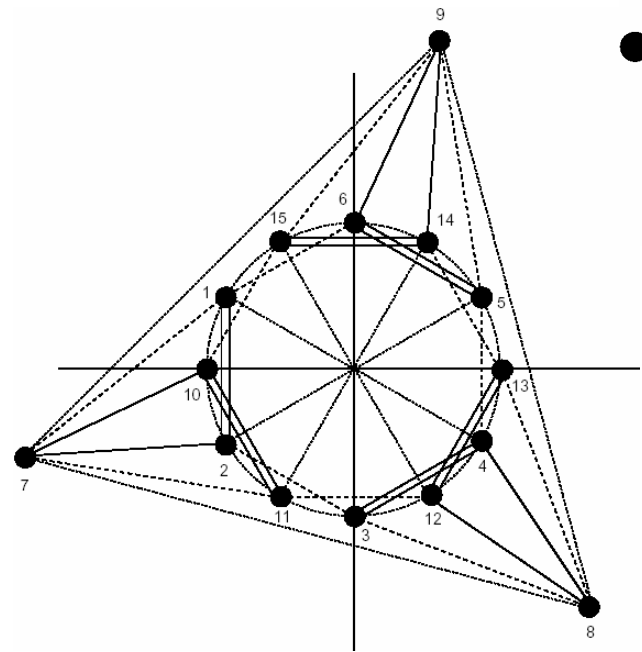
$$\vec{H}_s \perp c$$



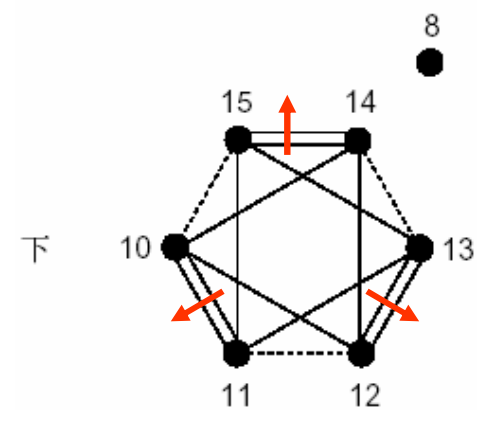
$$\vec{D}_{12} = (40, 40, 40)$$



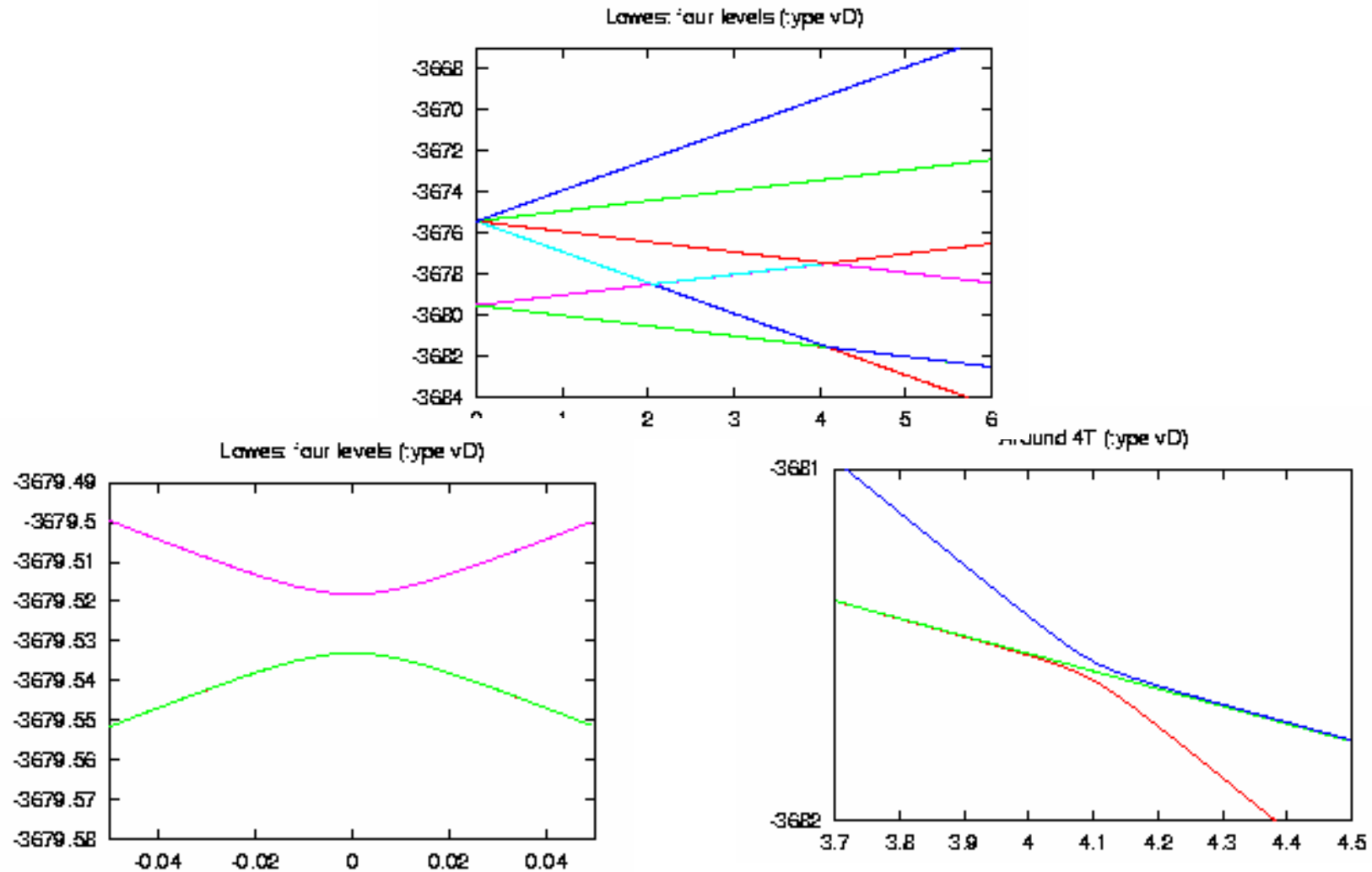
中
● 7



- ==== 800K
- _____ 160K
- 54.4K



Anisotropy of the Gap: Hard axis

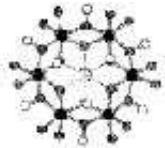


I.Chiorescu, W. Wernsdorfer, A. Mueller, SM, and B. Barbara:
PRB 67 (2003) 020402

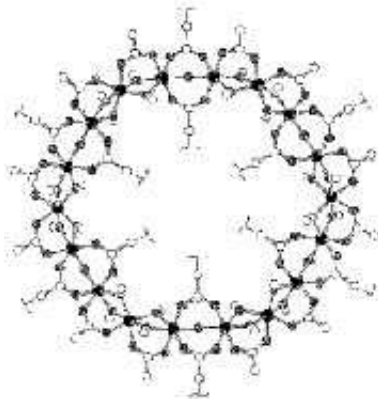
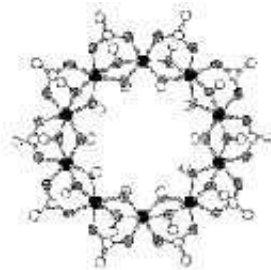
Fe ring

Fe^{3+} plays a role of a localized spin with $S=5/2$ and $L=0$.

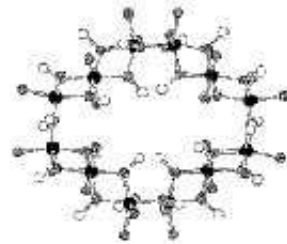
$n=6$



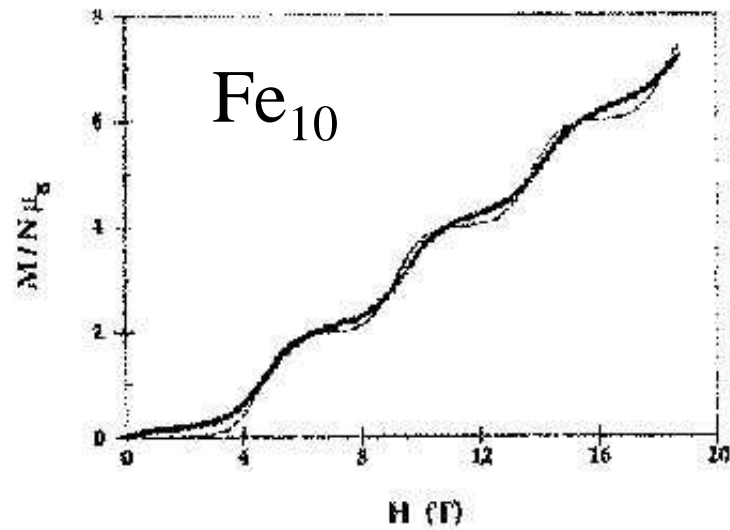
$n=10$

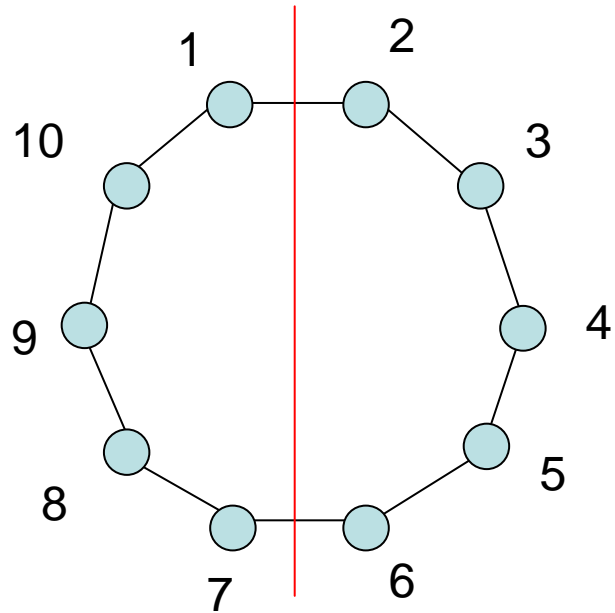


$n=18$



$n=12$





Fe10

$$\sum_{\alpha ij} D_{\alpha} (S_i^{\beta} S_j^{\gamma} - S_i^{\gamma} S_j^{\beta})$$

$$C_{10} + \text{Reflection} \rightarrow S_{10}$$

Mirror symmetry

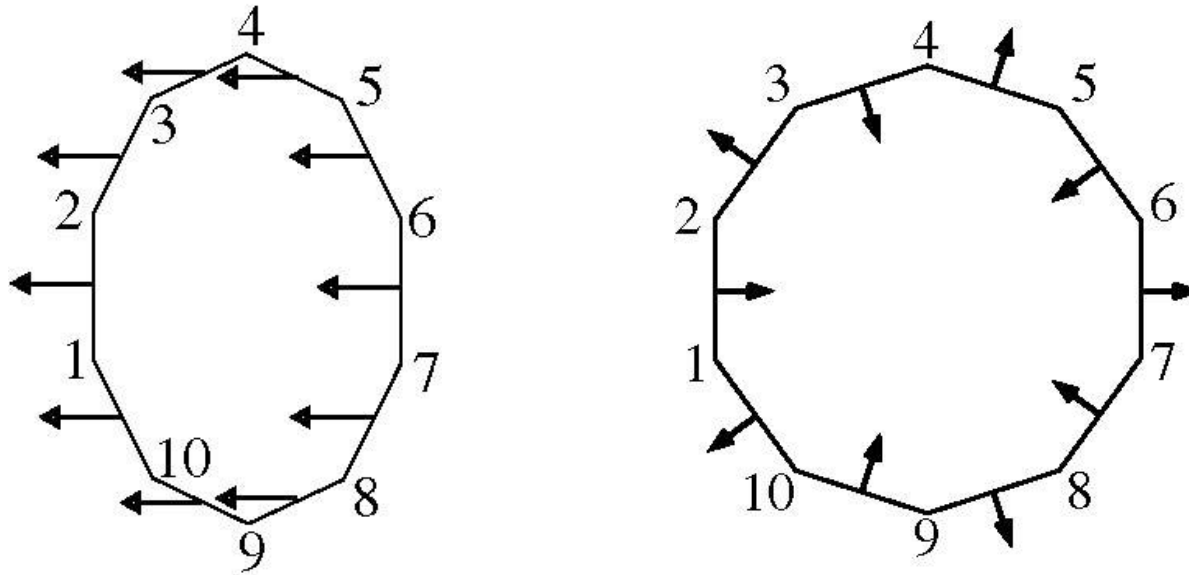
$$\begin{pmatrix} S_5^x \\ S_5^y \\ S_5^z \end{pmatrix} \rightarrow \begin{pmatrix} -S_8^x \\ S_8^y \\ -S_8^z \end{pmatrix}, \quad \begin{pmatrix} S_6^x \\ S_6^y \\ S_6^z \end{pmatrix} \rightarrow \begin{pmatrix} -S_7^x \\ S_7^y \\ -S_7^z \end{pmatrix}. \quad (13)$$

These transformations give

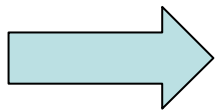
$$\begin{aligned} & \mathbf{d}_{56} \cdot (\mathbf{S}_5 \times \mathbf{S}_6) \\ &= d_{56}^x (S_5^y S_6^z - S_5^z S_6^y) + d_{56}^y (S_5^z S_6^x - S_5^x S_6^z) + d_{56}^z (S_5^x S_6^y - S_5^y S_6^x) \\ &\rightarrow d_{56}^x (-S_8^y S_7^z + S_8^z S_7^y) + d_{56}^y (S_8^z S_7^x - S_8^x S_7^z) + d_{56}^z (-S_8^x S_7^y + S_8^y S_7^x) \\ &= d_{56}^x (S_7^y S_8^z - S_7^z S_8^y) - d_{56}^y (S_7^z S_8^x - S_7^x S_8^z) + d_{56}^z (S_7^x S_8^y - S_7^y S_8^x). \end{aligned} \quad (14)$$

Thus, we obtain $d_{56}^x = d_{78}^x$, $d_{56}^y = -d_{78}^y$ and $d_{56}^z = d_{78}^z$. When one divide a \mathbf{d} vector into a component parallel to the mirror plane and a component

A set of D vectors from static regular structure

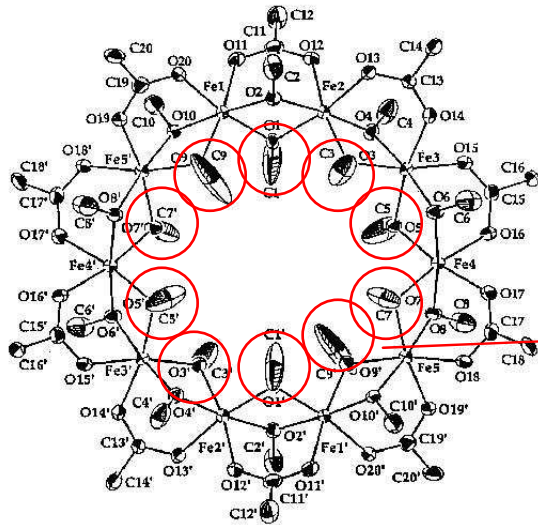


$$\langle \psi_M | \mathcal{H}_{DM} | \psi_{M+1} \rangle = 0$$



The DM interaction of the above D vectors is not the origin of the peaks in dM/dH .

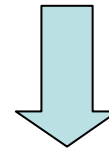
Oscillation of methyl groups



Structure is measured at $T_{st}=226$ K.

Each ellipsoid shows 50% possibility.

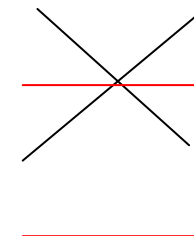
Oblong thermal ellipsoids
with the longer radius a



Elastic constant of an elastic energy of a methyl group
is briefly estimated as $K \sim 0.67^2 k_B T_{st}/a^2$.

H. Nakano and SM: JPSJ 71 (2002) 2580

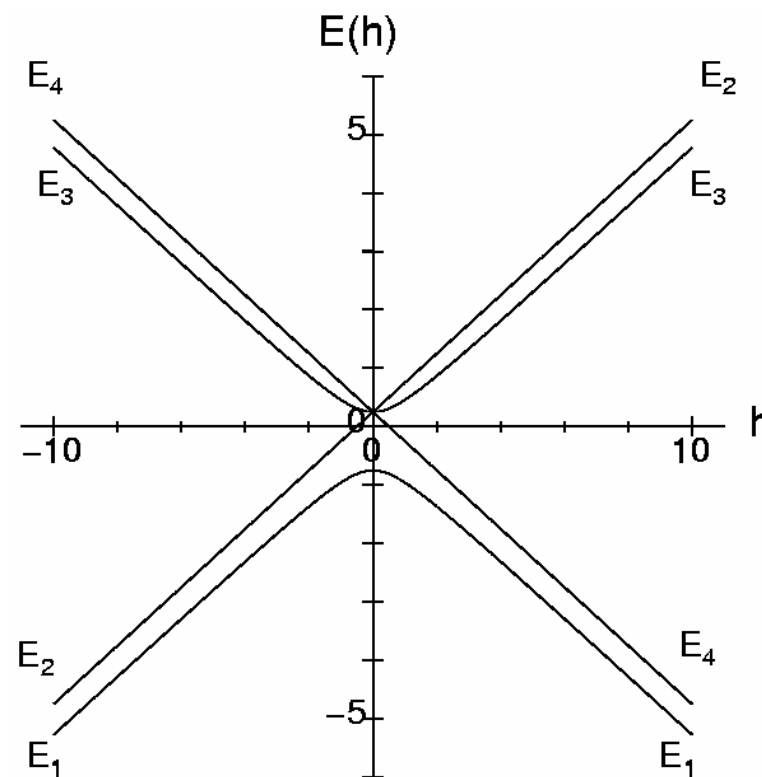
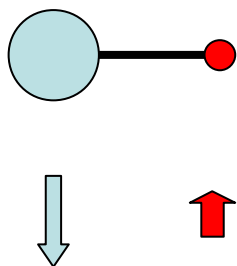
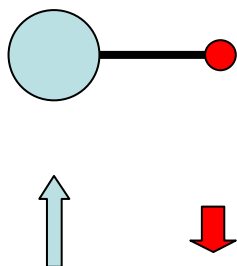
Change of state



$$\begin{cases} |\pm\rangle = \frac{1}{\sqrt{8A^2 + 2\Delta^2 \pm 2\Delta\sqrt{\Delta^2 + 4A^2}}} \left(-2A|+-\rangle + (-\Delta \mp \sqrt{\Delta^2 + 4A^2})|-+\rangle \right) \\ |++\rangle \\ |--\rangle \\ \Delta = h - h' \end{cases}$$

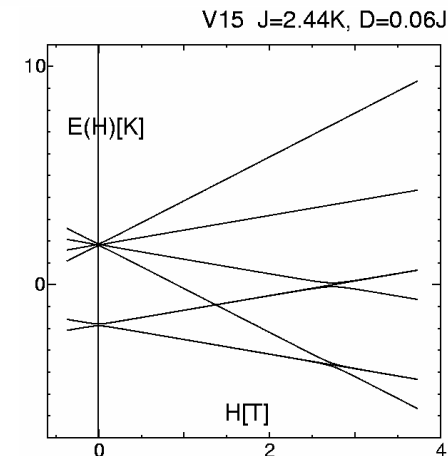
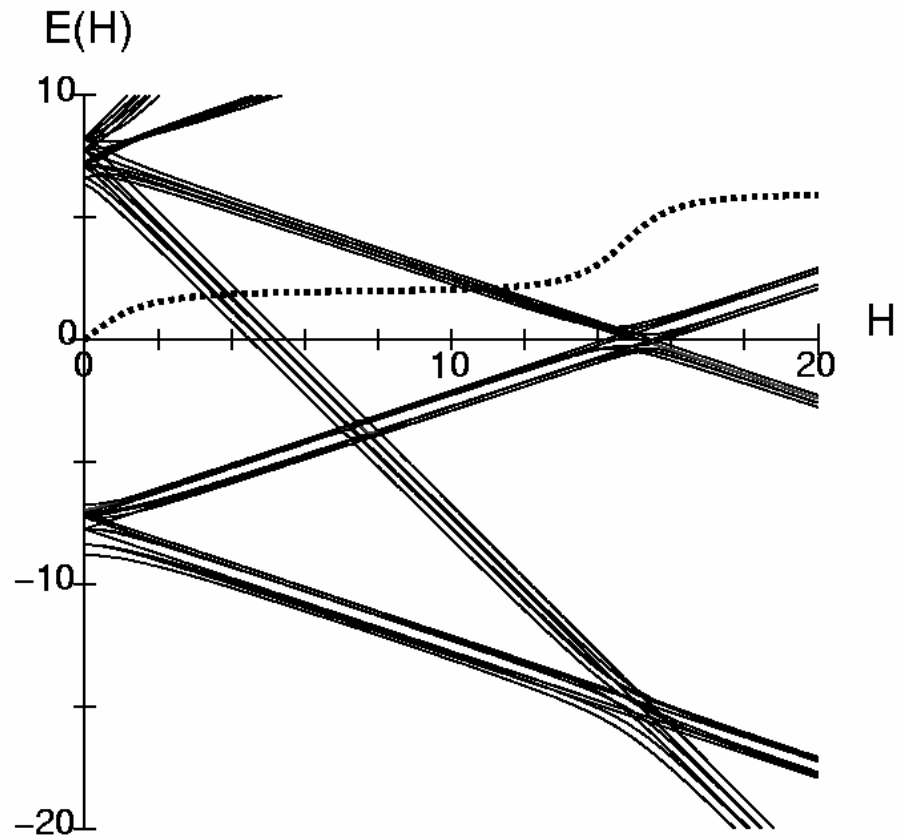
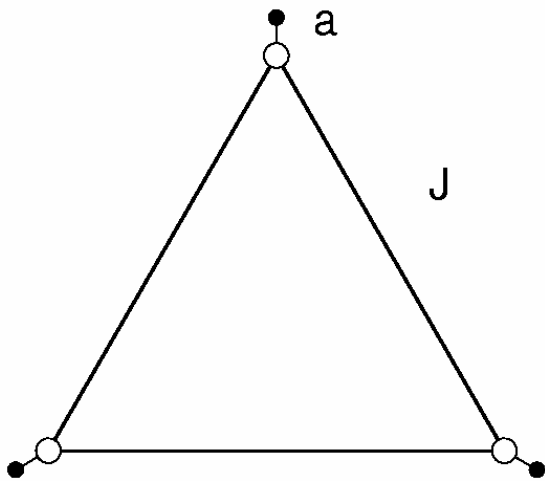
$$\lim_{\Delta \rightarrow \infty} |\pm\rangle = |+-\rangle,$$

$$\lim_{\Delta \rightarrow -\infty} |\pm\rangle = |-+\rangle$$

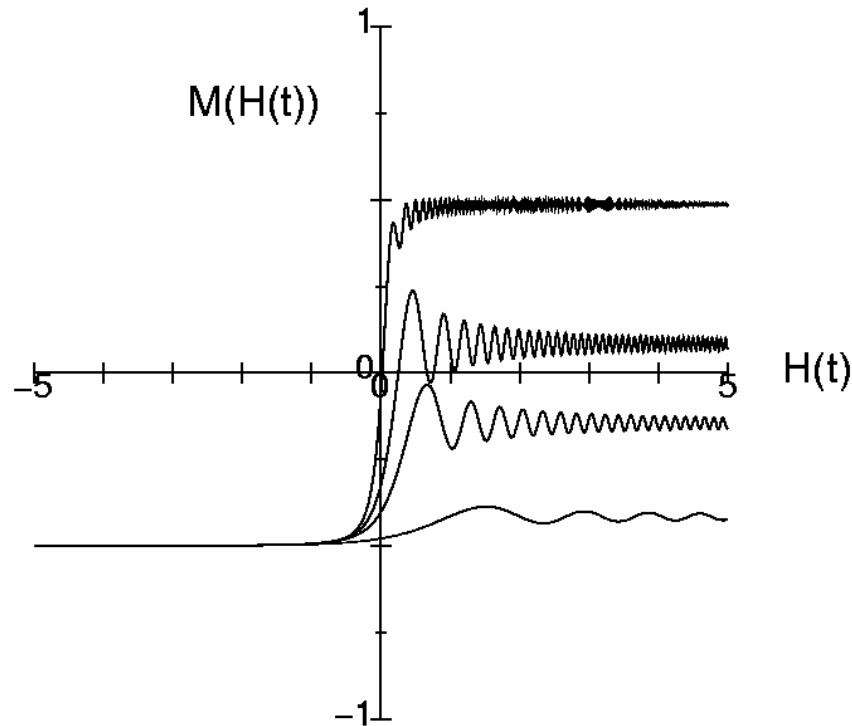


Triangle system

$$H = J \sum_{\langle ij \rangle} \vec{S}_i \cdot \vec{S}_j + \sum_i A \vec{S}_i \cdot \vec{\sigma}_i - \sum_i \left(g\mu_B \vec{S}_i \cdot \vec{h} + g_N \mu_N \vec{S}_i \cdot \vec{h} \right)$$



M(t) from the ground state



$$P = \left| \langle G(H_0) | \Psi(t_f) \rangle \right|^2$$

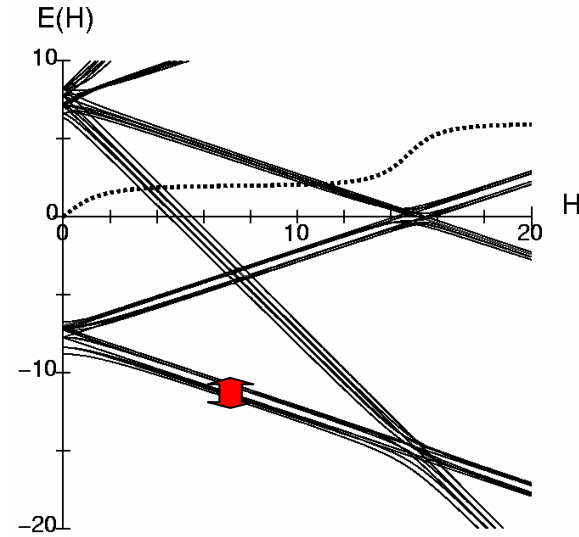
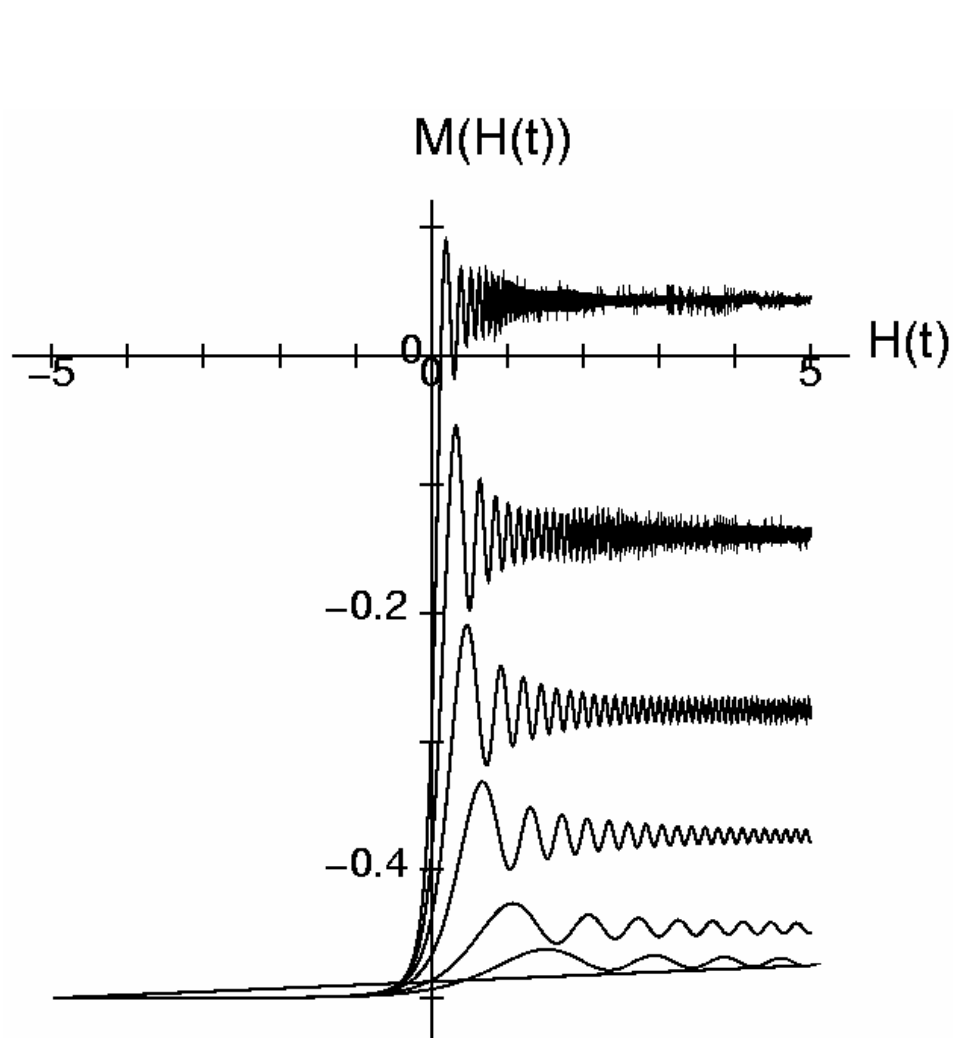
$$\Delta E = \sqrt{-2\nu \log(1-P) / \pi}$$

ν	P	ΔE
0.500	0.08371	0.16681
0.250	0.16067	0.16697
0.100	0.35481	0.16702
0.050	0.58378	0.16704
0.025	0.82678	0.16704
0.010	0.98751	0.16704

$$P = 1 - \exp\left(-\frac{\pi(\Delta E)^2}{2\hbar\nu}\right)$$

Apparent LZS relation

Finite temperature



$$m(t) = \frac{\sum m_i(t) e^{-\beta E_i}}{\sum e^{-\beta E_i}}$$

$$P_{\text{eff}} = \sum_{i=1}^{16} \left| \langle i(H_0) | \Psi(t_f) \rangle \right|^2$$

Reaction to the nuclear spin

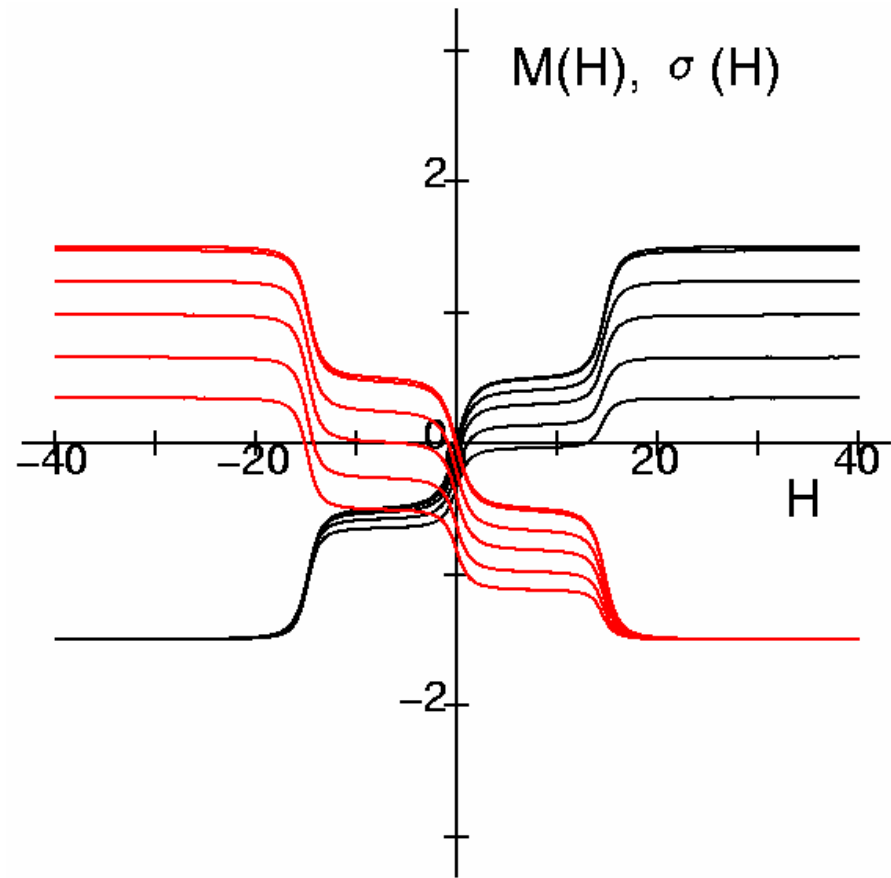
$$\left[\sum_i S_i^z + \sigma_i^z, H \right] = 0,$$

$$\text{c.f.} \left[\sum_i g\mu_B S_i^z + g\mu_N \sigma_i^z, H \right] \neq 0,$$

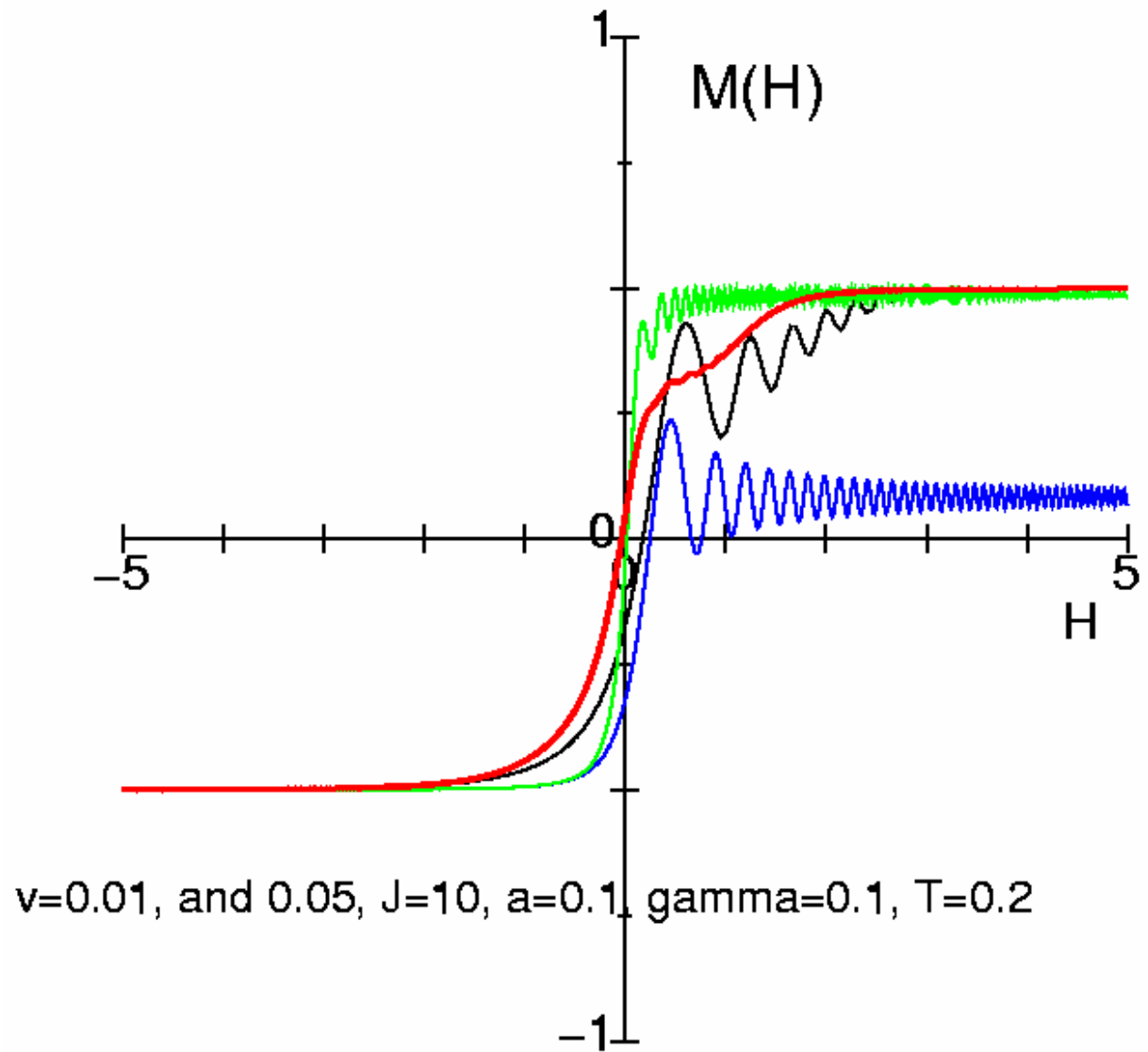
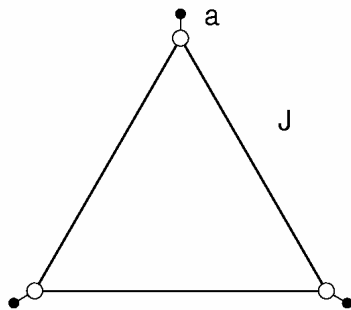
$(S_1, S_2, S_3, \sigma_1, \sigma_1, \sigma_1,)$

$(\text{---} \boxed{\text{---}}) \Rightarrow (\text{---} \boxed{\text{---}})$
 $(\text{---} \boxed{+ \text{---}}) \Rightarrow (+ \text{---} \boxed{\text{---}}),$
 $(\text{---} \boxed{+ + \text{---}}) \Rightarrow (+ + \text{---} \boxed{\text{---}}),$
 $(\text{---} \boxed{+ + +}) \Rightarrow (+ + + \boxed{\text{---}}), \text{etc.}$

$$\langle \sigma \rangle \approx 0 \Rightarrow \langle \sigma \rangle < 0$$

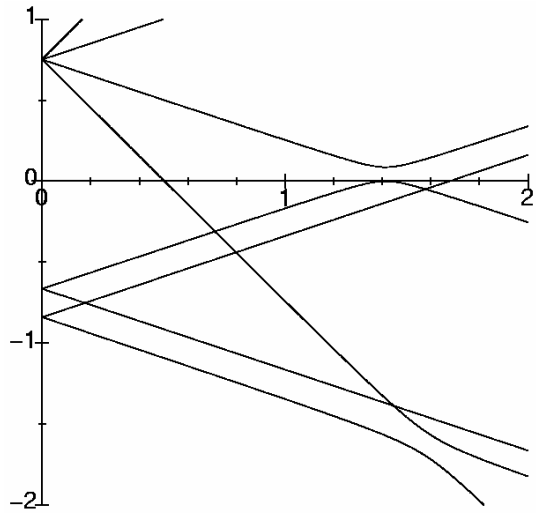


Effects of environments

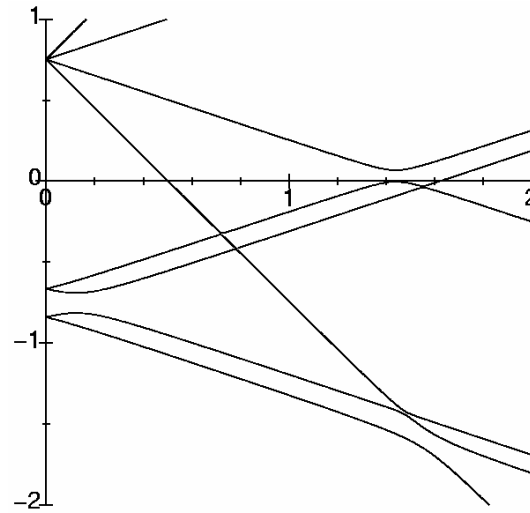


Angle dependence of the energy levels

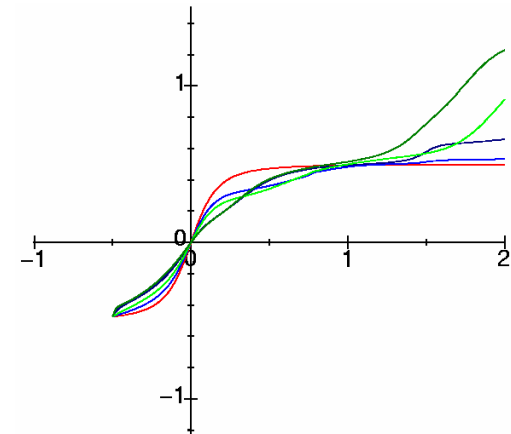
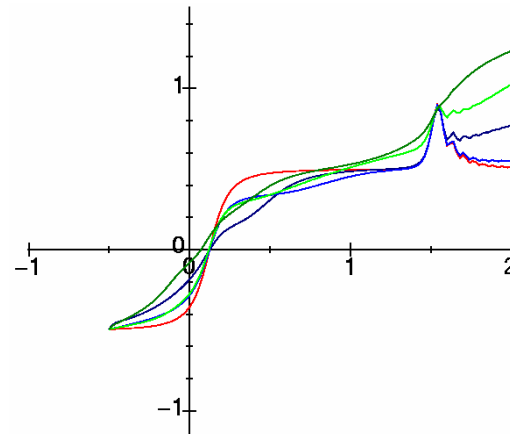
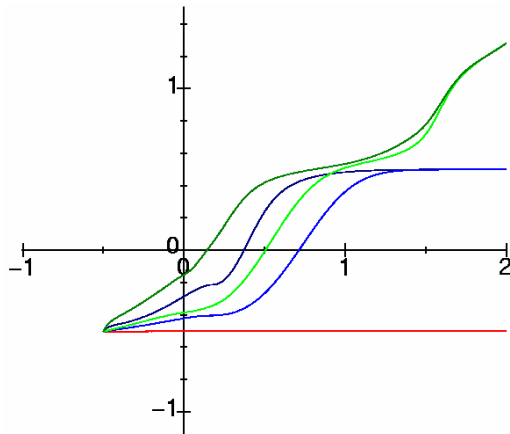
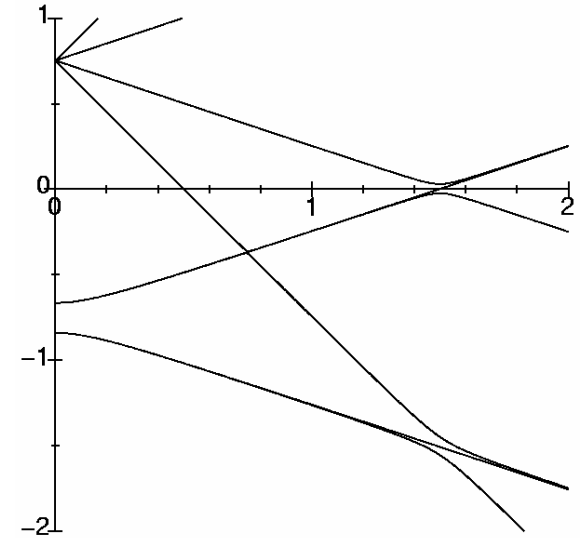
$\theta = 0^\circ$



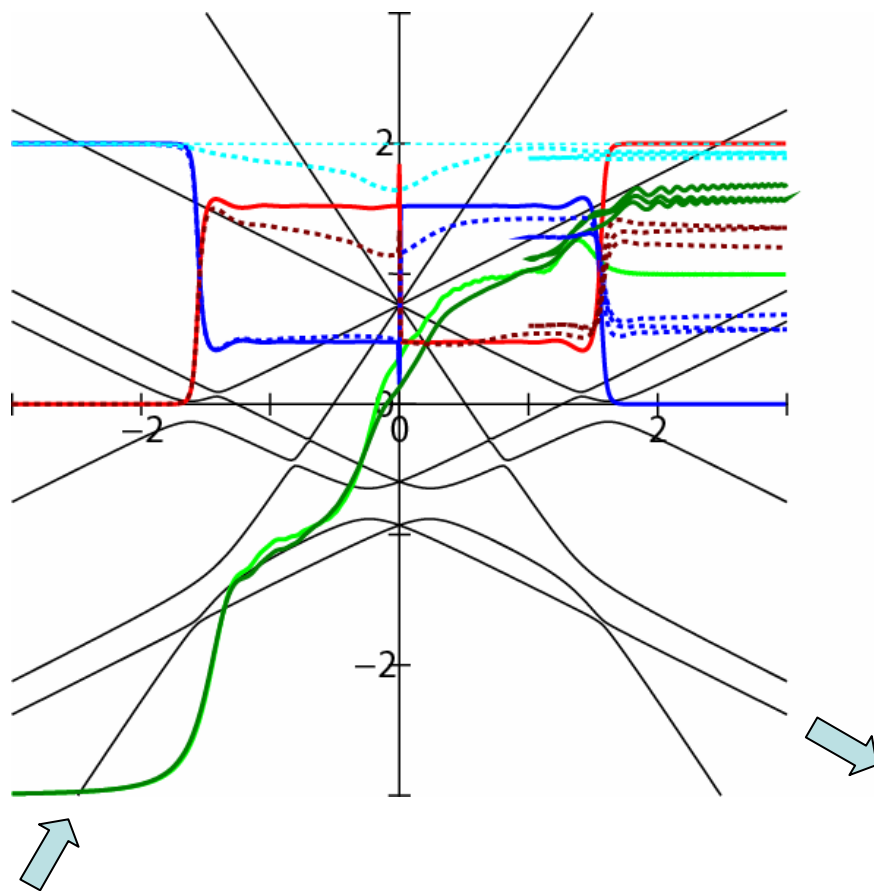
$\theta = 45^\circ$



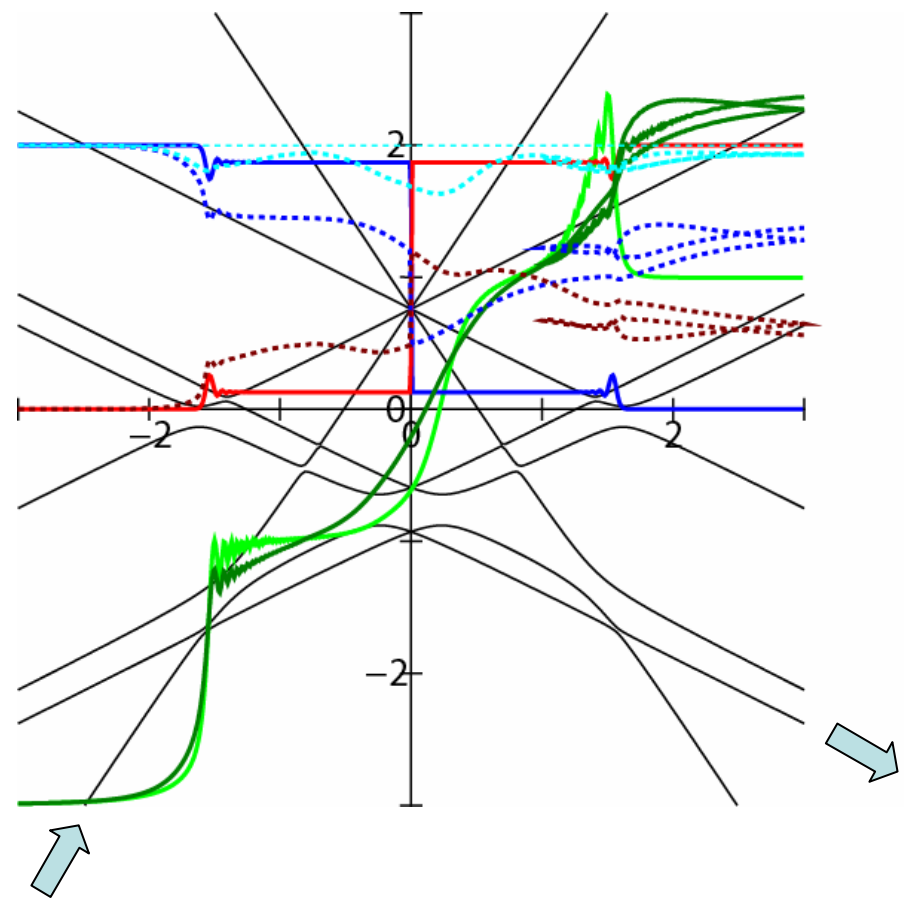
$\theta = 90^\circ$



Nontrivial coherence



$V=0.01$



$V=0.001$

Fluctuation-induced adiabatic transition

Temporal symmetry-breaking induced DM interaction

NaV₂O₅ : charge fluctuation reduces the symmetry

=> virtual DM ESR

Nojiri, et al.: JPSJ 69 (2000) 2291

Fe₁₂ : configuration fluctuation reduces the symmetry

=> virtual DM M(H)

H. Nakano and SM: JPSJ 71 (2002) 2580

SrCu₂(BO₃)₂ : configuration fluctuation reduces

the symmetry => Raman, ESR

Cepas and Zimann cond-mat 0401240

SM & Ogasahara: JPSJ 72 (2003) 2350

**Charge transfer, Phonon,
Orbital degree of freedom, etc.**

Fluctuation induced DM for a dimer

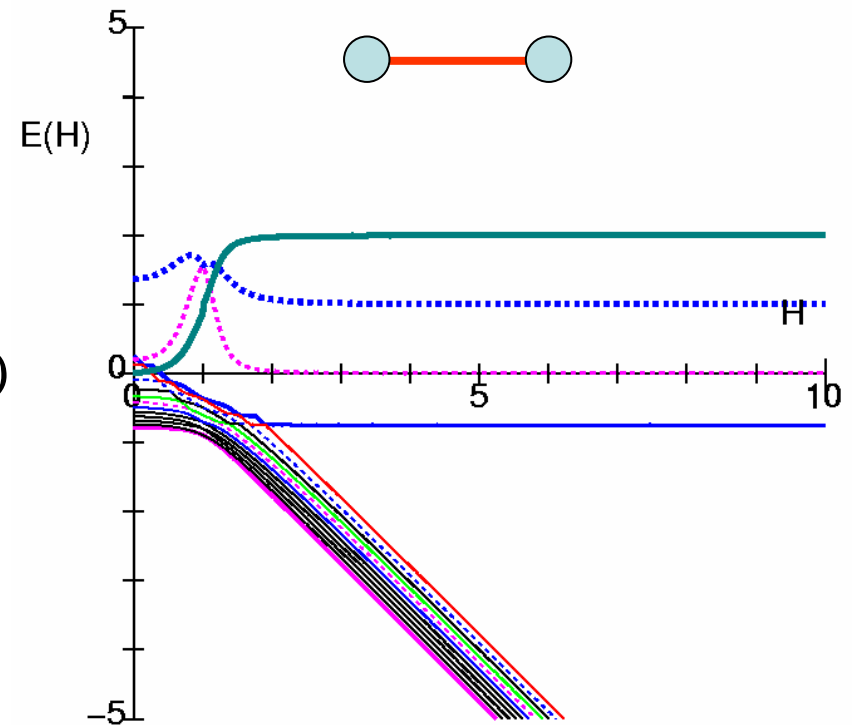
$$H = J \vec{S}_1 \cdot \vec{S}_2 + \vec{d} \cdot (\vec{S}_1 \times \vec{S}_2) + H(S_1^z + S_2^z) + \frac{k}{2} x^2 + \frac{1}{2m} p^2$$

$$\vec{d} = \vec{d}_0 x \quad [x, p] = i\hbar \quad \langle x \rangle = 0$$

$$H = H_{\text{Spin}} + H_{\text{SP}} + H_{\text{Phonon}}$$

$$\left\{ \begin{array}{l} H_{\text{Spin}} = J \vec{S}_1 \cdot \vec{S}_2 \\ H_{\text{SP}} = \sum_k (\alpha_k a_k^+ + \alpha_k^+ a_k) \vec{D} \cdot (\vec{S}_1 \times \vec{S}_2) \\ H_{\text{Phonon}} = \sum_k \omega_k a_k^+ a_k \end{array} \right.$$

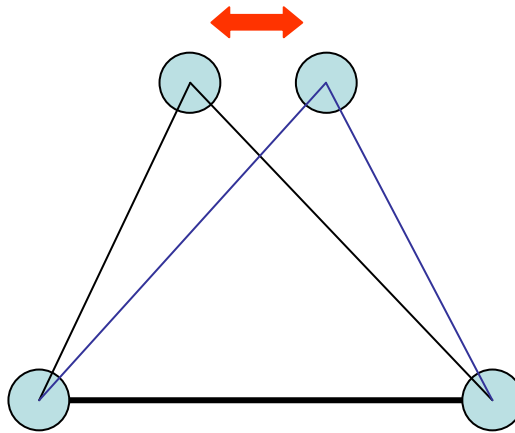
$m=10, \omega=0.1, D_x=0.1$



Effect of bond fluctuation

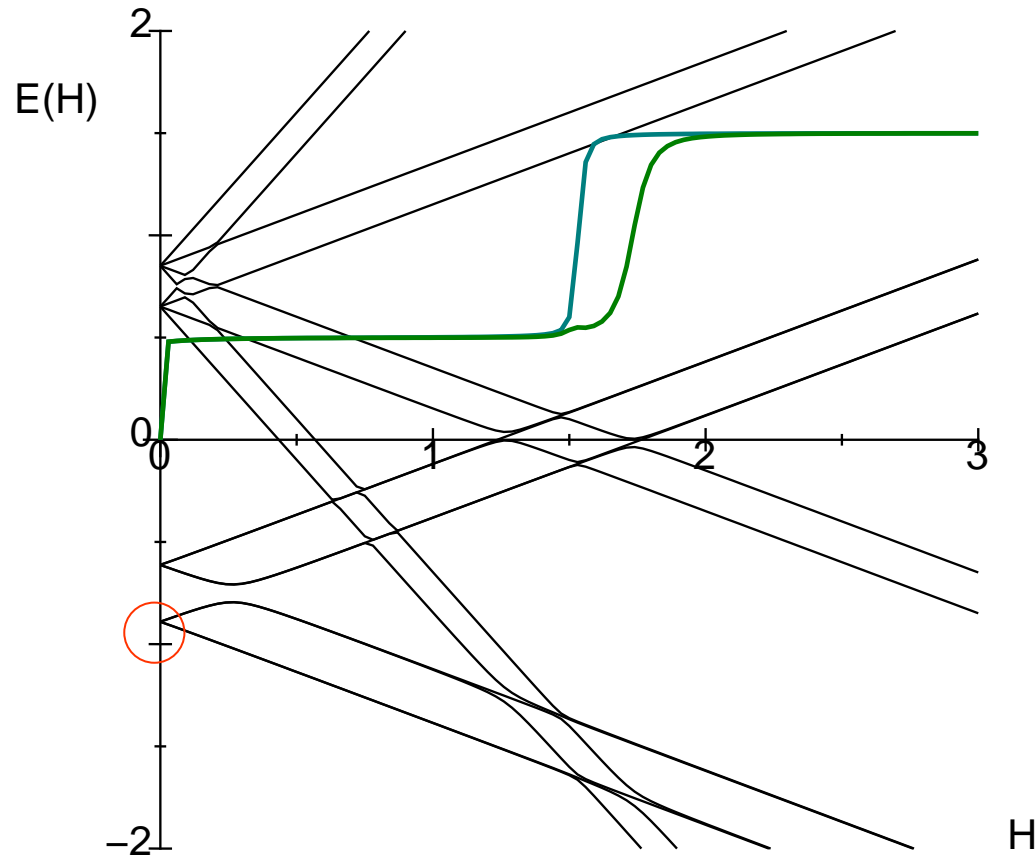
A minimal model

$$H = \sum_{\langle ij \rangle} \left(J_{ij} + \sigma^z \Delta J_{ij} \right) \vec{S}_i \cdot \vec{S}_j + \sigma^z \sum_{\langle ij \rangle} \vec{D}_{ij} \cdot \vec{S}_i \times \vec{S}_j + a \sigma^x$$

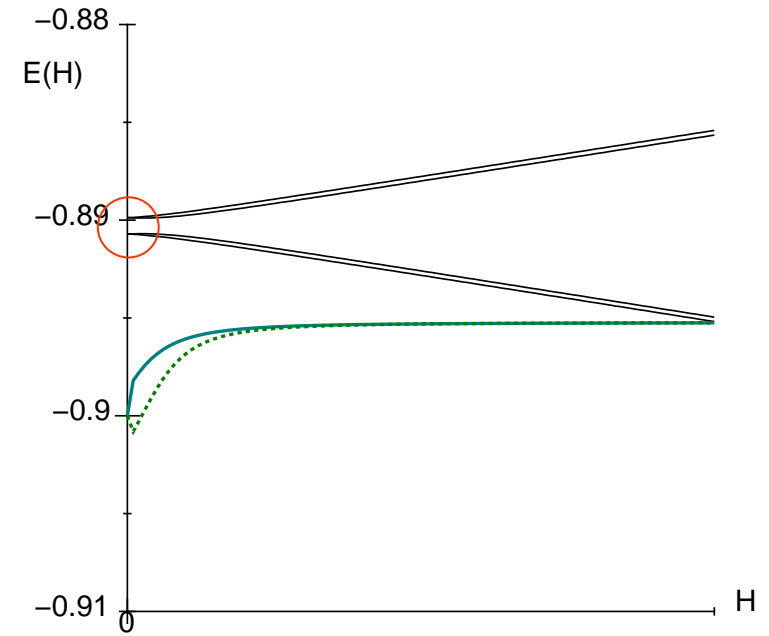


Small energy split at H=0

0.10 0.10 0.05 90



0.05 0.05 0.05 90



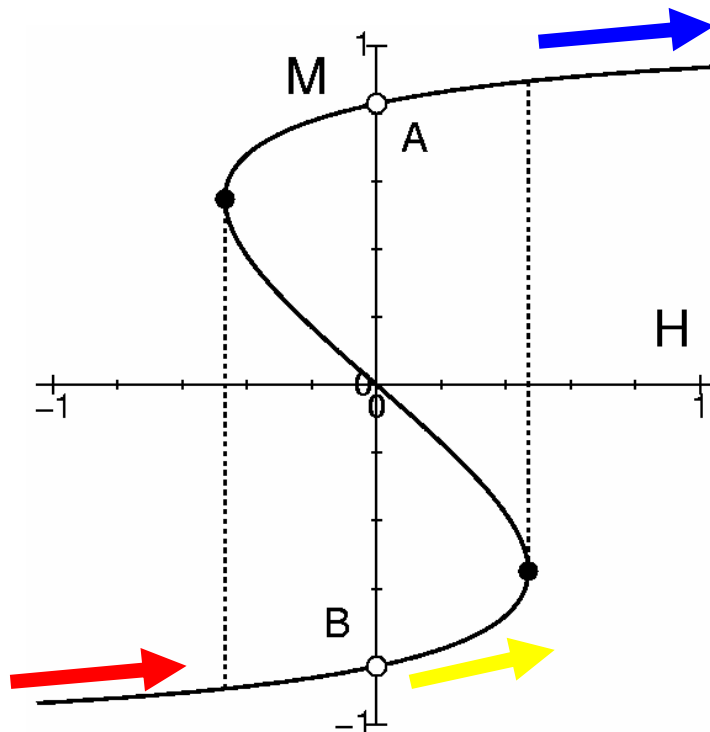
$\theta = 90^\circ$

Quantum Switching

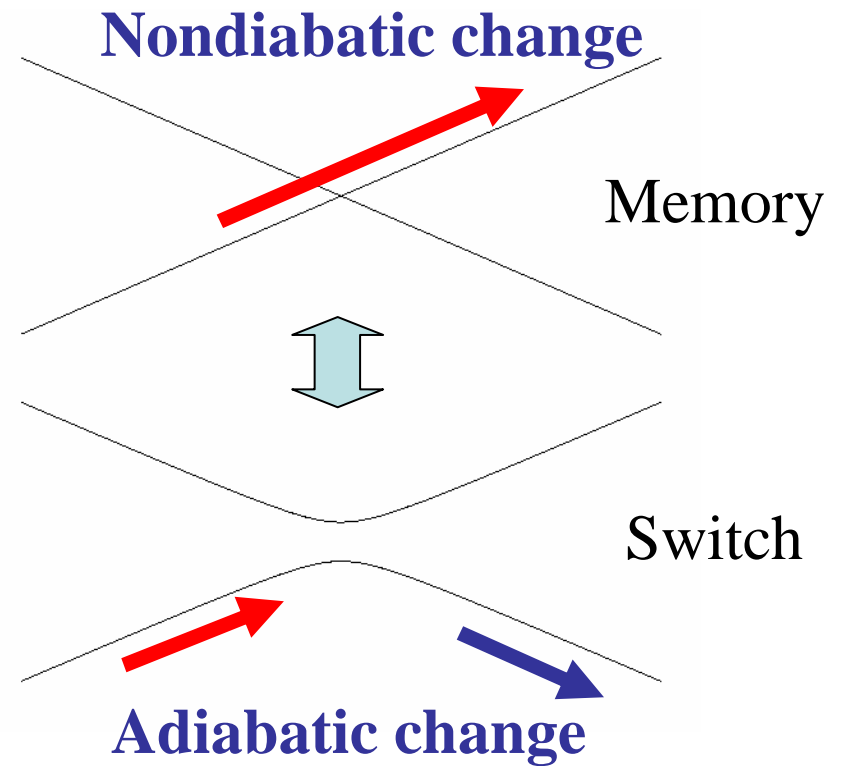
Memory: 2-values + Metastability

Classical: Hysteresis

Dissipation



Quantum: Dynamics

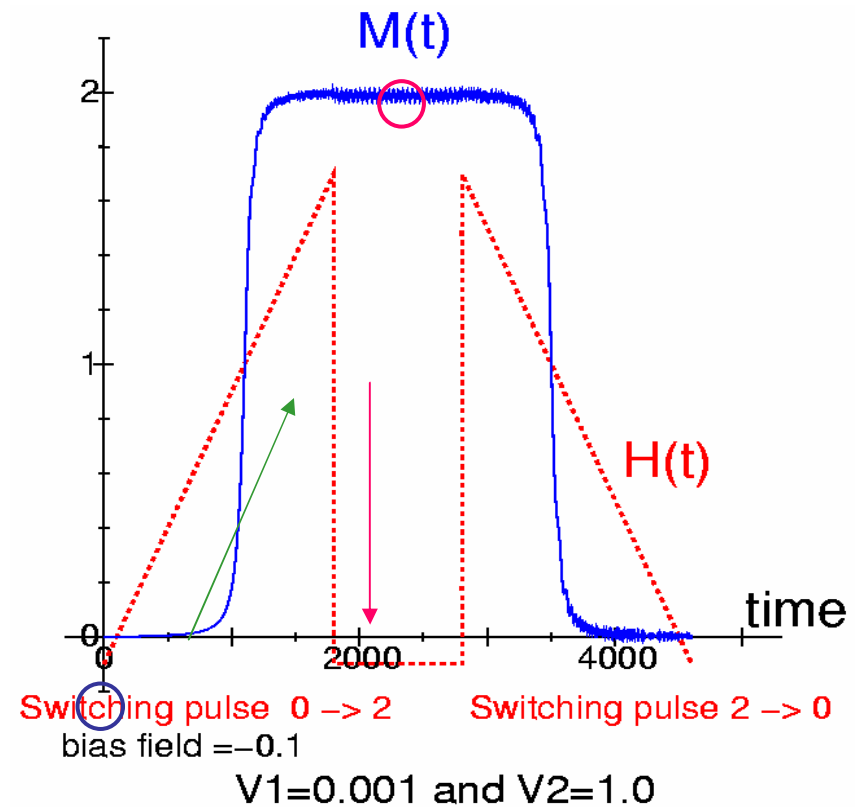
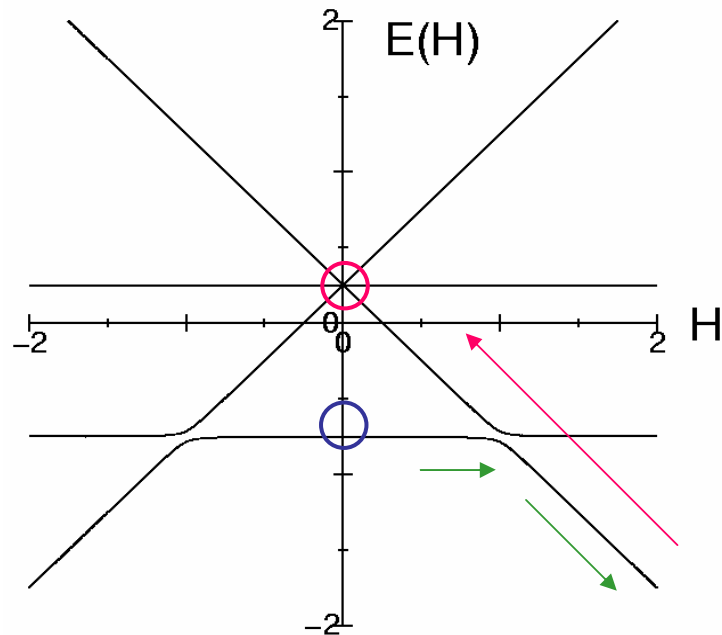


No Hysteresis loss

2. Sweeping velocity control

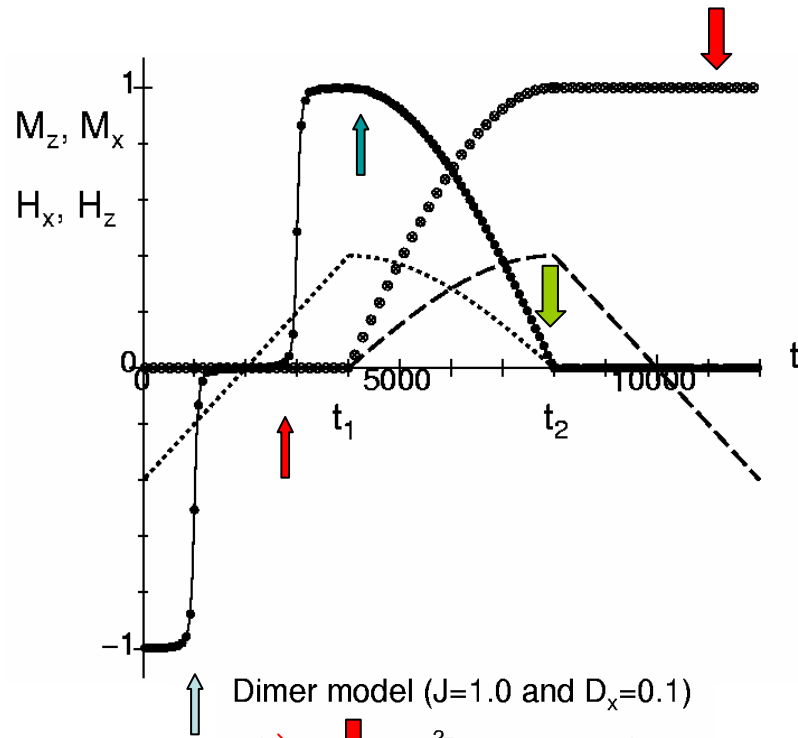
$$H = J \vec{S}_1 \cdot \vec{S}_2 - \vec{D} \cdot \vec{S}_1 \times \vec{S}_2 \quad \vec{D} = (0.1, 0, 0)$$

Dimer model ($J=1.0$ and $D_x=0.1$)

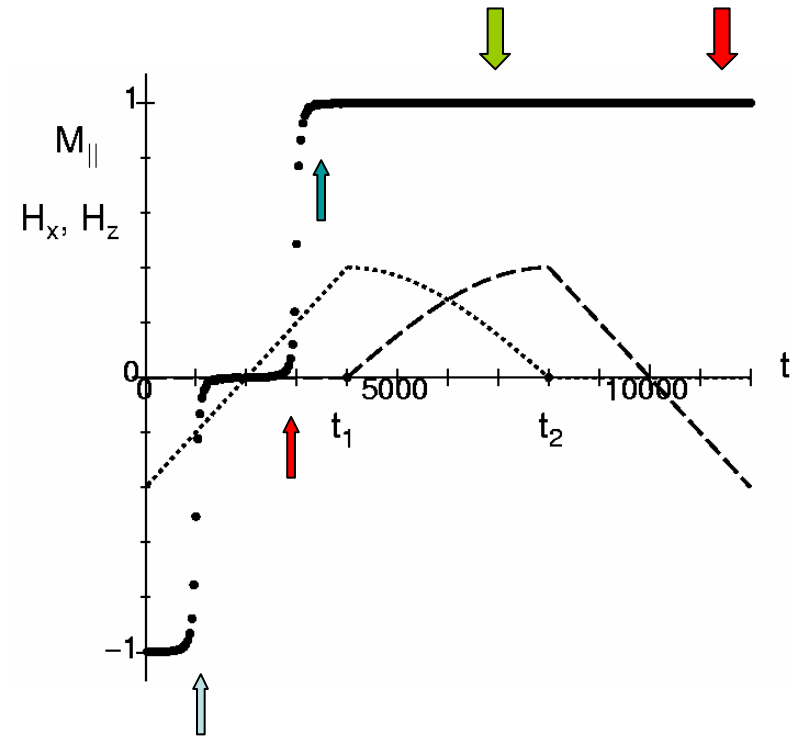
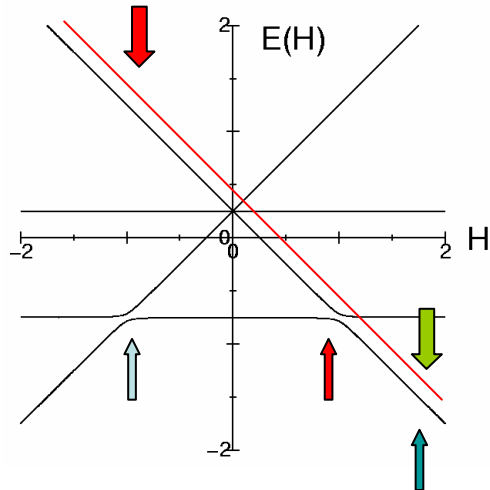


Switching between different S values

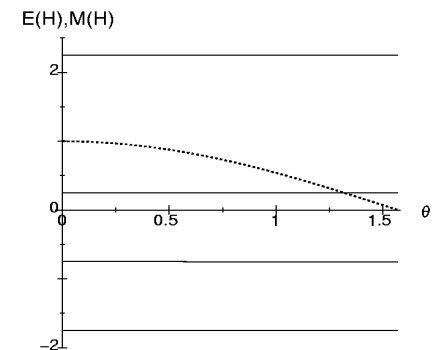
3. Rotation of the field (or sample)



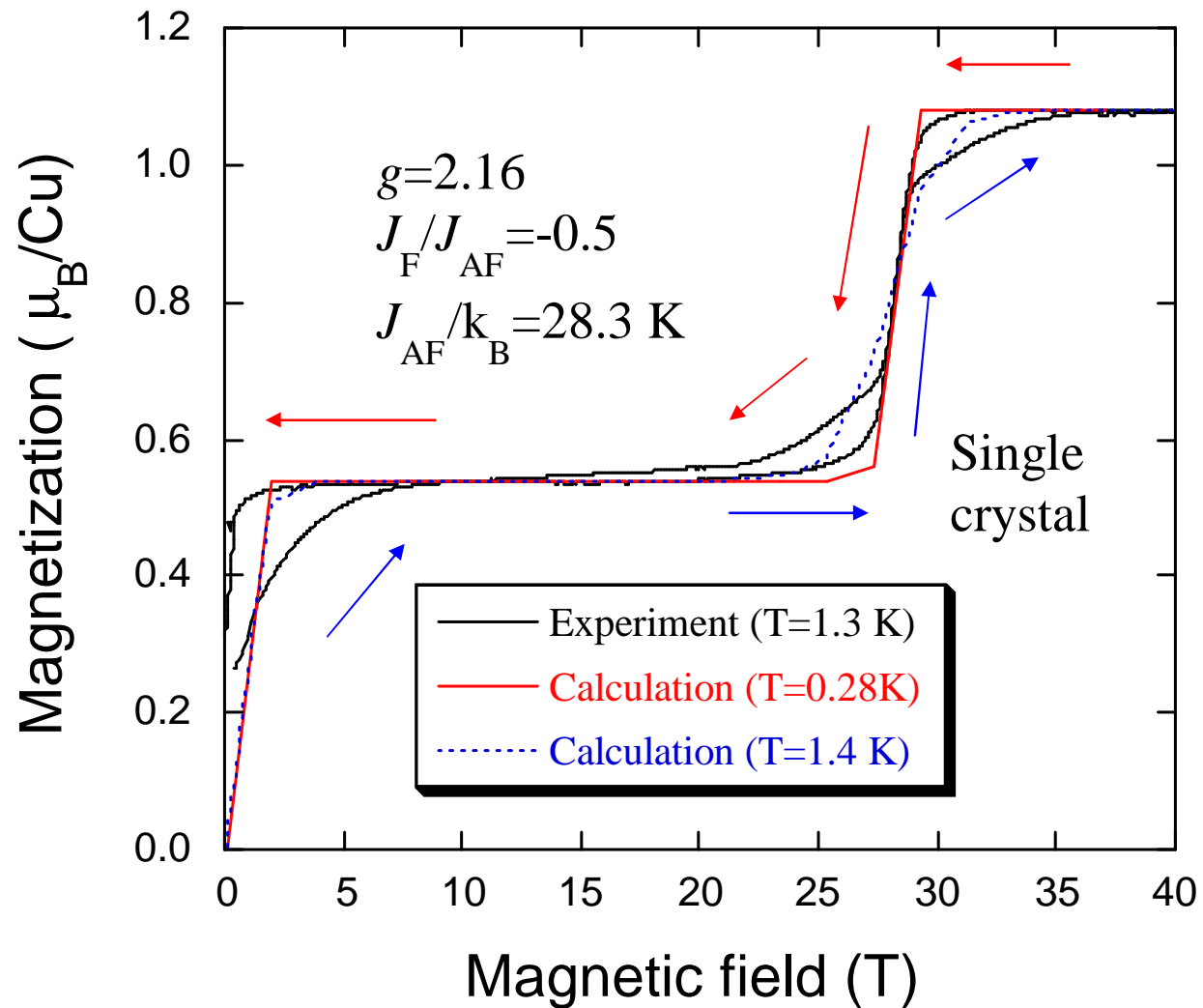
Dimer model ($J=1.0$ and $D_x=0.1$)



Rosen-Zener process



Magnetization as a function of magnetic field



Adiabatic
motion
in
Heisenberg
model

$$H = \sum_{ij} J_{ij} \vec{S}_i \cdot \vec{S}_j + Q - h(t) \sum_i S_i^z$$

$$M_x = \sum_i S_i^x, M_y = \sum_i S_i^y, M_z = \sum_i S_i^z$$

$$M_z(t) = e^{iHt/\hbar} M_z e^{-iHt/\hbar}$$

$$i\hbar \frac{\partial M_z(t)}{\partial t} = [M_z, H] = [M_z, Q], \text{ etc.}$$

$$Q = \Gamma M_x \quad Q - h(t) \sum_i S_i^z = -\vec{h} \cdot \vec{M}$$

$$i\hbar \frac{\partial \vec{M}}{\partial t} = [\vec{M}, -\vec{h} \cdot \vec{M}]$$

Torque equation

$$\frac{\partial \vec{M}}{\partial t} = \vec{M} \times \vec{h}$$

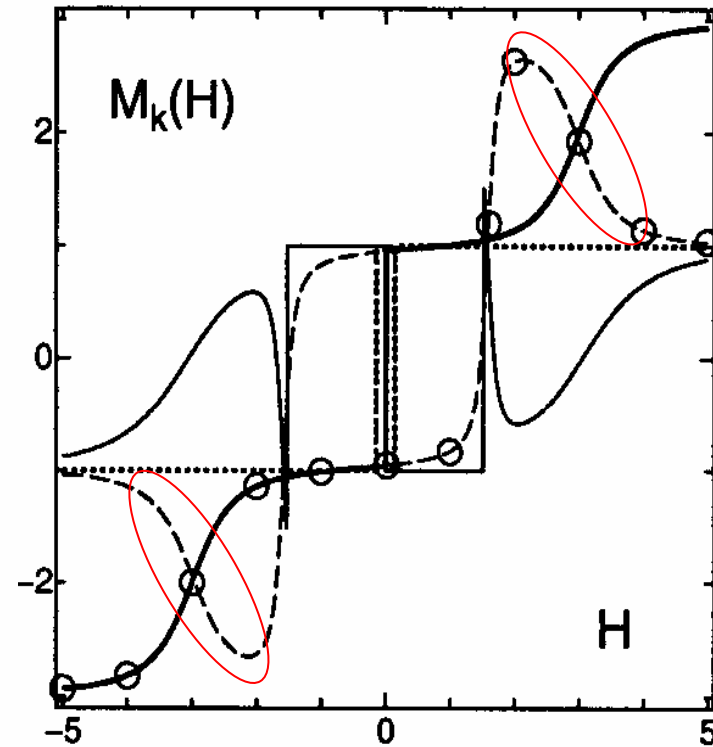
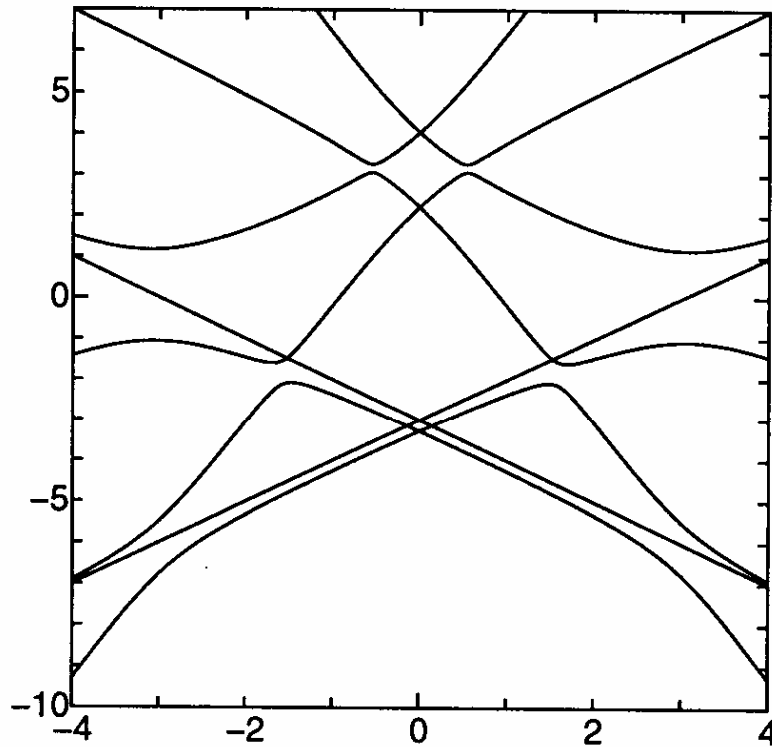
Response is the same as that of S=1/2 single spin

Weak coercive force

Quantum Control of state: Non Adiabatic Transitions

Non-monotonic magnetization process

SM, & N. Nagaosa, Prog. Theor. Phys. 106 (2001) 533



Observation and Control of the Quantum Dynamics

- **Magnetic field**
- Pressure
- Bias voltage
- Temperature
- Photo-irradiation
- etc.

Quantum Mechanical Response

- Molecular magnets:

isolation

Magnetic field

$$g\mu_B HS \quad 9.274 \times 10^{-24} [\text{J}]$$

- Electric polarization :

couple to

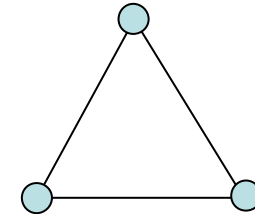
distortion

Electric field

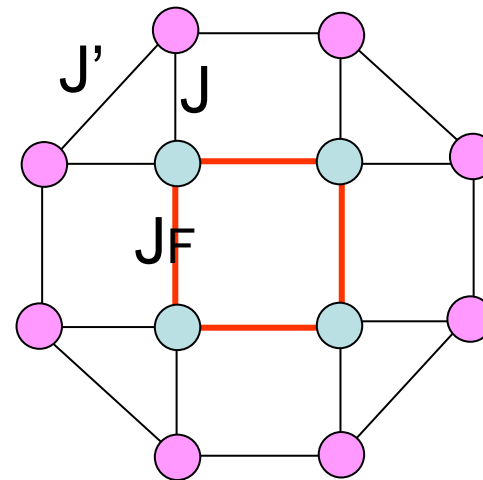
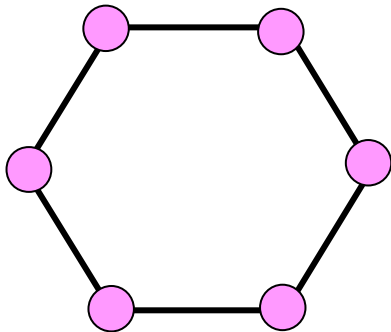
$$eE \quad 1.602 \times 10^{-19} [\text{J}]$$

Types of microscopic spin states

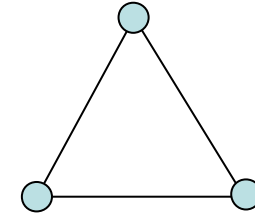
- Triangle lattice and odd rings
- Even rings
- New types of microscopic spin state



Non-collinear ferrimagnetism



Local magnetization



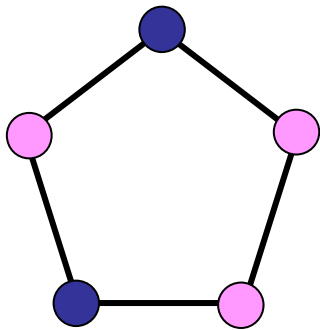
Distorted case (without C3 symmetry)

$$\begin{array}{ccc} \langle S_1 \rangle, & \langle S_2 \rangle, & \langle S_3 \rangle \\ + & - & + \end{array} \quad \langle S_1 + S_2 + S_3 \rangle = \frac{1}{2}$$

with C3 symmetry

$$\begin{array}{ccc} \langle S_1 \rangle, & \langle S_2 \rangle, & \langle S_3 \rangle \\ ? & ? & ? \end{array} \quad \langle S_1 + S_2 + S_3 \rangle = \frac{1}{2}$$

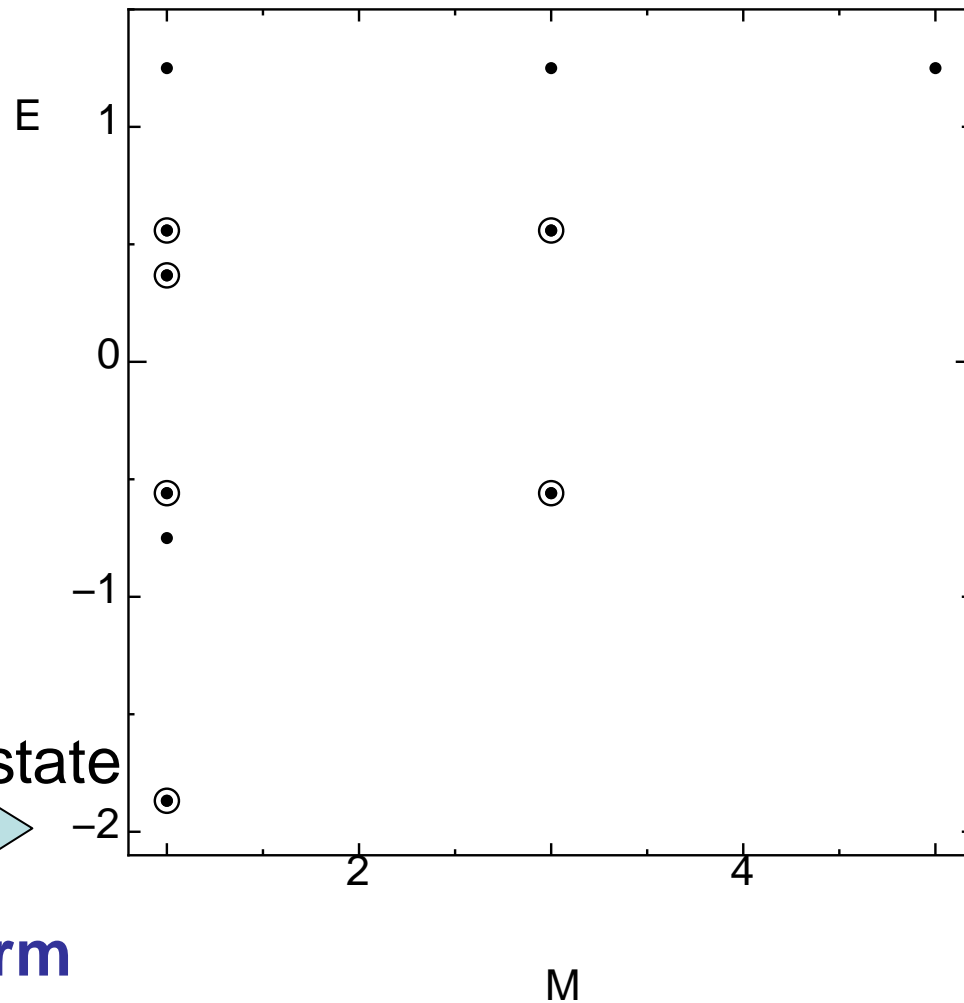
Odd ring $N=5$



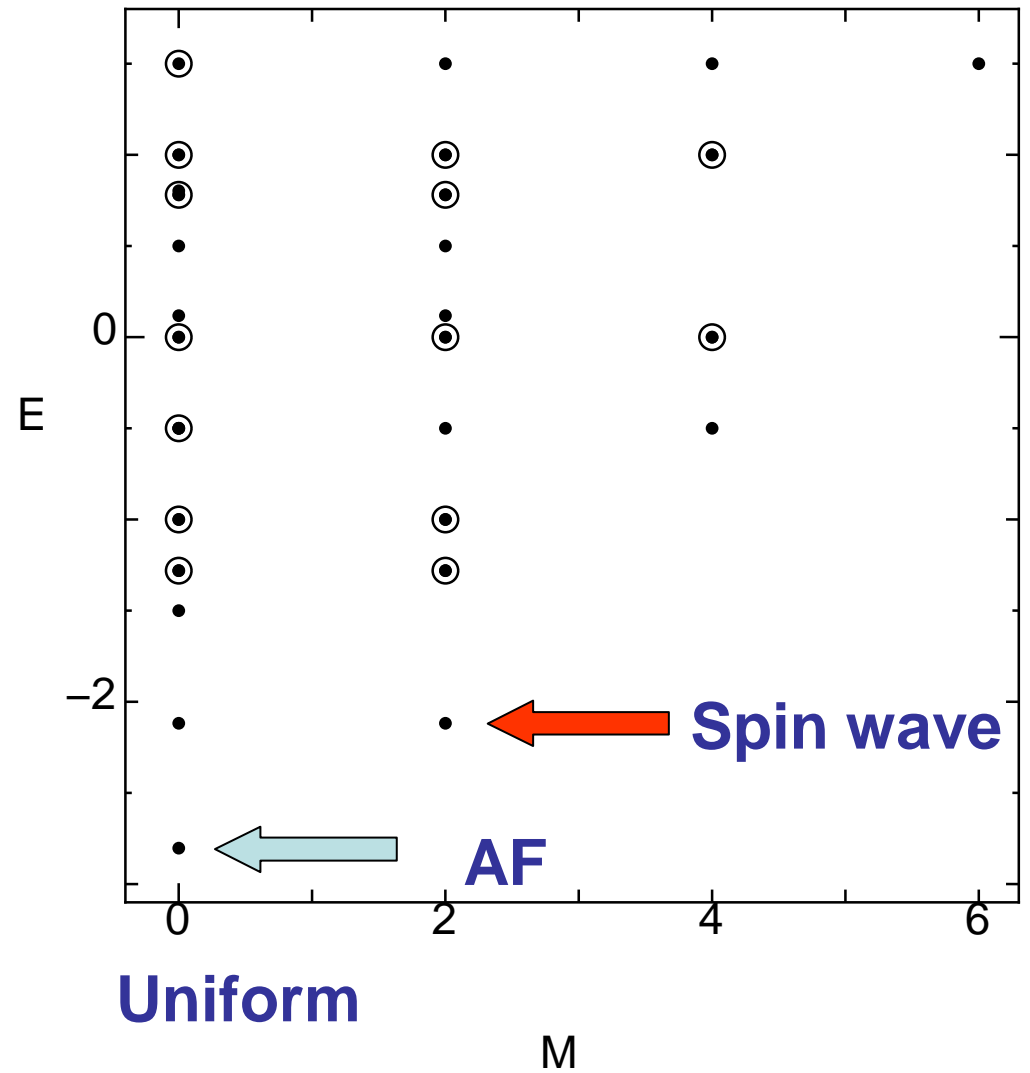
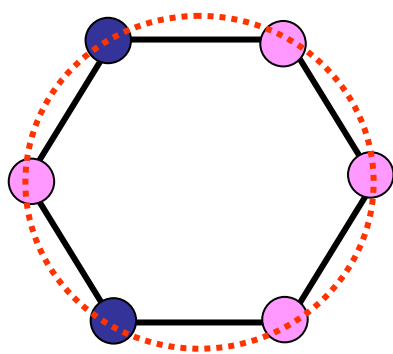
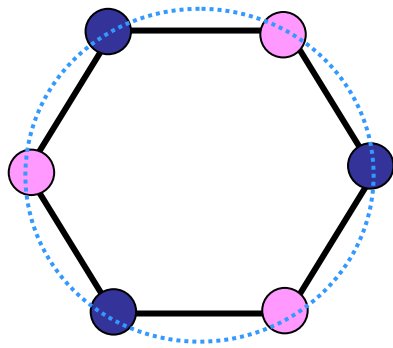
Degenerate ground state



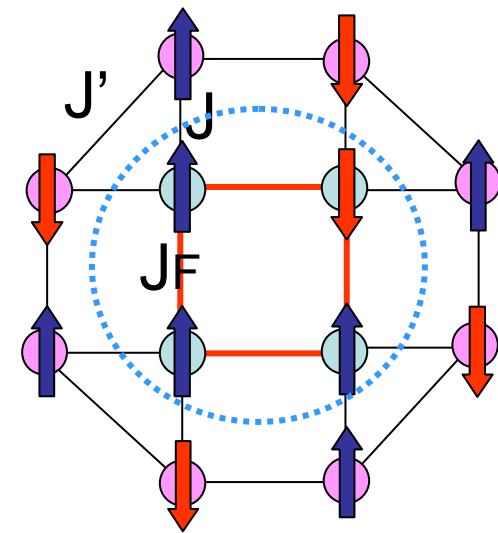
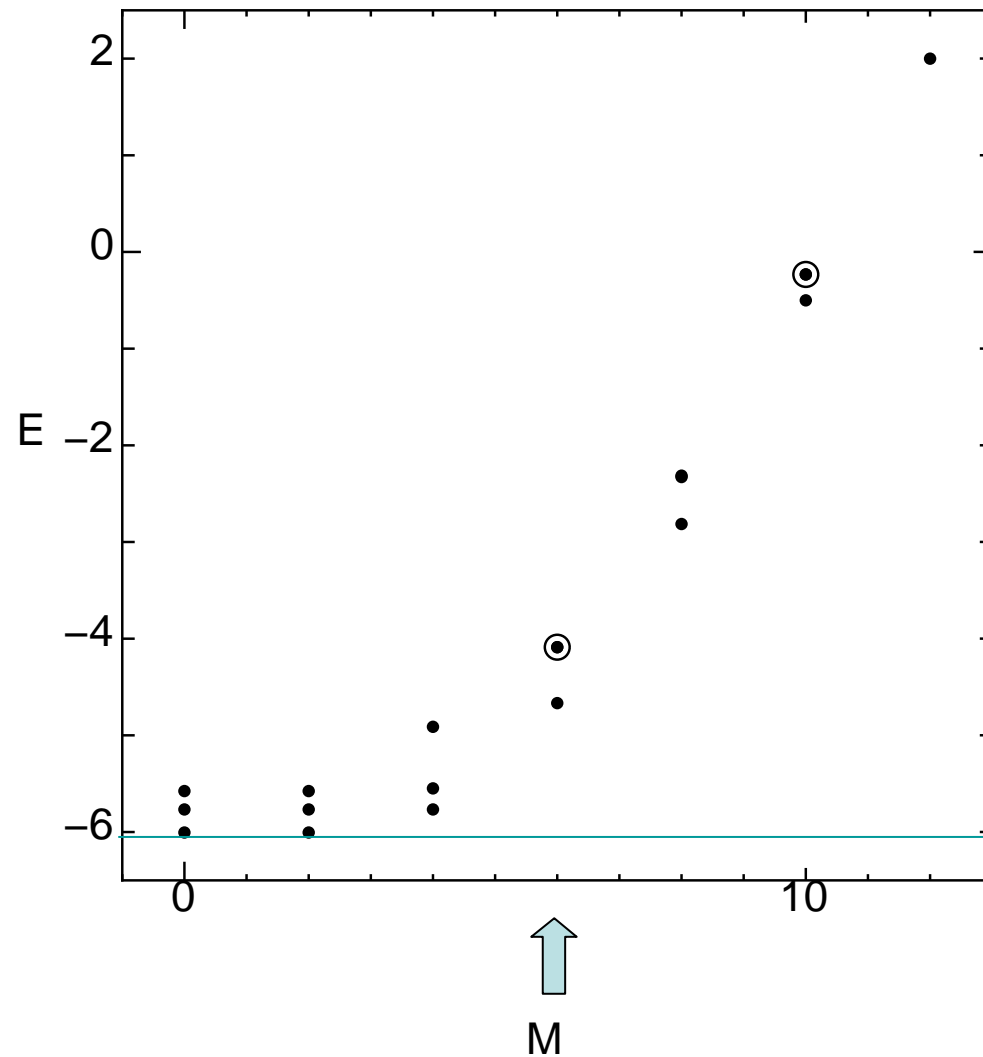
Non-uniform



Even spin case $N=6$



N=12 Non-collinear Ferrimagnetism

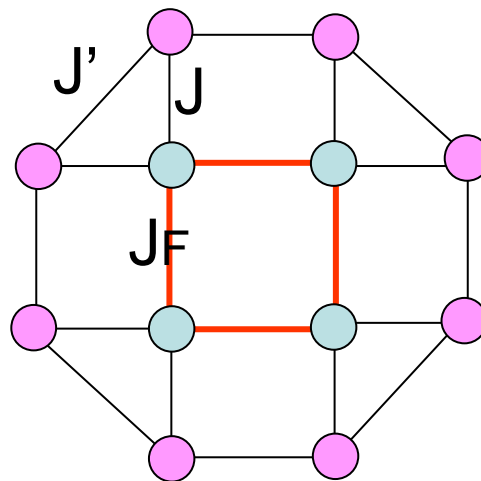


$$J=J'=1, J_F=2$$

Uniformly fluctuating magnetic state?

Spin wave type $|\Psi\rangle = \frac{1}{\sqrt{3}} (|++-\rangle + |+-+\rangle + |-++\rangle)$

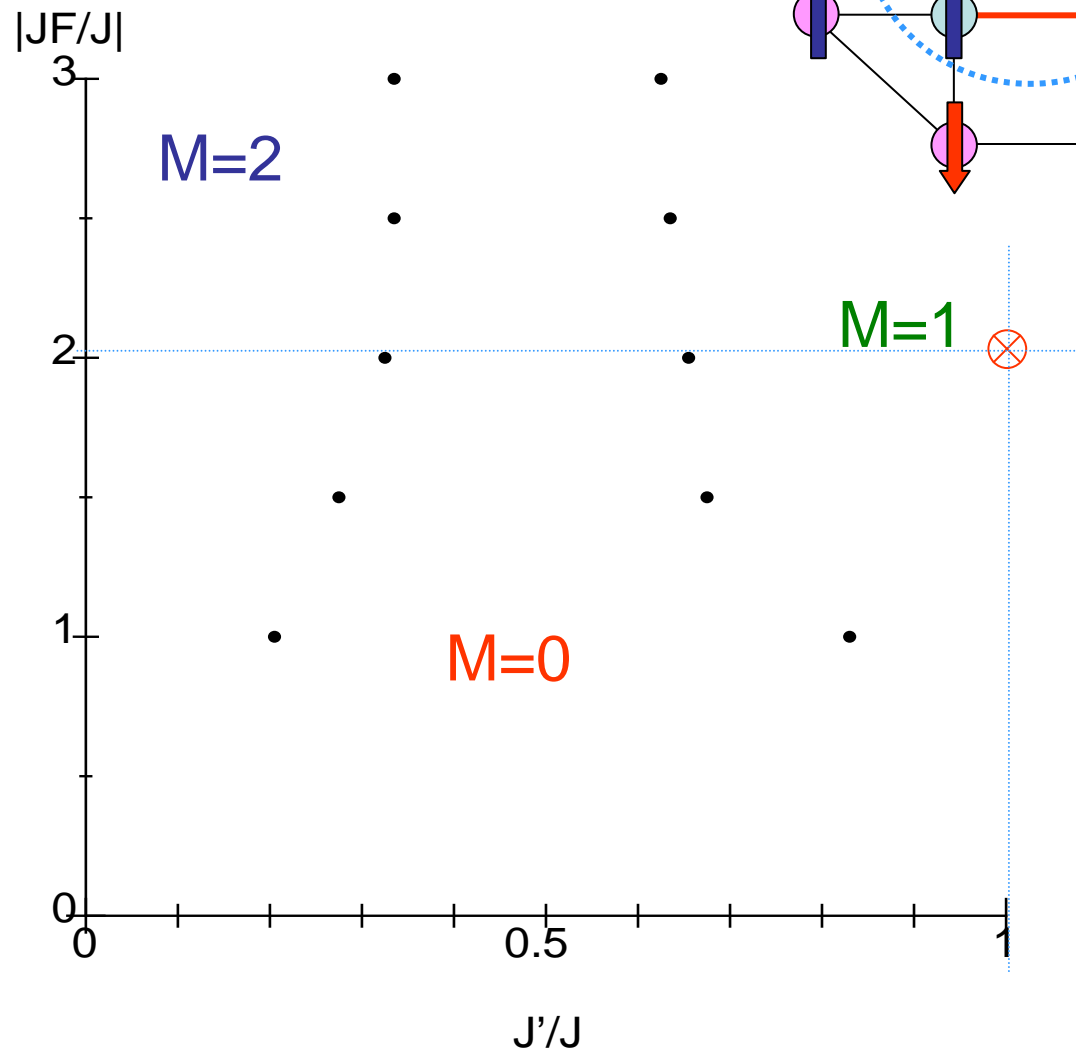
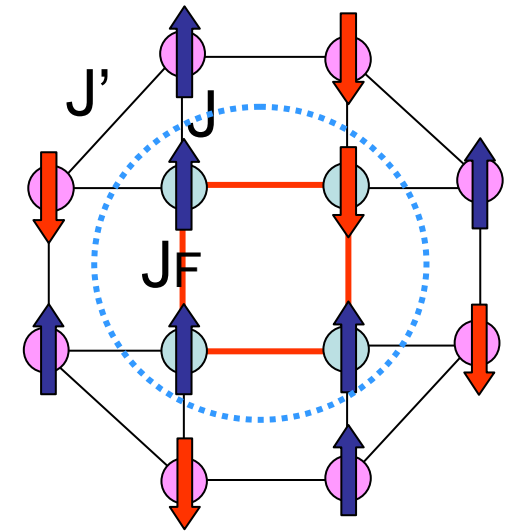
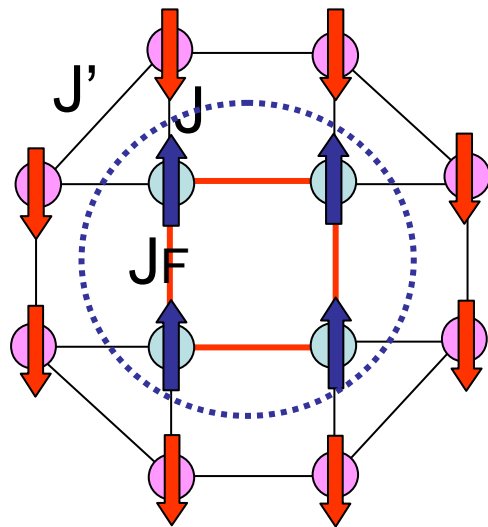
Non-collinear ferrimagnetic state: ground state



$J \gg J' : \text{LMFR}$

$J \ll J' : \text{Non-LMFR}$

LM & Non-Collinear ferrimagnetism

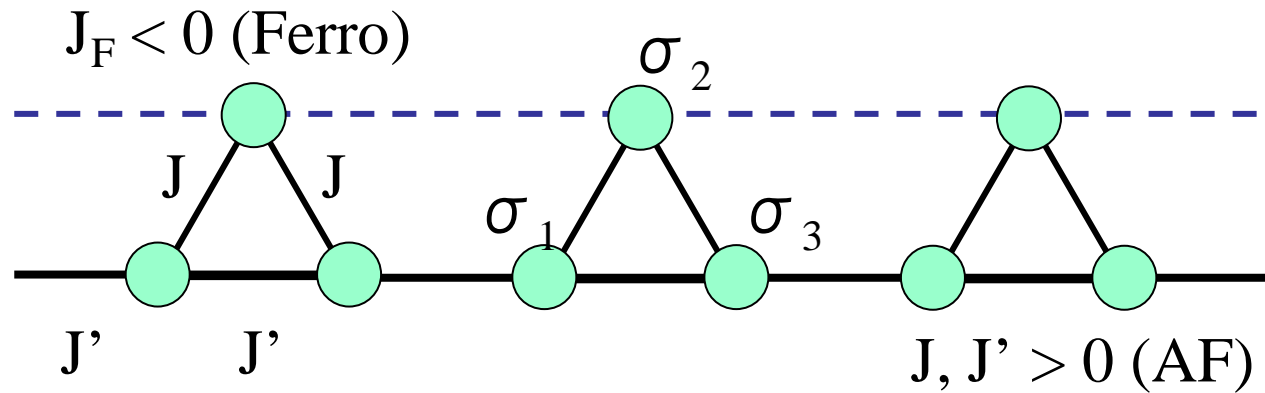


Uniform nonzero magnetization in the ground state?

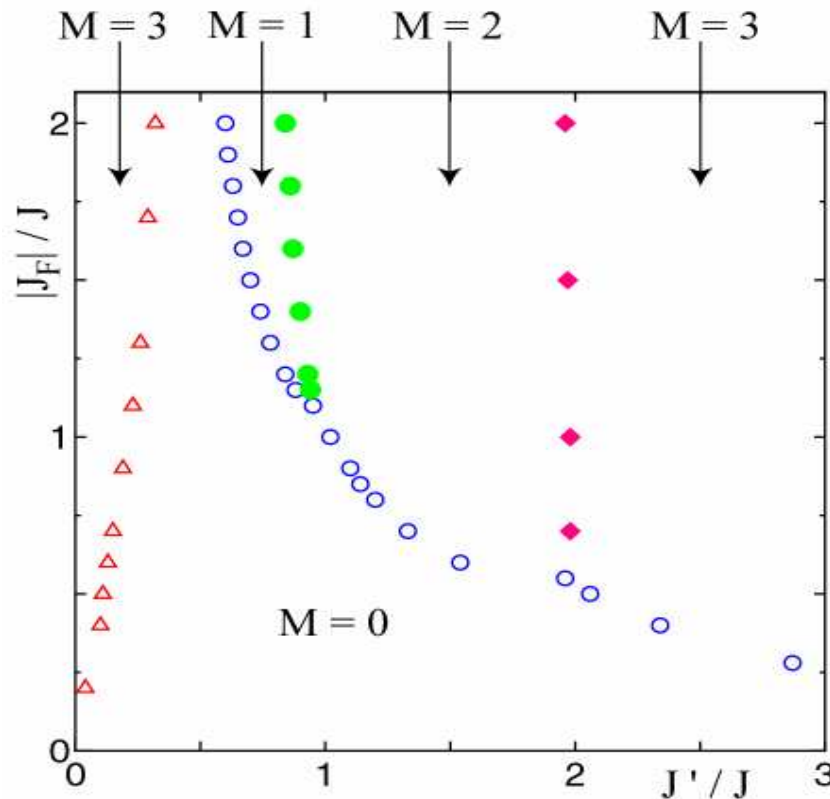
Ferri-magnetic state

- Lieb-Mattis type
 Localized magnetic moment
- Non-collinear type
 Uniform magnetic moment

Non-saturated magnetized state



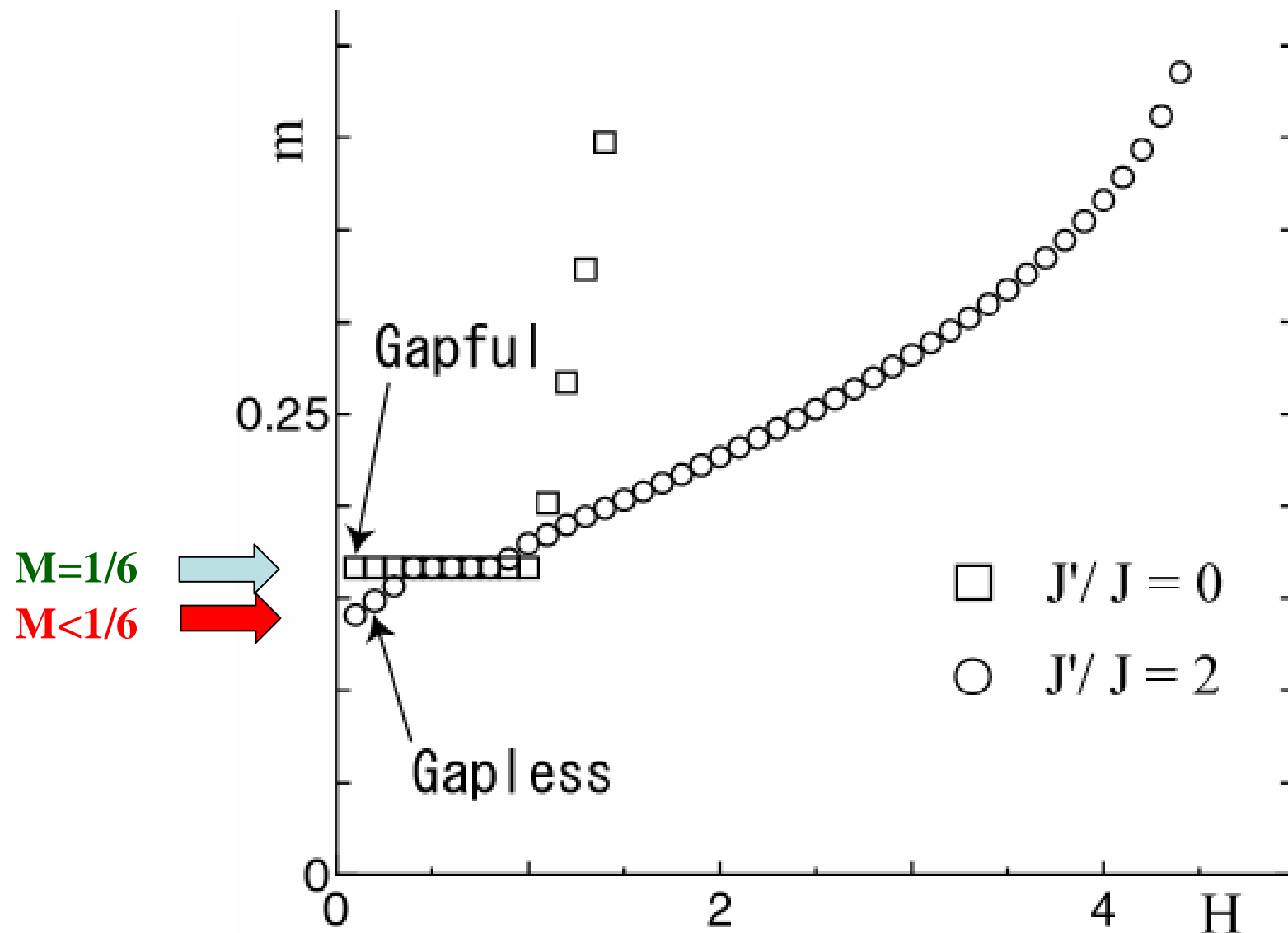
$N=18$



$J \gg J' : \text{LMFR}$

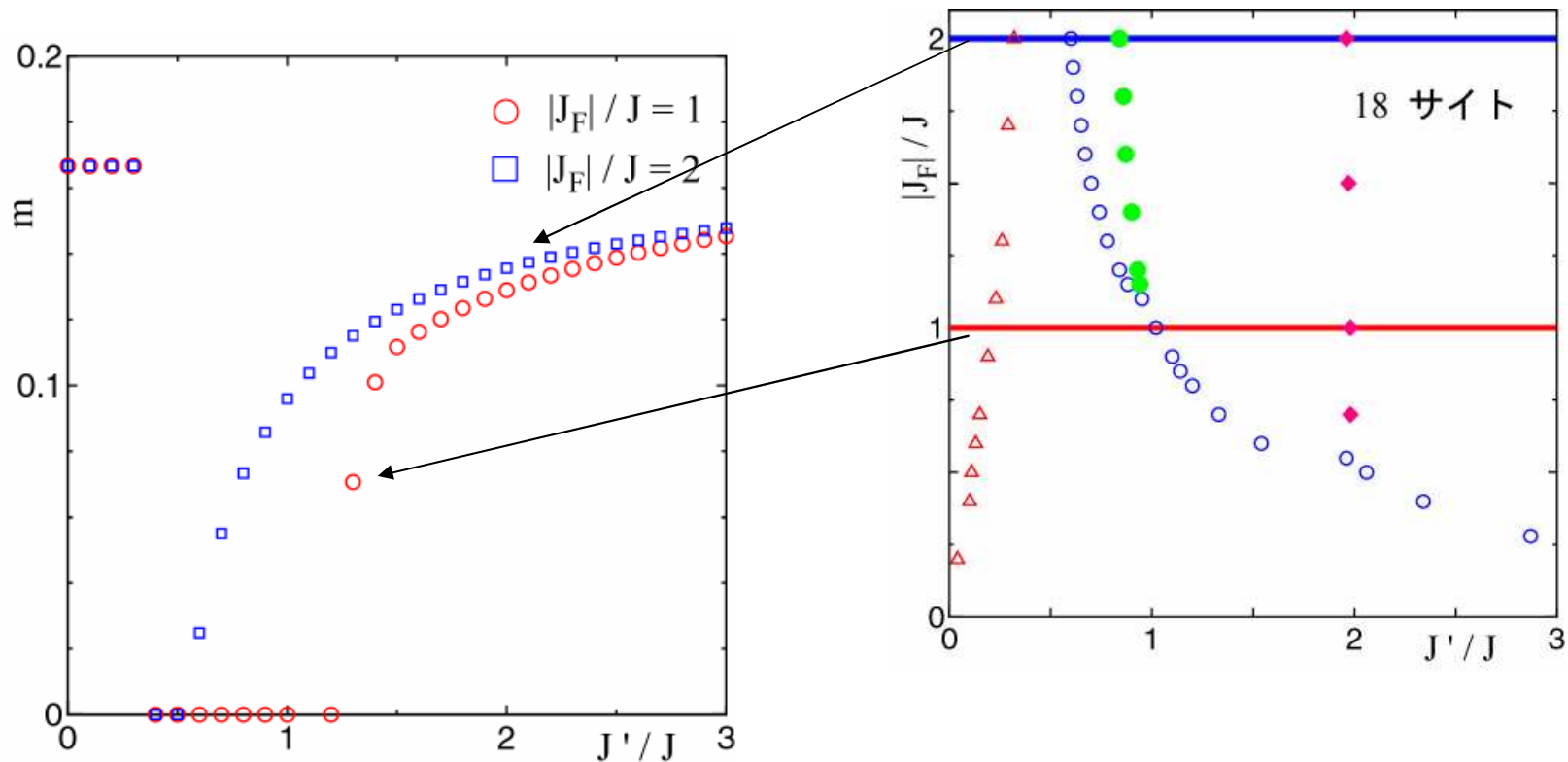
$J \ll J' : \text{Non-LMFR}$

Magnetization processes



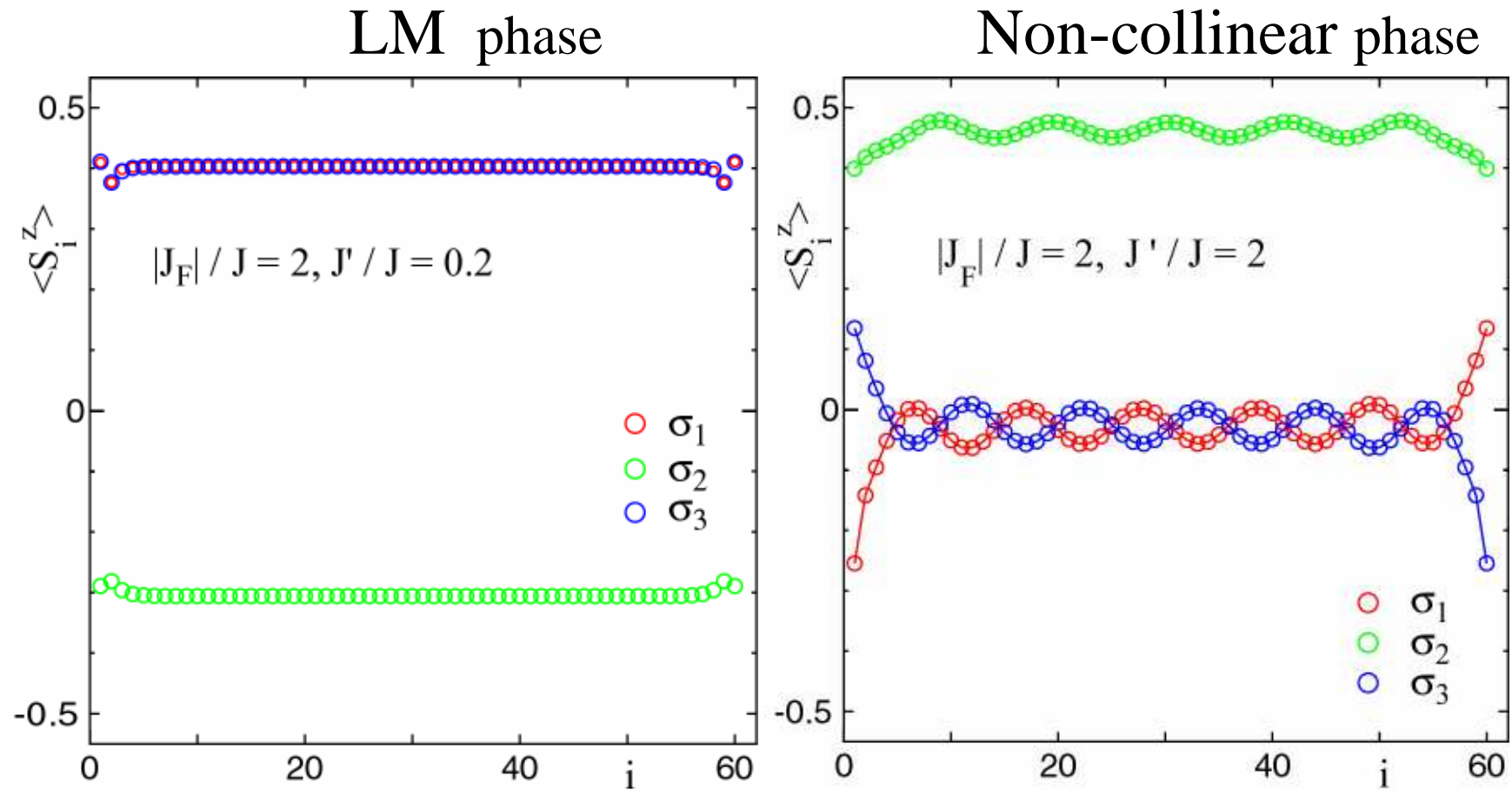
Phase diagram

J_F fixed



As J' increases the jump of the magnetization becomes large.

Local magnetic structures



3×60